

2016

The Economics of Food and Agricultural Markets

Andrew Barkley

Kansas State University, barkley@ksu.edu

Follow this and additional works at: <http://newprairiepress.org/ebooks>



Part of the [Agricultural Economics Commons](#), and the [Higher Education Commons](#)

Recommended Citation

Barkley, Andrew, "The Economics of Food and Agricultural Markets" (2016). *NPP eBooks*. 12.
<http://newprairiepress.org/ebooks/12>

This Book is brought to you for free and open access by the Monographs at New Prairie Press. It has been accepted for inclusion in NPP eBooks by an authorized administrator of New Prairie Press. For more information, please contact cads@k-state.edu.

2016

The Economics of Food and Agricultural Markets

Andrew Barkley

Kansas State University, barkley@ksu.edu

Follow this and additional works at: <http://newprairiepress.org/ebooks>



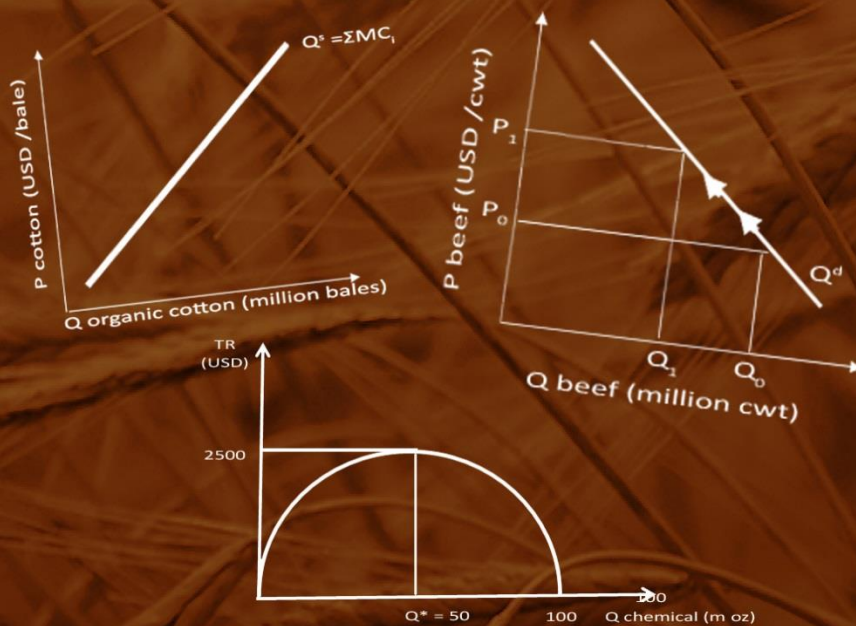
Part of the [Agricultural Economics Commons](#), and the [Higher Education Commons](#)

Recommended Citation

Barkley, Andrew, "The Economics of Food and Agricultural Markets" (2016). *NPP eBooks*. 12.
<http://newprairiepress.org/ebooks/12>

This Book is brought to you for free and open access by the Monographs at New Prairie Press. It has been accepted for inclusion in NPP eBooks by an authorized administrator of New Prairie Press. For more information, please contact cads@k-state.edu.

THE ECONOMICS OF FOOD AND AGRICULTURAL MARKETS



Andrew Barkley

The Economics of Food and Agricultural Markets

Andrew Barkley

NEW prairie PRESS


open access scholarly publishing

Copyright © 2016 Andrew Barkley

New Prairie Press
Kansas State University Libraries
Manhattan, Kansas

Cover design by: Kansas State University Libraries

Electronic edition available online at: <http://newprairiepress.org/ebooks/12>

This work is licensed under a Creative Commons
Attribution 4.0 International License
<http://creativecommons.org/licenses/by/4.0/>

ISBN-13: 978-1-944548-05-6

Table of Contents

The Economics of Food and Agricultural Markets

Chapter 1. Introduction to Economics

- 1.1 Introduction to the Study of Economics
 - 1.1.1 Economics is Important and Interesting!
 - 1.1.2 Scarcity
 - 1.1.3 Microeconomics and Macroeconomics
 - 1.1.4 Economic Models and Theories
 - 1.1.4.1 The Scientific Method
 - 1.1.5 Positive Economics and Normative Economics

- 1.2 Supply and Demand
 - 1.2.1 Supply
 - 1.2.1.1 Properties of Supply
 - 1.2.1.2 The Determinants of Supply
 - 1.2.1.3 Movements along vs. Shifts In Supply
 - 1.2.2 Demand
 - 1.2.2.1 Properties of Demand
 - 1.2.2.2 The Determinants of Demand
 - 1.2.2.3 Movements along vs. Shifts In Demand

- 1.3 Markets
 - 1.3.1 Competitive Market Properties
 - 1.3.2 Outcomes of Competitive Markets
 - 1.3.3 Supply and Demand Shift Examples
 - 1.3.3.1 Demand Increase
 - 1.3.3.2 Demand Decrease
 - 1.3.3.3 Supply Decrease
 - 1.3.3.4 Supply Increase
 - 1.3.4 Mathematics of Supply and Demand

- 1.4 Elasticities
 - 1.4.1 Introduction to Elasticities
 - 1.4.2 Own Price Elasticity of Demand: E_d
 - 1.4.2.1 Price Elasticity of Demand Example
 - 1.4.2.2 Elastic and Inelastic Demand Examples

- 1.4.3 Own Price Elasticity of Supply: E_s
- 1.4.4 Income Elasticity: E_i
- 1.4.5 Cross-Price Elasticity of Demand: E_{dxy}
- 1.4.6 Cross-Price Elasticity of Supply: E_{sxy}
- 1.4.7 Price Elasticities and Time
- 1.4.8 Elasticities of Demand along a Linear Demand Curve
- 1.4.9 Agricultural Policy Example of Elasticity of Demand
- 1.4.10 Calculation of Market Supply and Demand Elasticities

- 1.5 Welfare Economics: Consumer and Producer Surplus
 - 1.5.1 Introduction to Welfare Economics
 - 1.5.2 Consumer Surplus and Producer Surplus
 - 1.5.3 Mathematics of Welfare Economics: Phone Market

- 1.6 The Motivation for and Consequences of Free Trade
 - 1.6.1 The Motivation for Free Trade and Globalization
 - 1.6.2 Excess Supply and Excess Demand
 - 1.6.3 Three-Panel Diagram of Free Trade between Two Nations
 - 1.6.4 Welfare Impacts of International Trade

Chapter 2. Welfare Analysis of Government Policies

- 2.1 Price Ceiling
 - 2.1.1 Welfare Analysis
 - 2.1.2 Quantitative Analysis

- 2.2 Price Support
 - 2.2.1 Case One: Price Support with No Surplus
 - 2.2.2 Case Two: Price Support When Surplus Exists
 - 2.2.3 Case Three: Price Support When Government Purchases Surplus
 - 2.2.4 Quantitative Analysis of a Price Support

- 2.3 Quantity Control (Supply Control)

- 2.4 Import Quota
 - 2.4.1 Welfare Analysis of an Import Quota
 - 2.4.2 Quantitative Welfare Analysis of an Import Quota

- 2.5 Taxes
 - 2.5.1 Welfare Analysis of a Tax

2.5.2 Quantitative Welfare Analysis of a Tax

2.6 Subsidies

2.6.1 Welfare Analysis of a Subsidy

2.6.2 Quantitative Welfare Analysis of a Subsidy

Chapter 3. Market Power: Monopoly and Monopsony

3.1 Market Power Introduction

3.2 Monopoly Profit-Maximizing Solution

3.2.1 Monopoly Revenues

3.2.2 Monopoly Costs

3.2.3 Monopoly Profit-Maximizing Solution

3.3 Marginal Revenue and the Elasticity of Demand

3.3.1 The Monopolist's Tradeoff between Price and Quantity

3.3.2 The Tradeoff between MR and E_d

3.3.3 Pricing Rule One

3.4 Monopoly Characteristics

3.4.1 The Absence of a Supply Curve for a Monopolist

3.4.2 The Effect of a Tax on a Monopolist's Price

3.4.3 Multiplant Monopoly

3.5 Monopoly Power

3.5.1 The Lerner Index of Monopoly Power

3.5.2 Welfare Effects of Monopoly

3.5.3 Sources of Monopoly Power

3.5.4 Natural Monopoly

3.6 Monopsony

3.6.1 Terminology of Monopsony

3.6.2 Sources of Monopsony Power

3.6.3 Welfare Effects of Monopsony

Chapter 4. Pricing with Market Power

4.1 Introduction to Pricing with Market Power

4.2 Price Discrimination

- 4.2.1 First Degree Price Discrimination
- 4.2.2 Second Degree Price Discrimination
- 4.2.3 Third Degree Price Discrimination

4.3 Intertemporal Price Discrimination

4.4 Peak Load Pricing

4.5 Two Part Pricing

4.6 Bundling

- 4.6.1 Bundling Examples
- 4.6.2 Tying

4.7 Advertising

- 4.7.1 Graphical Analysis
- 4.7.2 General Rule for Advertising

Chapter 5. Monopolistic Competition and Oligopoly

5.1 Market Structures

- 5.1.1 Market Structure Spectrum and Characteristics
- 5.1.2 Review of Perfect Competition
- 5.1.3 Review of Monopoly

5.2 Monopolistic Competition

- 5.2.1 Monopolistic Competition in the Short and Long Runs
- 5.2.2 Economic Efficiency and Monopolistic Competition

5.3 Oligopoly

- 5.3.1 Strategic Interactions
- 5.3.2 Cournot Model
- 5.3.3 Bertrand Model
- 5.3.4 Stackelberg Model
- 5.3.5 Collusion and Game Theory
- 5.3.6 Rigid Prices: Kinked Demand Curve Model
- 5.3.7 Dominant Firm Model: Price Leadership
- 5.3.8 Cartels

Chapter 6. Game Theory One

6.1 Game Theory Introduction

6.2 Equilibrium in Dominant Strategies

6.2.1 Prisoner's Dilemma: Dominant Strategy

6.3 Nash Equilibrium

6.3.1 Prisoner's Dilemma: Nash Equilibrium

6.4 Advertising Game

6.4.1 Advertising: Dominant Strategy

6.4.2 Advertising: Nash Equilibria

6.5 Maximin Strategy (Safety First)

6.5.1 Prisoner's Dilemma: Maximin Strategy (Safety First)

6.5.2 Advertising Game: Maximin Strategy (Safety First)

6.6 Cooperative Strategy (Collusion)

6.7 Game Theory Example: Steak Pricing Game

6.7.1 Steak Pricing Game: Dominant Strategy

6.7.2 Steak Pricing Game: Nash Equilibrium

6.7.3 Steak Pricing Game: Maximin Equilibrium (Safety First)

6.7.4 Steak Pricing Game: Cooperative Equilibrium (Collusion)

Chapter 6. Game Theory Two

6.8 Repeated Games

6.9 Sequential Games

6.9.1 Product Choice Game One

6.9.2 Product Choice Game Two

6.10 First Mover Advantage

6.10.1 First Mover Advantage Example: Ethanol

6.10.2 Empty Threat

6.10.3 Pre-Emptive Strike

6.11 Commitment and Credibility

Chapter 1. Introduction to Economics

1.1 Introduction to the Study of Economics

1.1.1 *Economics is Important and Interesting!*

The Economics of agriculture is important and interesting! Food and agricultural markets are in the news and on social media every day. Numerous fascinating and complex issues are the subject of this course: food prices, food safety, diet and nutrition, agricultural policy, globalization, obesity, use of antibiotics and hormones in meat production, hog confinement, and many more. As we work through the course material this semester, please find examples of the economics of food and agriculture in the news. You can earn extra credit by writing a report on a topic that is related to our course material!

1.1.2 *Scarcity*

Economics can be defined as, “the study of choice.” The concept of **scarcity** is the foundation of economics. Scarcity reflects the human condition: fixed resources and unlimited wants, needs, and desires.

Scarcity = Unlimited wants and needs and fixed resources.

Since we have unlimited desires, and only a fixed amount of resources available to meet those desires, we can't have everything that we want. Thus, scarcity forces us to choose: we can't have everything. Since scarcity forces us to choose, and economics is the study of choice, scarcity is the fundamental concept of all economics. If there were no scarcity, there would be no need to choose between alternatives, and no economics!

1.1.3 *Microeconomics and Macroeconomics*

The subject of economics is divided into two major categories: microeconomics and macroeconomics.

Microeconomics = The study of individual decision-making units, such as firms and households.

Macroeconomics = The study of economy-wide aggregates, such as inflation, unemployment, economic growth, and international trade.

This course studies microeconomics, the investigation of firm and household decision making. Our basic assumption is that firms desire to maximize profits, and households seek to maximize utility, or satisfaction.

1.1.4 Economic Models and Theories

The real world is enormously complex. Think of how complicated your daily life is: just waking up and getting ready for class has a huge number of possible complications! Since our world is complicated, we must simplify the real world to understand it. A **Model** is a simplified representation of the world, not intended to be realistic.

Model = A theoretical construct, or representation of a system using symbols, such as a flow chart, schematic, or equation.

We frequently use models in sciences such as chemistry and physics. Think of the model of an atom, with the atomic particles: neutron, proton, and electrons. No one has ever seen an atom, but there is significant evidence for this model. It is easy to be critical of economic models, since we are more familiar with economic events. When we simplify supply and demand into a model, we can think of many oversimplifications and limitations of the theory... the real world is complicated. However, this is how all science works: we must simplify the complex real world in order to understand it.

1.1.4.1 The Scientific Method

Our economic models are built and used following the **Scientific Method**.

Scientific Method = A body of techniques for investigating phenomena, acquiring new knowledge, or correcting and integrating previous knowledge.

The major characteristic of the scientific method is to use measurable evidence to support or detract from a given model or theory. Following this method, economists will keep a theory as long as evidence backs it up. If the evidence does not support the model, the theory will be modified or replaced. Science, or knowledge, advances in this imperfect manner. To repeat, "We have to simplify the real world in order to understand it."

1.1.5 *Positive Economics and Normative Economics*

As social scientists, economists seek to be unbiased and objective in their study of the world. Economists have developed two terms to separate factual statements from value judgments, or opinions.

Positive Economics = Statements that include only factual information, with no value judgments.

Normative Economics = Statements that include value judgments, or opinions. "What ought to be."

In our study of food and agriculture, we will strive to purge our analysis and understanding from opinions and value judgments. Our background and experience can make this challenging. For example, a corn producer might say, "The price of corn is higher, which is a good thing." But, the buyer of the corn, a feedlot operator, might see things differently. All price changes have winners and losers, so economists try to avoid describing price movements in terms of "good" or "bad."

1.2 Supply and Demand

The study of markets is a powerful, informative, and useful method for understanding the world around us, and interpreting economic events. The use of supply and demand allows us to understand how the world works, how changes in economic conditions affect prices and production, and how government policies and programs affect prices, producers, and consumers. A huge number of diverse and interesting issues can be usefully analyzed using supply and demand.

1.2.1 Supply

The **Supply** of a good represents the behavior of firms, or producers. Supply refers to how much of a good will be produced at a given price.

Supply = The relationship between the price of a good and quantity supplied, *ceteris paribus*.

Notice the important term, “*ceteris paribus*” at the end of the definition of supply. Recall the complexity of the real world, and how economists must simplify the world to understand it. Use of the concept, *ceteris paribus*, allows us to understand the supply of a good. In the real world, there are numerous forces affecting the supply of a good: weather, prices, input prices, just to name a few.

Ceteris Paribus = Holding all else constant (Latin).

When studying supply, we seek to isolate the relationship between the price and quantity supplied of a good. We must hold everything else constant (*ceteris paribus*) to make sure that the other supply determinants are not causing changes in supply. An example is the supply of organic cotton. Patagonia spearheaded the movement into using only organic cotton in clothing. Nike and other clothing manufacturers are increasing organic clothing production to meet the growing demand for this good. Interestingly, conventional (non-organic) cotton is the most chemical-intensive field crop, and can result in agricultural chemical runoff in the soil and groundwater. A small but convicted group of consumers are willing to pay high premiums for clothing made with organic cotton, to reduce the potential environmental damage from agricultural chemicals used in cotton production. Notice that this graph has two items on each axis:

(1) a label, and (2) units. Every graph drawn must have both labels and units on each axis to effectively communicate what the graph is about.

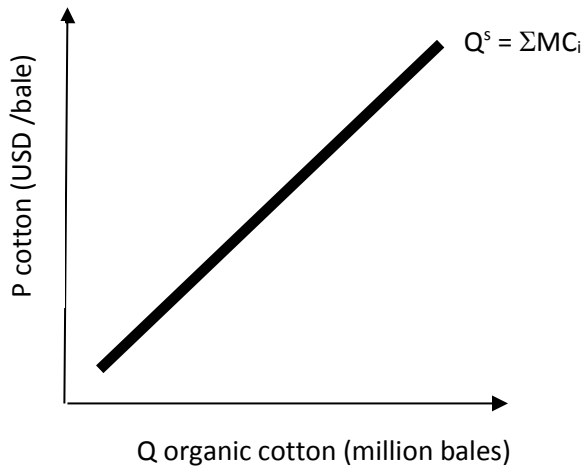


Figure 1.1 Market Supply Curve of Organic Cotton

The supply curve seen in Figure 1.1 is a market supply curve, as it represents the entire market of organic cotton. The market supply curve was derived by horizontal summation all of the individual firm supply curves. The individual firm supply curve is the firm's marginal cost curve (MC) for all prices above the shut down point, and equal to zero for all prices below the shut down point. The shut down point is the minimum point on the firm's average variable cost curve (AVC), as shown in Figure 1.2

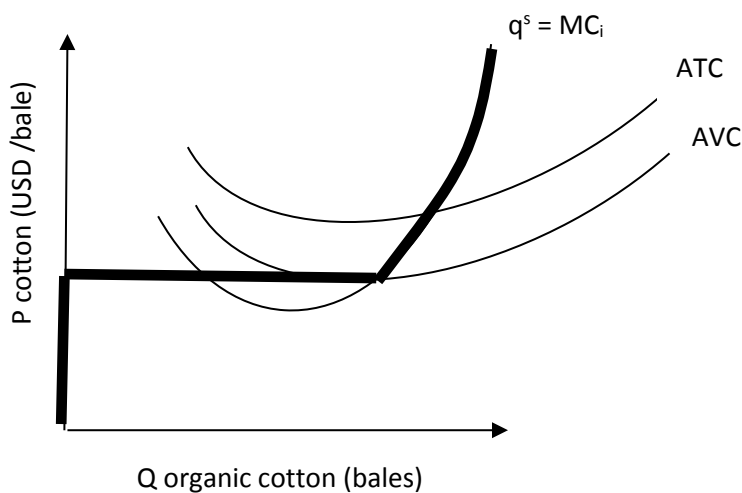


Figure 1.2 Individual Firm Supply Curve of Organic Cotton

Since the market supply curve is the sum of all of the individual firms' marginal cost curves, the market supply curve represents the cost of production: the total amount that a business firm must pay to produce a given quantity of a good.

There are three properties of a market supply curve.

1.2.1.1 *Properties of Supply*

1. upward-sloping: if price increases, quantity supplied increases,
2. $Q^s = f(P)$, and
3. *Ceteris Paribus*, Latin for "holding all else constant."

The first property reflects the Law of Supply, which states that there is a direct relationship between price and quantity supplied.

Law of Supply = There is a direct, positive relationship between the price of a good and the quantity supplied, *ceteris paribus*.

The second property demonstrates that price (P) is the independent variable, and quantity supplied (Q^s) is the dependent variable. Graphs of supply and demand are drawn "backward" with the independent variable (P) on the vertical axis. This is due to economist Alfred Marshall, who drew the original supply and demand graphs this way in his *Principles of Economics* book in 1890. The third property reflects the need to simplify all of the determinants of supply to isolate the relationship between price and quantity supplied, using the *ceteris paribus* assumption.

1.2.1.2 *The Determinants of Supply*

There are numerous determinants of supply, so we will focus on five important ones. The most important supply determinant, or driver, is price (P). Other determinants include input prices (P_i), the prices of related goods (P_r), technology (T), and government taxes and subsidies (G).

$$(1.1) \quad Q^s = f(P, P_i, P_r, T, G)$$

To draw a supply curve, we focus on the most important determinant of supply: the good's own price. We hold all of the other determinants constant. To show this in

equation form, we use a vertical bar to designate *ceteris paribus*: all variables that appear to the right of the vertical bar are held constant. Equation 1.2 shows the relationship between quantity supplied and price, holding all else constant. This relationship is the market supply curve in Figure 1.1 and in supply and demand graphs.

$$(1.2) \quad Q^s = f(P \mid P_i, P_r, T, G)$$

Input prices (P_i) are important determinants of supply, since the supply curve represents the cost of production. Prices of related goods (P_r) represent prices of substitutes and complements in production. Substitutes in production are goods that are produced either/or, such as corn and soybeans. One land parcel can be used to grow either corn or soybeans. Complements in production are goods that are produced together in a fixed ratio. Beef and leather are complements in production. Technology (T) is major driver of supply, as new methods and techniques are available, they increase the amount of food produced. Technological change allows more output to be produced with the same level of inputs. Government policies and programs (G) can shift the supply of a good through taxes or subsidies.

1.2.1.3 Movements Along vs. Shifts In Supply

The supply curve represents the mathematical relationship between the price and quantity supplied of a good. Therefore, when a good's own price changes, it is as a **movement along** the supply curve. When any of the other supply curve determinants change, it will shift the entire curve.

A movement along a supply curve, caused by a change in the good's own price, is called a change in quantity supplied (left panel, figure 1.3). A shift in the supply curve, caused by a change in any supply determinant other than the good's own price, is called a change in supply (right panel, figure 1.3). The change in supply shown in Figure 1.3 is an increase in supply, since it increases the quantity supplied at any given price.

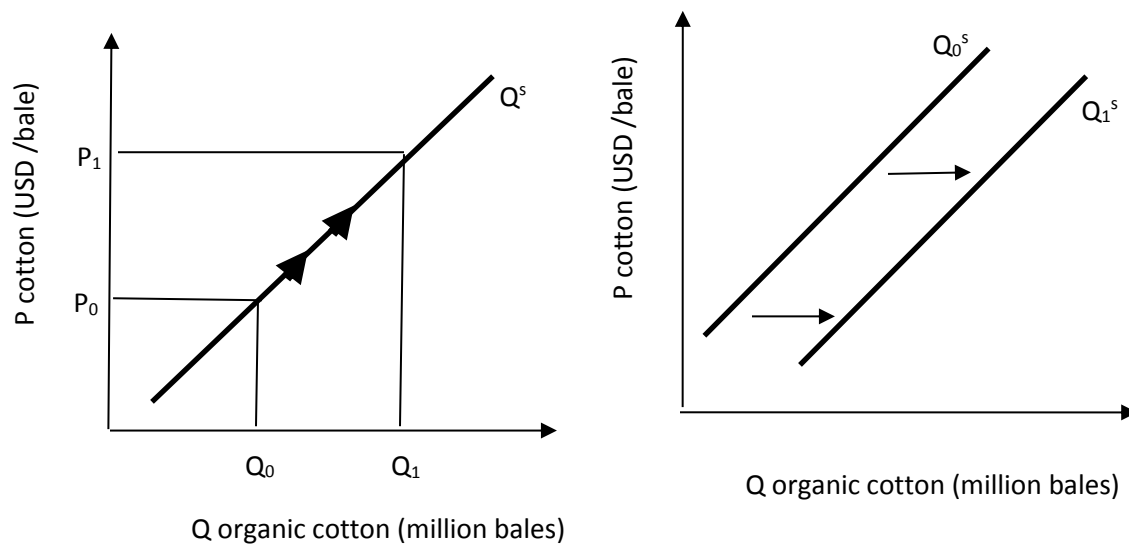


Figure 1.3 Movement Along and Shift in the Supply of Organic Cotton

Notice that the supply curve has shifted down, yet this represents an increase in supply. The supply change is measured on the horizontal axis, so a movement from left to right represents an increase in supply. The shift shown could be the impact of technological change on organic cotton supply: suppose that biotechnology allows for higher yielding varieties of organic cotton.

1.2.2 Demand

The **Demand** of a good represents the behavior of households, or consumers. Demand refers to how much of a good will be purchased at a given price.

Demand = The relationship between the price of a good and quantity demanded, *ceteris paribus*.

Figure 1.4 shows the market demand curve for beef (Q^d), derived by the summation of all individual consumers demand curves (q_i).

Demand represents the willingness and ability of consumers to purchase a good. As with supply, there are three properties of demand

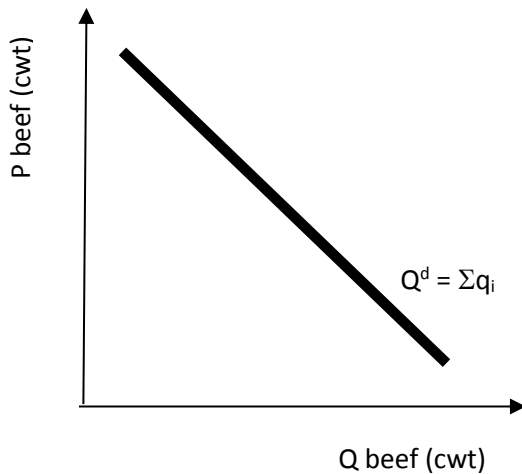


Figure 1.4 Market Demand for Beef

1.2.2.1 Properties of Demand

1. Downward-sloping: if price increases, quantity demanded decreases,
2. $Q^d = f(P)$, and
3. *Ceteris Paribus*, Latin for holding all else constant.

The first property reflects the Law of Demand, which states that if the price of a good increases, the quantity demanded of that good decreases, holding all else constant.

Law of Demand = There is an inverse relationship between the price of a good and the quantity supplied, *ceteris paribus*.

The Law of Demand is one of the major “take home messages” of economic principles. Price increases lead to smaller quantities of goods purchased. The Law of Demand does not say that all consumers will stop buying a good, it says that at least some consumers will decrease consumption of the good. The magnitude of the decrease will depend on the price elasticity of demand for the good, as we will see shortly!

1.2.2.2 The Determinants of Demand

There are numerous demand shifters, or determinants of demand. Six of the most important determinants are included in the demand equation in Equation 1.3. The good's own price (P) is the most important determinant. Demand is also influenced by: the price of related goods (P_r), future prices (P_f), income (I), tastes and preferences (T), and government programs and policies (G).

$$(1.3) \quad Q^d = f(P, P_r, P_f, I, T, G)$$

Related goods include substitutes and complements in consumption. Substitutes in consumption are goods that are purchased either/or, such as hot dogs and hamburgers. If the price of hot dogs increases, at least some consumers will shift out of hot dogs and into hamburgers. Complements in consumption are goods that are consumed together, for example hot dogs and hot dog buns. If the price of hot dogs increases, consumers will purchase fewer hot dogs and fewer buns.

Expectations of future prices (P_f) have a large influence on consumption decisions today. If the price of corn was expected to increase in the future, corn demand would increase today, as corn buyers would seek to buy prior to the price increase. Income (I) can have a large impact on purchase decisions. Cars, houses, and other expensive items will be affected by changes in income. Tastes and preferences (T) shift the demand for goods and services, based on the diverse wants, needs, and desires of consumers in the market. Taxes and subsidies, as well as other government programs, policies, and regulations (G) influence demand, sometimes significantly.

To draw a demand curve, the most important determinant of demand is isolated: the good's own price. We hold all of the other determinants constant, *ceteris paribus*.

$$(1.4) \quad Q^d = f(P \mid P_r, P_f, I, T, G)$$

1.2.2.3 Movements Along vs. Shifts In Demand

The demand curve represents the mathematical relationship between the price and quantity demanded of a good. Therefore, when a good's own price changes, it is depicted as a movement along the demand curve. When any of the other demand curve determinants change, it will shift the entire curve.

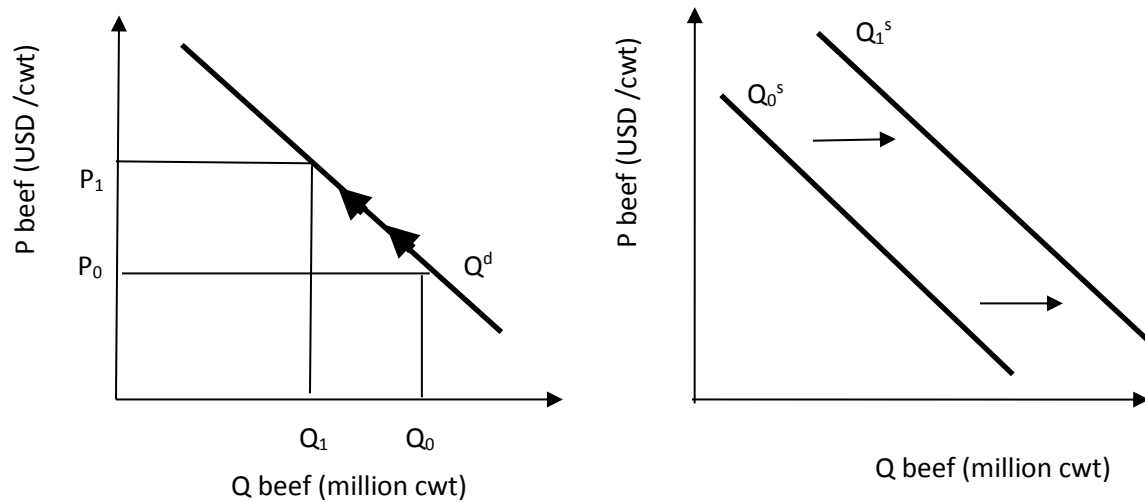


Figure 1.5 Movement Along and Shift in the Demand for Beef

As with supply, if the good's own price changes, it results in a movement along the demand curve, called a change in quantity demanded. If any other demand determinant changes, it causes a shift in demand, called a change in demand. The shift shown in the right panel of Figure 1.5 is an increase in demand, since the demand curve has shifted upward and to the right.

Supply and demand form the foundation for the study of markets, the interaction of supply and demand. Market analysis is the core concept of all of economics, and will be explored in the next section.

1.3 Markets: Supply and Demand

In the previous section, supply and demand were introduced and explored separately. In what follows, the interaction of supply and demand will be presented. The market mechanism is a useful and powerful analytical tool. The market model can be used to explain and forecast movements in prices and quantities of goods and services. The market impacts of current events, government programs and policies, and technological changes can all be evaluated and understood using supply and demand analysis. Markets are the foundation of all economics!

A market equilibrium can be found at the intersection of supply and demand curves, as illustrated for the wheat market in Figure 1.6. An equilibrium is defined as, “a point from which there is no tendency to change.”

Equilibrium = a point from which there is no tendency to change.

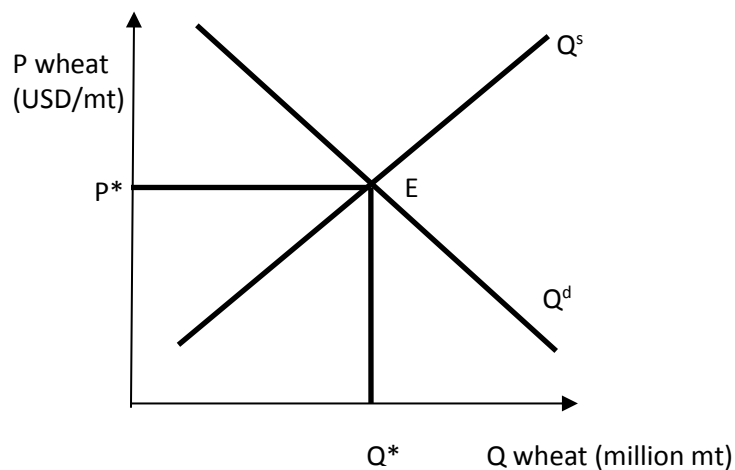


Figure 1.6 Wheat Market

Point E is the only equilibrium in the wheat market shown in Figure 1.6. At any other price, market forces would come into play, and bring the price back to the equilibrium market price, P^* . At any price higher than P^* , such as P' in Figure 1.7, producers would increase the quantity supplied to Q_1 million metric tons of wheat, and consumers would decrease the quantity demanded to Q_0 million metric tons of wheat. A surplus would result, since quantity supplied is greater than quantity demanded.

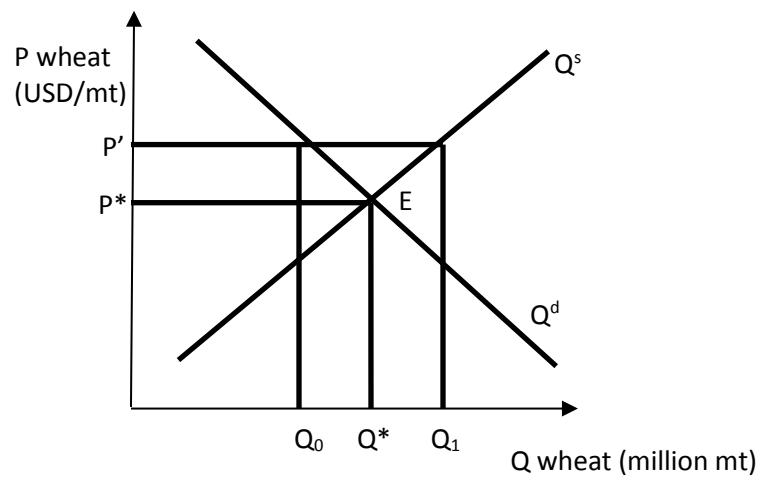


Figure 1.7 Wheat Market Surplus

The wheat surplus would bring market forces into play. Wheat producers would lower the price of wheat in order to sell it. It would be preferable to earn a lower price than it would do let the surplus go unsold. Consumers would increase the quantity demanded along Q^d until the equilibrium point E was reached. In this way, any price higher than the market equilibrium price will be temporary, as the resulting surplus will bring the price back down to P^* .

Market forces also come into play at prices lower than the equilibrium market price, as shown in Figure 1.8. At the lower price P'' , producers reduce the quantity supplied along Q^s to Q_0 , and consumers increase the quantity demanded to Q_1 . A shortage occurs, since the quantity demanded is greater than the quantity supplied. The shortage will bring market forces into play, as consumers will bid up the price in order to purchase more wheat. This process will continue until the market price returns to the equilibrium market price, P^* .

The market mechanism that results in an equilibrium price and quantity performs a truly amazing function in the economy. Markets are self-regulating, since no intervention or coercion is needed to achieve desirable outcomes. If there is a drought, the price of wheat will rise, causing more resources to be devoted to wheat production, which is desirable, since wheat is in short supply during a drought. If good weather causes a surplus, the price will fall, causing wheat producers to shift resources out of wheat and into more profitable opportunities. In this fashion, the market mechanism

allows voluntary trades between willing parties to allocate resources to the highest return. Efficiency of resource use and high incomes are a feature of market-based economies.

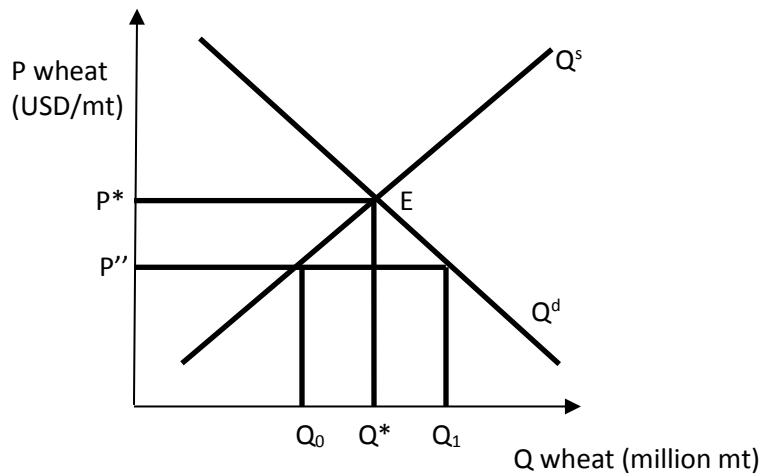


Figure 1.8 Wheat Market Shortage

The market graphs of supply and demand are based on the assumption of perfectly competitive markets. Perfect competition is an ideal state, different from actual market conditions in the real world. Once again, economists simplify the complex real world in order to understand it. We will begin with the extreme of perfect competition, and later introduce realism into our analysis.

1.3.1 Competitive Market Properties

1. homogeneous product,
2. numerous buyers and sellers,
3. freedom of entry and exit, and
4. perfect information.

The first property of perfect competition is a homogeneous product. This means that the consumer can not distinguish any differences in the good, no matter which firm produced it. Wheat is an example, as it is not possible to determine which farmer produced the wheat. A John Deere tractor is an example of a nonhomogeneous good, since the brand is displayed on the machine, not to mention the company's well known green paint.

The assumption of numerous buyers and sellers means something specific. The word, “numerous” refers to an industry so large that each individual firm can not affect the price. Each firm is so small relative to the industry that it is a price taker.

Freedom of entry and exit means that there are no legal, financial, or regulatory barriers to entering the market. A wheat market allows anyone to produce and sell wheat. Attorneys and physicians, however, do not have freedom of entry. To practice law or medicine, a license is required.

Perfect information is an assumption about industries where all firms have access to information about all input and output prices and all technologies. There are no trade secrets or patented technologies in a perfectly competitive industry. These four properties of perfect competition are stringent, and do not reflect real-world industries and markets. Our study of market structures in this course will examine each of these properties, and use them to define industries where these properties do not hold. Competitive markets have a number of attractive properties.

1.3.2 Outcomes of Competitive Markets

Competitive markets result in desirable outcomes for economies. A competitive market maximizes social welfare, or the total amount of well-being in a market. Competitive markets use voluntary exchange, or mutually beneficial trades, to achieve this result. In a market-based economy, no one is forced, or coerced, to do anything that they do not want to do. In this way, all trades are mutually beneficial: a producer or consumer would never make a trade unless it made him or her better off. This idea will be a theme throughout this course: free markets and free trade lead to superior economic outcomes.

It should be emphasized that free markets and free trade are not perfect, since there are negative features associated with markets and capitalism. Income inequality is an example. Markets do not solve all of society’s problems, but they do create conditions for higher levels of income and wealth than other economic organizations, such as a command economy. There are winners and losers to market changes. An example is free trade. Free trade lowers prices for consumers, but often causes hardships for producers in importing nations. Similarly, open borders allow immigrants to improve their conditions and earnings by moving from low-income nations to high-income nations such as the United States (US) or the European Union (EU). Workers in the US and the EU will face competition from a larger labor supply, causing reductions in wages and salaries. A simple example of markets is an increase in the price of corn. Corn producers are made better off, but livestock producers, the major buyers of corn,

are made worse off. Thus, the market shifts that allow prosperity also create winners and losers in a free market economy.

1.3.3 Supply and Demand Shift Examples

Given our knowledge of markets and the market mechanism, current events and policies can be better understood.

1.3.3.1 Demand Increase

China was a command economy until 1986. At that time, the government introduced the Household Responsibility System, which allowed farmers to earn income based on how much agricultural output they produced. The new policy worked very well, and China moved from being a net food importer to a net food exporter. Soon, the policy was extended to all industries, and China was on its way to a market-based economy. The result has been a truly unprecedented increase in income. China has gone from a low income nation to a middle income nation, and the rates of economic growth are higher than any nation in history. And, these growth rates are for the world's most populous nation: 1.4 billion people (for comparison, the US has about 320 million people).

This historical income growth has been good for US farmers and ranchers. As incomes increase, consumers shift out of grain-based diets such as rice and wheat, and into meat. There has been a large increase in beef consumption in China as incomes increased. This is an increase in the demand for US beef, as shown in Figure 1.9. The units for beef are hundredweight (cwt), or one hundred pounds. This is called an increase in demand (do you remember why this is not an increase in quantity demanded?). The outward shift in demand results in a movement from equilibrium E_0 to E_1 . The movement along the supply curve for beef is called an increase in quantity supplied. The equilibrium market price increases from P_0 to P_1 , and the equilibrium market quantity increases from Q_0 to Q_1 .

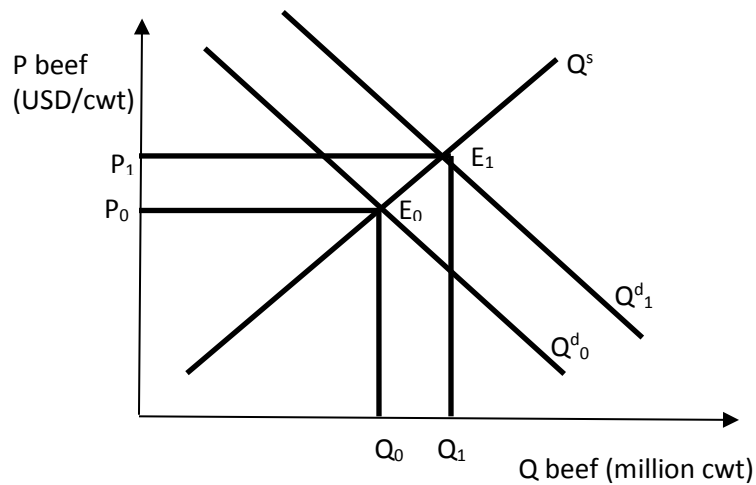


Figure 1.9 Increase in China Income Impact on US Beef Market

Interestingly, income growth in China is beneficial to not only US beef producers, who face an increased demand for beef, but also for grain farmers. The major input into the production of beef is corn, sorghum (also called milo) and soybeans. These grains are fed to cattle in feedlots, and it takes seven pounds of grain to produce one pound of beef. Therefore, any increase in the global demand for beef will result in an increase in demand for beef and a large increase in the demand for feed grains.

1.3.3.2 Demand Decrease

The demand for beef offals (tripe, tongue, etc.) has decreased in the past few decades. As incomes increase, consumers shift out of these goods and into more expensive meat products such as hamburger and steaks. The demand for offals has decreased as a result, as in Figure 1.10. This is a decrease in demand (shift inward), and a decrease in quantity supplied (movement along the supply curve). The outcome is a decrease in the equilibrium market price and quantity of beef offals.

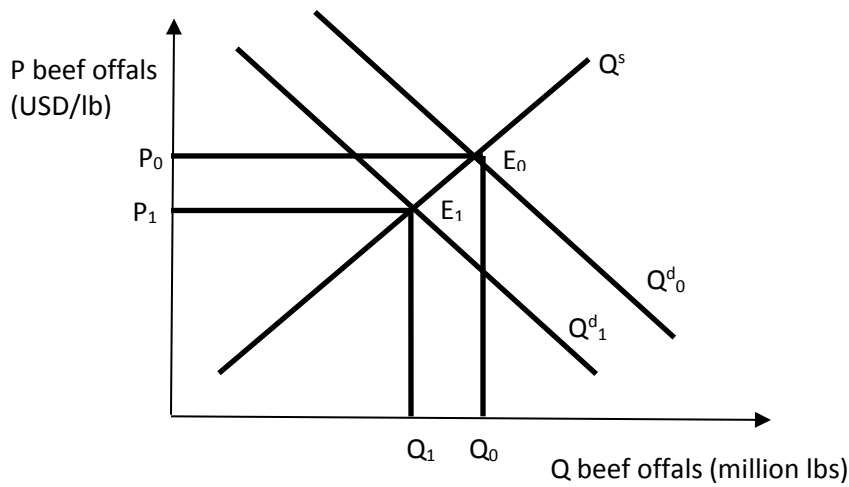


Figure 1.10 Increase in US Income Impact on US Beef Offal Market

1.3.3.3 Supply Decrease

A large share of citrus fruit in the US is grown in Florida and California. If there is bad weather in either State, the market for oranges, lemons, limes, and grapefruit is affected. An early freeze can damage the citrus fruit, resulting in a decrease in supply (Figure 1.11).

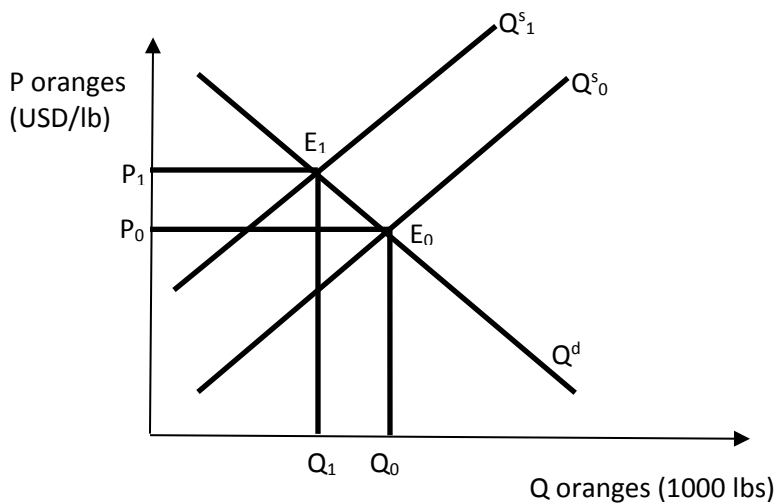


Figure 1.11 Frost Damage Impact on US Orange Market

The supply decrease is a shift in the supply curve to the left, resulting in a movement along the demand curve: a decrease in quantity demanded. The equilibrium price increases, and the equilibrium quantity decreases.

1.3.3.4 Supply Increase

Technological change is a constant in global agriculture. Science and technology has provided more output from the same levels of inputs for many decades, and especially since 1950. Biotechnology in field crops has been a recent enhancement in the world food supply. Biotechnology is also referred to as genetically modified organisms (GMOs). Although GMOs are often in the news media as a potential health risk or environmental risk, they have been produced and consumed in the US for many years, with no documented health issues. However, the herbicide glyphosate has been determined to be a carcinogen in recent studies. Glyphosate is the ingredient in “RoundUp,” a widely used herbicide in corn and soybean production. Genetically modified corn and soybeans are resistant to this herbicide, so it has been used extensively since the introduction of GM crops. Biotechnology has increased the availability of food enormously, and is considered the largest technological change in the history of agriculture. The impact of biotechnology is shown in Figure 1.12.

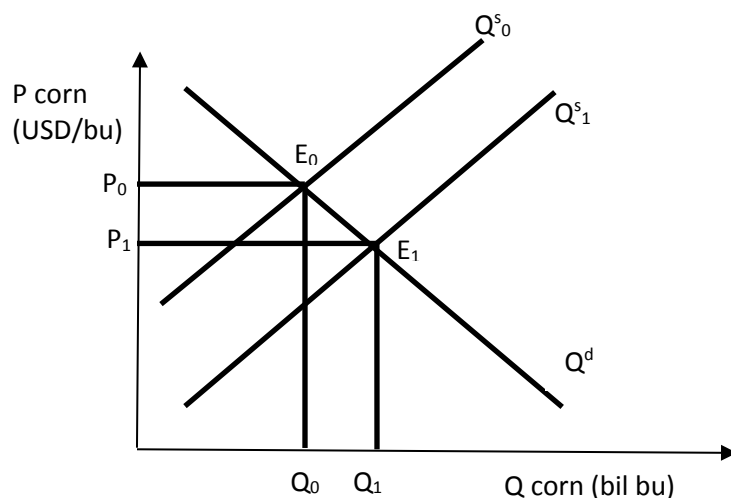


Figure 1.12 Biotechnology Impact on Corn Market

Biotechnology results in an increase in supply, the rightward shift in the supply curve. This supply shift results in a movement along the demand curve, an increase in quantity demanded. The equilibrium quantity increases, and the equilibrium price decreases. It may seem that the decrease in price is bad for corn producers. However, in a global economy, this keeps the US competitive in global grain markets. Since a large fraction of US grain crops are exported, this provides additional income to the corn industry.

1.3.4 Mathematics of Supply and Demand

The above market analyses are qualitative, or non-numerical. Numbers can be added to the supply and demand graphs to provide quantitative results. The numbers used here are simple, but can be replaced with actual estimates of supply and demand to yield important and interesting quantitative results to market events.

As an example, consider the phone market. Let the inverse demand for phones be given by Equation 1.5. The equation is called, “inverse” because the independent variable (P) appears on the left-hand side and the dependent variable (Q^d) appears on the right hand side. Traditionally, the independent variable (x) is on the right, and the dependent variable (y) is on the left. We use inverse supply and demand equations for easier graphing, since P is on the vertical axis, typically used for the dependent variable (can you remember why these graphs are backwards?).

$$(1.5) \quad P = 100 - 2Q^d$$

In the inverse demand equation, P is the price of phones in USD/unit, and Q is the quantity of phones in millions. The inverse supply equation is given in Equation 1.6.

$$(1.6) \quad P = 20 + 2Q^s$$

These examples of inverse supply and demand functions are called “price-dependent” for ease of graphing. The equations can be quickly and easily inverted to “quantity-dependent” form.

To find equilibrium, set $Q^s = Q^d = Q^e$. This is the point where the market “clears,” and supply is equal to demand. By inspection of the market graph (Figure 1.13), there is only one price where this can occur.

$$P = 100 - 2Q^e = 20 + 2Q^e$$

$$80 = 4Q^e$$

$$Q^e = 20$$

$$P^e = 100 - 2Q^e = 100 - 2 \cdot 20 = 100 - 40 = 60$$

This result can be checked by plugging $Q^e = 20$ into the inverse supply equation:

$$P^e = 20 + 2Q^e = 20 + 2 \cdot 20 = 20 + 40 = 60$$

The equilibrium price and quantity of phones are:

$$P^e = \text{USD } 60/\text{phones}$$

$$Q^e = 20 \text{ million phones.}$$

Notice that these equilibrium values have both labels (phones) and units.

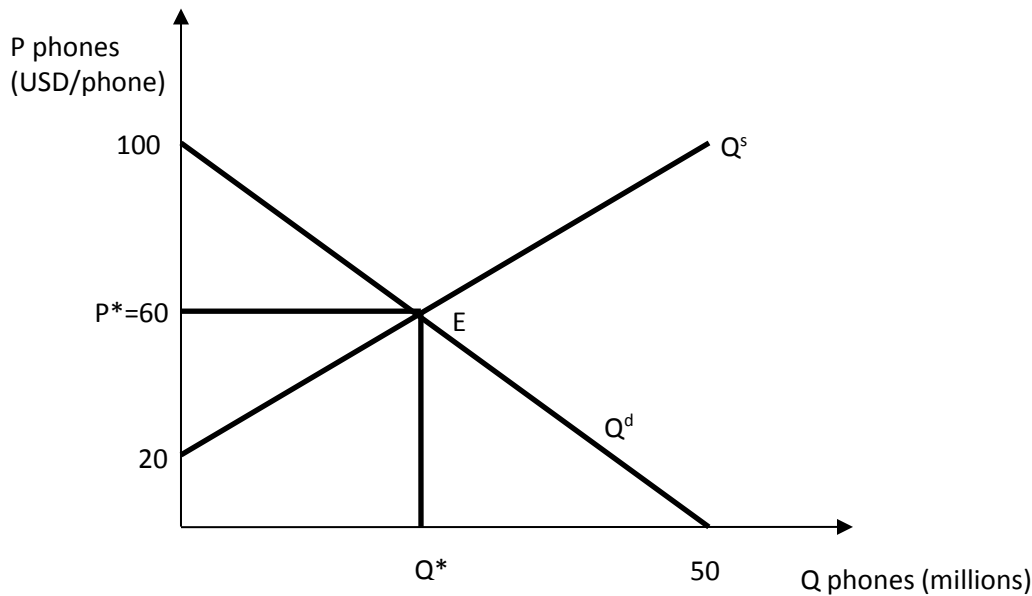


Figure 1.13 Phone Market Equilibrium

We will be using quantitative market analysis throughout the rest of the course. If you have any questions about how to graph the functions, or how to solve for equilibrium price and quantity, be sure to ask for help now. We will be using these graphs throughout our study of market structures!

1.4 Elasticities

1.4.1 Introduction to Elasticities

An **elasticity** is a measure of responsiveness.

Elasticity = How responsive one variable is to a change in another variable.

The elasticity (E), or responsiveness, is measured by the percentage change of each variable. The change in a variable is the ending value (X_1) minus the initial value (X_0), or $\Delta X = X_1 - X_0$. A percentage change is the change in the variable divided by the initial value of the variable: $\% \Delta X = \Delta X / X_0$. Using this formula, Equation 1.7 shows the responsiveness of Y to a change in X:

$$(1.7) \quad E = \% \Delta Y / \% \Delta X = (\Delta Y / \Delta X)(X / Y).$$

Elasticities can be calculated for any two variables. Elasticities are widely used in economics to measure how responsive producers and consumers are to changes in prices, income, and other economic variables. Elasticities have a very desirable property: they do not have units. Since the two variables are measured in percentage changes, the units of each variable are cancelled, and the resulting elasticity has no units. This allows elasticities to be compared to each other, when prices and quantities cannot be directly compared. For example, the quantity of apples cannot be directly compared to the quantity of orange juice, since they are in different units.

1.4.2 Own Price Elasticity of Demand: E_d

The own-price elasticity of demand (most often called simply the “price elasticity of demand” or the “elasticity of demand”) measures the responsiveness of consumers to a change in price, as shown in Equation 1.8:

$$(1.8) \quad E_d = \% \Delta Q^d / \% \Delta P = (\Delta Q^d / \Delta P)(P / Q^d).$$

Own Price Elasticity of Demand = the percentage change in quantity demanded given a one percent change in the good’s own price, *ceteris paribus*.

The own-price elasticity of demand is the most important thing that a business firm can know. The price elasticity informs the business about how a change in price will affect the quantity demanded. If consumers are responsive to price changes, the firm may think twice before raising the price and losing customers to the competition. On the other hand, if consumers are relatively unresponsive to price changes, the firm may increase the price, and the customers will purchase the good at the higher price. Food is an example of an inelastic good, since we all need to eat.

The price elasticity of demand (E_d) depends on the availability of substitutes. If there are no substitutes for a good (food, toilet paper, toothpaste), the good is called, “price inelastic.” Consumers will purchase the good even at a high price. If substitutes are available, the good is considered to be “price elastic”: a higher price will cause customers to buy the substitute good. Green shirts are an example: if the price of green shirts is increased, consumers will shift purchases to blue shirts, or shirts of a different color.

The price elasticity of demand is the most critical aspect of a business firm, since it provides the most crucial information about customers!

1.4.2.1 Price Elasticity of Demand Example

Suppose that the price of wheat is equal to USD 4/bu, and increases to USD 6/bu. Due to the higher price, assume that wheat millers reduce their purchases of wheat from 10 million bushels (m bu) to 8 million bushels. The price elasticity of demand can be calculated for wheat using Equation 1.9. By convention, the initial values of P and Q^d are used in the elasticity calculation.

$$(1.9) E_d = \% \Delta Q^d / \% \Delta P = (\Delta Q^d / \Delta P) (P / Q^d) = (8 - 10 \text{ m bu}) / (6 - 4 \text{ USD/mt}) * (4 \text{ USD/bu}) / (10 \text{ m bu})$$

Notice that the units cancel: there are (m bu) in both the numerator and denominator, and (USD/bu) also appears in both numerator and denominator. This allows the math to be greatly simplified:

$$E_d = (-2/2) * (4/10) = (-1)/(0.4) = -0.4$$

The price elasticity of demand is always negative, due to the Law of Demand. We take the absolute value to make E_d positive. For example, in this case, $E_d = -0.4$, then $|E_d| = 0.4$. The own price elasticity of demand provides important information about the wheat market: how responsive wheat buyers are to a change in price. To interpret the

elasticity, it means that for a one percent increase in price, the quantity demanded of wheat will decrease by 0.4 percent. This is a relatively inelastic response, since the change in quantity demanded is smaller than the price change.

Elasticities are classified into three categories, based on consumer responsiveness to a one percent change in price.

Price elastic	$ E_d > 1$
Price inelastic	$ E_d < 1$
Unitary elastic	$ E_d = 1$

Goods that are price elastic have substitutes available, and the percentage change in quantity demanded will decrease more than the percentage increase change in price. A price inelastic good, on the other hand, will have a smaller percentage change in quantity demanded than the percentage increase in price. For unitary elastic goods, the percentage change in quantity demanded is equal to the percentage change in price.

1.4.2.2 Elastic and Inelastic Demand Examples

To compare elastic and inelastic demands, think of a student who would like to purchase a pack of cigarettes during a late night study session for an exam. If the student arrives at the convenience store to find that the price of Marlboros, her usual brand, has been doubled, she can switch to many other brands: Lucky Strikes, Winstons, etc. The demand for Marlboro cigarettes is price elastic (left panel, Figure 1.14). The price elasticity of demand depends on the availability of substitutes. An elastic demand will have a small slope, since a small change in price results in a relatively larger change in quantity demanded.

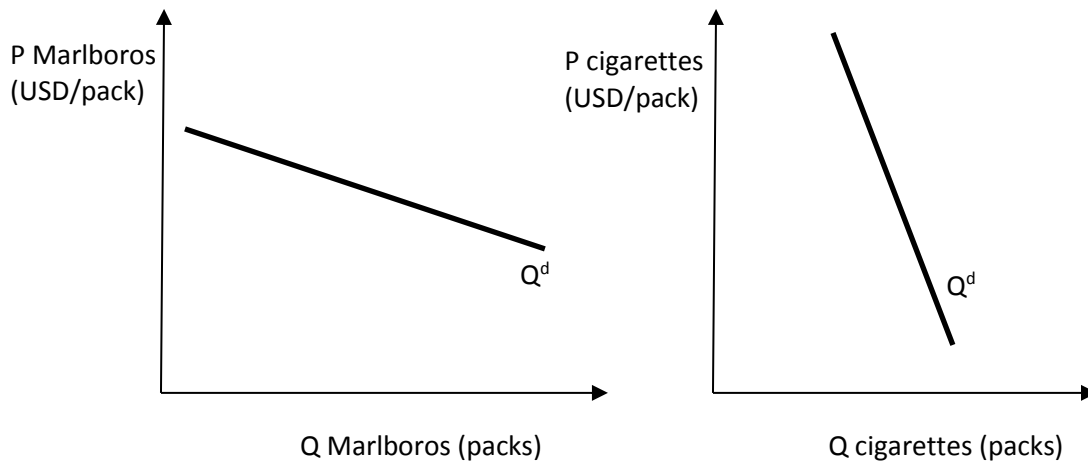


Figure 1.14 Price Elasticity of Demand for Marlboros and Cigarettes

On the other hand, if the convenience store increases the price of all cigarettes, the student will pay for a pack, since there are no substitutes for all cigarettes (right panel, Figure 1.14). More narrowly defined goods will have larger absolute values of own price elasticities, since there are more substitutes for narrowly defined goods. For example, apples are more price elastic than all fruit, and green shirts are more price elastic than all shirts. An inelastic good will have a steep slope, since the change in quantity demanded is small relative to the change in price.

Figure 1.15 shows a range of own price elasticities, from perfectly inelastic to perfectly elastic.

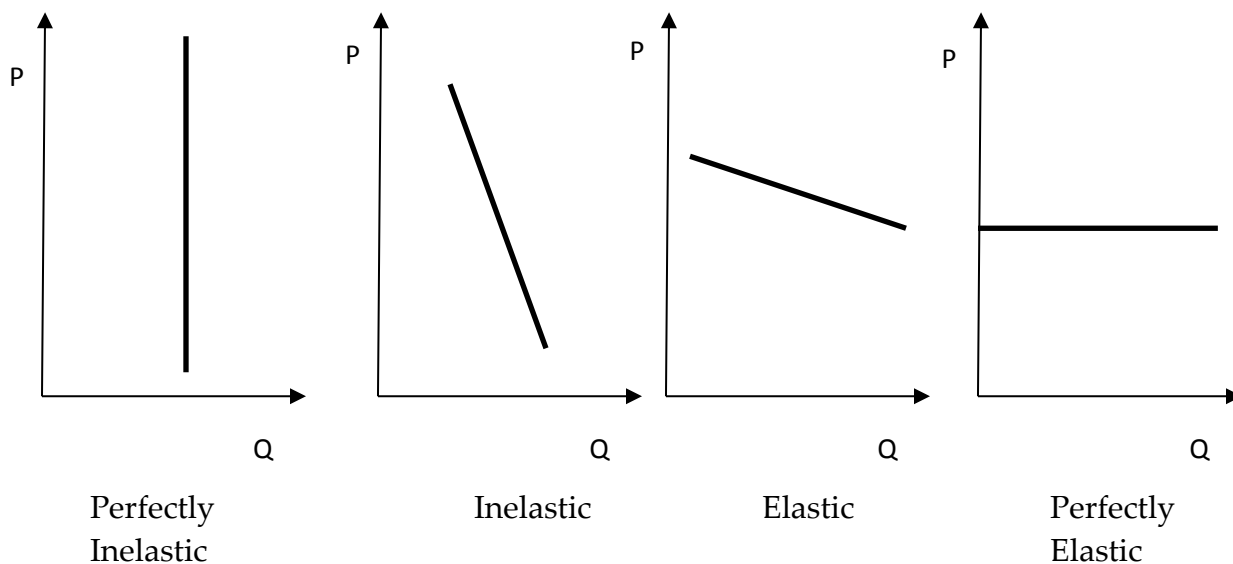


Figure 1.15 Price Elasticity of Demand

A good that is perfectly inelastic is one that consumers purchase no matter what the price is. Within a certain range of prices, this could be food or electricity. In this case, quantity demanded is completely unresponsive to changes in price: $|E_d| = 0$. An inelastic demand is one where the percentage change in price is larger than the percentage change in quantity demanded: $\% \Delta Q^d < \% \Delta P$, and $|E_d| < 1$. Goods that are price inelastic are characterized by consumers being unresponsive to price changes. Goods that are price elastic exhibit relatively high levels of consumer responsiveness to price movements. For elastic goods, the percentage change in quantity demanded is larger than the percentage change in price: $\% \Delta Q^d > \% \Delta P$, and $|E_d| > 1$. A perfectly elastic good is characterized by a horizontal demand curve. In this case, if the price of the good is increased even one cent, all customers will not purchase the good. An individual wheat farmer's crop is an example. If the farmer tries to increase the price by one cent more than the prevailing market price, no consumers would purchase her wheat. There are a large number of perfect substitutes available from other wheat farmers.

1.4.3 Own Price Elasticity of Supply: E_s

Producer responsiveness to a change in price is measured with the own price elasticity of supply, often called the price elasticity of supply, or the elasticity of supply (E_s). The formula for the price elasticity of supply is given in Equation 1.10:

$$(1.10) \quad E_s = \% \Delta Q^s / \% \Delta P.$$

Own Price Elasticity of Supply = the percentage change in quantity supplied given a one percent change in the good's own price, *ceteris paribus*.

The own price elasticity of supply is always positive, because of the Law of Supply: there is a direct, positive relationship between the quantity supplied of a good and the good's own price. Similar to the price elasticity of demand, the price elasticity of supply is categorized into three elasticity classifications.

Price elastic	$E_s > 1$
Price inelastic	$E_s < 1$
Unitary elastic	$E_s = 1$

A good with an elastic supply is one where the percentage change in quantity supplied is greater than the percentage change in price: $\% \Delta Q^s > \% \Delta P$, and $E_s > 1$. Since E_s is always positive, the absolute value is not necessary. A good with an inelastic supply has a smaller percentage change in quantity supplied, given a percent change in price: $\% \Delta Q^s < \% \Delta P$, and $E_s < 1$. A good with unitary elasticity of supply has equal percent changes in quantity supplied and price: $\% \Delta Q^s = \% \Delta P$, and $E_s = 1$. Figure 1.16 illustrates the different categories of the own price elasticity of supply.

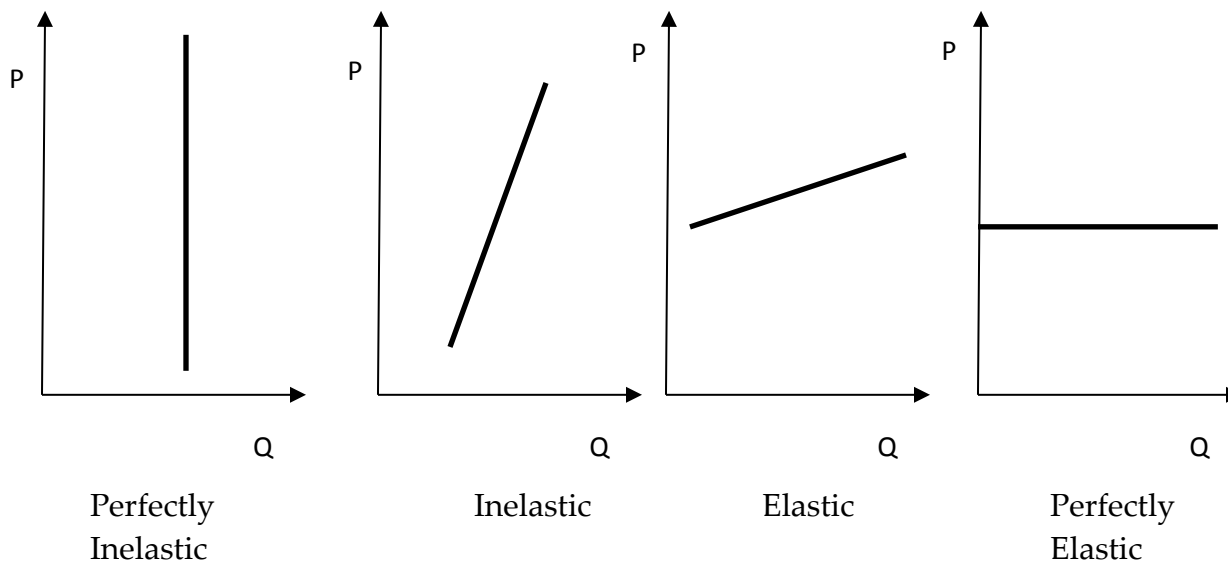


Figure 1.16 Price Elasticity of Supply

1.4.4 Income Elasticity: E_i

The income elasticity (E_i) measures how consumers respond to a one percent increase in income (I), as shown in Equation 1.11:

$$(1.11) \quad E_i = \% \Delta Q^d / \% \Delta I.$$

The income elasticity is defined in a similar way as the price elasticities.

Income Elasticity = the percentage change in demand given a one percent change in income, *ceteris paribus*.

Income elasticities are also categorized into responsiveness classifications. A normal good is one that increases with an increase in income ($E_i > 0$). There are two subcategories of normal goods: necessities and luxury goods. Notice that necessity goods and luxury goods are normal goods. They represent subgroups of the normal category, since E_i is positive in both cases.

Normal Good	$E_i > 0$
Necessity Good	$0 < E_i < 1$
Luxury Good	$E_i > 1$
Inferior Good	$E_i < 0$

The graphs of the relationship between income and demand are called, “Engel Curves,” named for Ernst Engel (1821-1896), a German statistician who first investigated the impact of income on consumption.

A necessity good is a normal good that has a positive, but small, increase in demand given a one percent increase in income. Food is an example, since consumers increase the consumption of food with an increase in income, but the total amount of food consumed reaches an upper limit. This is shown in Figure 1.17, left panel.

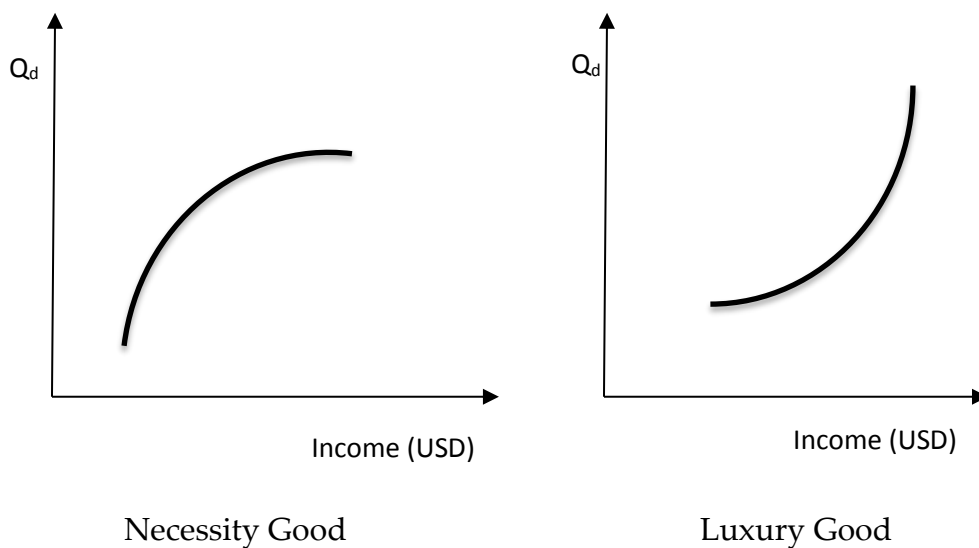


Figure 1.17 Engel Curves for Necessity Goods and Luxury Goods

A luxury good is one that has increasing demand as income increases, as shown in the right panel of Figure 1.17. Good such as boats, golf club memberships, and expensive clothing are examples of luxury goods. Inferior goods (Figure 1.18) are characterized by

lower levels of consumption as income increases: ramen noodles and used clothes are examples.

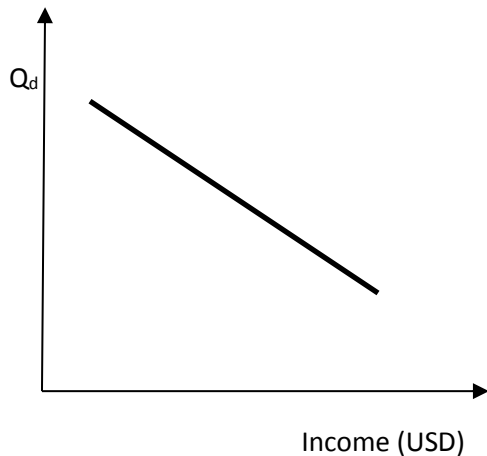


Figure 1.18 Engel Curve for an Inferior Good

It is important to point out that a good can be a normal good at low income levels, and an inferior good at higher income levels. Hamburger (ground beef) is an example. At low levels of income, hamburger consumption might increase when income rises (Figure 1.19). However, at higher levels of income, consumers might shift out of ground beef and into more expensive meats such as steak. Figure 1.19 shows that the same good can be both a normal good and an inferior good, at different levels of income.

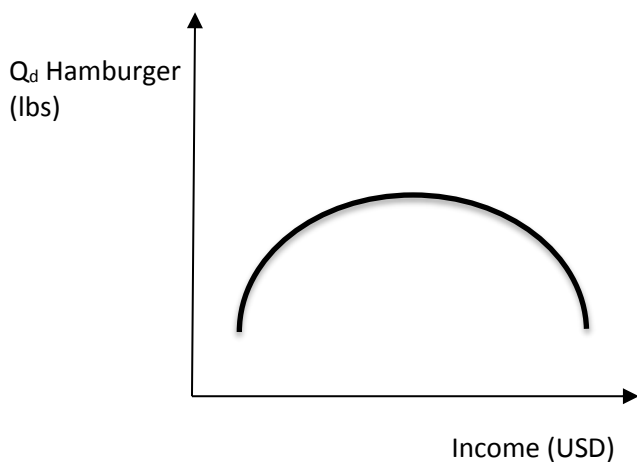


Figure 1.19 Engel Curve for Hamburger: A Necessity Good and An Inferior Good

1.4.5 Cross-Price Elasticity of Demand: E_{dxy}

The cross price elasticity of demand measures the responsiveness of demand for one good with respect to a change in the price of another good.

$$(1.12) \quad E_{dxy} = \% \Delta Q_y^d / \% \Delta P_x$$

Cross Price Elasticity of Demand = the percentage change in the demand of one good given a one percent change in a related good's price, *ceteris paribus*.

The cross price elasticity is important for two categories of related goods: substitutes and complements in consumption. Substitutes in consumption will have a positive cross price elasticity of demand, since consumers will decrease purchases of the good that has the price increase, and buy more substitute goods. Complements in consumption are goods that are consumed together, like macaroni and cheese. If the price of macaroni increases, then consumption of both macaroni and cheese decreases.

Substitutes in Consumption $E_{dxy} = \% \Delta Q_y^d / \% \Delta P_x > 0$

Complements in Consumption $E_{dxy} = \% \Delta Q_y^d / \% \Delta P_x < 0$

Unrelated Goods in Consumption $E_{dxy} = \% \Delta Q_y^d / \% \Delta P_x = 0$

Unrelated goods have a cross price elasticity of demand equal to zero.

1.4.6 Cross-Price Elasticity of Supply: E_{sxy}

The cross price elasticity of supply captures the responsiveness of the supply of one good, given a change in the price of another good.

$$(1.13) \quad E_{sxy} = \% \Delta Q_y^s / \% \Delta P_x$$

Cross Price Elasticity of Supply = the percentage change in the supply of one good given a one percent change in a related good's price, *ceteris paribus*.

Substitutes in production are goods that are produced "either/or," such as corn and soybeans. The same resources could be used to produce either corn or soybeans, but the

two crops can not be grown on the same land at the same time. The cross price elasticity of supply of substitutes in production is negative. If the price of corn increases, for example, then producers will devote more land to corn and less to soybeans.

Substitutes in Production	$E_{s_{xy}} = \% \Delta Q_y^s / \% \Delta P_x < 0$
Complements in Production	$E_{s_{xy}} = \% \Delta Q_y^s / \% \Delta P_x > 0$
Unrelated Goods in Production	$E_{s_{xy}} = \% \Delta Q_y^s / \% \Delta P_x = 0$

Complements in production are goods that are produced together, such as beef and leather. Complements in production have a positive cross price elasticity: if the price of beef increases, both more beef and more leather will be supplied to the market.

Unrelated goods in production have a cross price elasticity of supply equal to zero.

1.4.7 Price Elasticities and Time

The determinant of the price elasticity of supply measures how easy it is for the firm to adjust to price changes. In the immediate run (a short time period), the firm can not adjust the production process, so the supply is typically perfectly inelastic. In the short run, a time period when some inputs are fixed and some inputs are variable, the firm may be able to adjust some inputs, so supply is inelastic, but not perfectly inelastic. In the long run, all inputs are variable, and the firm can make adjustments to the production process. In this case, supply is elastic. As more time passes, the price elasticity of supply increases.

This relationship also holds for the price elasticity of demand. If the price of a good increases in the immediate run, there is little consumers can do other than purchase the good. Air travelers who have an emergency that they need to attend to will pay a high price of an airline ticket on the same day of the flight. As time passes, there are more options available to the consumer, and the price elasticity of demand is more elastic.

1.4.8 Elasticity of Demand along a Linear Demand Curve

Interestingly, the elasticity of demand changes along a linear demand curve. This is due to the calculation of the own price elasticity of demand as percentage change in one variable caused by a percentage change in another variable. In Figure 1.20, the slope of the demand function is constant: it does not change over the entire demand curve.

For example, suppose that the inverse demand function is given by: $P = 10 - Q^d$, where P is the price of the good and Q^d is the quantity demanded. In this case, the vertical intercept (y-intercept) is equal to 10, and the slope is equal to negative one. It should be emphasized that the slope is constant and equal to minus one for the entire demand curve.

The elasticity of demand, however, changes in value quite dramatically from the y-intercept to the x-intercept. It changes from a value of zero along the x-axis to a value of negative infinity on the y-axis. The cause is the calculation of percentage change.

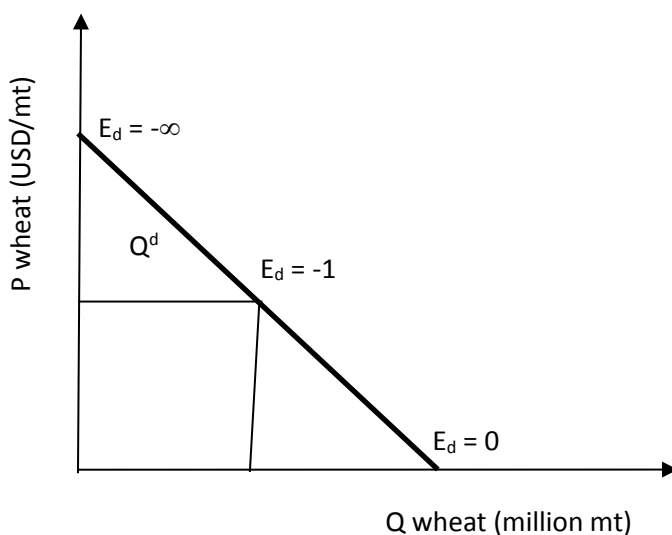


Figure 1.20 The Price Elasticity of Demand along a Linear Demand Curve

Consider an example of a mouse and an elephant. If both gain one pound, the weight gain is identical, but the percentage change is vastly different. Suppose that the mouse weighs one-tenth of a pound, the elephant weighs 10,000 pounds, and the total weight gain for both the mouse and the elephant is one pound. The percentage weight gain is $\% \Delta WG = \Delta WG / WG_0$, where ΔWG is the change in weight, and WG_0 is the initial weight gain. For the mouse,

$$(1.14) \quad \% \Delta WG \text{ mouse} = \Delta WG / WG_0 = 1 \text{ lb} / 0.1 \text{ lbs} = 10 = 1000 \text{ percent!}$$

For the elephant,

$$(1.15) \quad \% \Delta WG \text{ elephant} = \Delta WG / WG_0 = 1 \text{ lb} / 10,000 \text{ lbs} = 0.0001 = 0.01 \text{ percent!}$$

The take home message of the story is that the total weight gain was identical for both the elephant and the mouse (one pound), whereas the percentage weight gain was enormously different.

This is also true of the elasticity of demand along the linear demand curve. Consider the point where the linear demand curve crosses the x-axis. At this point, the price is equal to zero. Suppose that we we raised the price by one unit to find out how responsive consumers are to an increase in price. The price elasticity of demand is:

$$(1.16) \quad E_d = \% \Delta Q^d / \% \Delta P.$$

At the x-intercept, the percentage change in price ($\% \Delta P$) is equal to $\Delta P / P = 1 / 0 = \text{infinity}$. The elasticity of demand is equal to the percentage change in quantity demanded ($\% \Delta Q$) divided by the percentage change in price ($\% \Delta P = \text{infinity}$). Thus, $E_d = 0$, since dividing any number by infinity is equal to zero.

How responsive consumers are to a change in price at the vertical axis? At the y-intercept, the percentage change in quantity demanded ($\% \Delta Q_d$) is equal to $\Delta Q_d / Q_d = 1 / 0 = \text{infinity}$. Therefore, the elasticity of demand is equal to the percentage change in quantity demanded ($\% \Delta Q = \text{infinity}$) divided by the percentage change in price ($\% \Delta P$). Thus, $|E_d| = \text{infinity}$.

At the midpoint, the price elasticity of demand is equal to negative one.

$$(1.17) \quad E_d = \% \Delta Q^d / \% \Delta P = (\Delta Q^d / \Delta P)(P / Q^d) = -1$$

At the midpoint, the slope of the demand curve is equal to minus one, and the price is equal to the quantity demanded. Therefore the own price elasticity of demand at the midpoint of a linear demand curve is equal to minus one.

A valuable lesson is learned in this example: be careful to distinguish between the slope of a demand curve and the elasticity of demand. When interpreting graphs, the slope is not a good determinant of elasticity, since a graph could be drawn steep or shallow depending on the units. The elasticity is related to the slope, but it is not equal to the slope!

1.4.9 Agricultural Policy Example of Elasticity of Demand

The impact of agricultural policies depends enormously on the elasticity of demand. It was claimed earlier that the price elasticity of demand is the most important thing that a business firm can know. This section provides evidence of the importance of the price elasticity of demand. The own price elasticity of demand for food is inelastic in a domestic economy with no trade. Everyone must eat, and the caloric intake will not be greatly influenced by the price of food.

This changes enormously in a global economy. In an open economy that has international trade, there are many customers for food exports, and many competing nations that export food. For example, the US is a major wheat exporter. The other wheat exporting nations include: Canada, Australia, Argentina, the European Union (EU), and many of the former Soviet nations in Eastern Europe. In this case, the US faces a highly elastic demand for wheat in the global economy: if the US increased the price of wheat above the world price, wheat importers would shift purchases from the US to other wheat exporters. A global economy changes the effectiveness of price policies enormously.

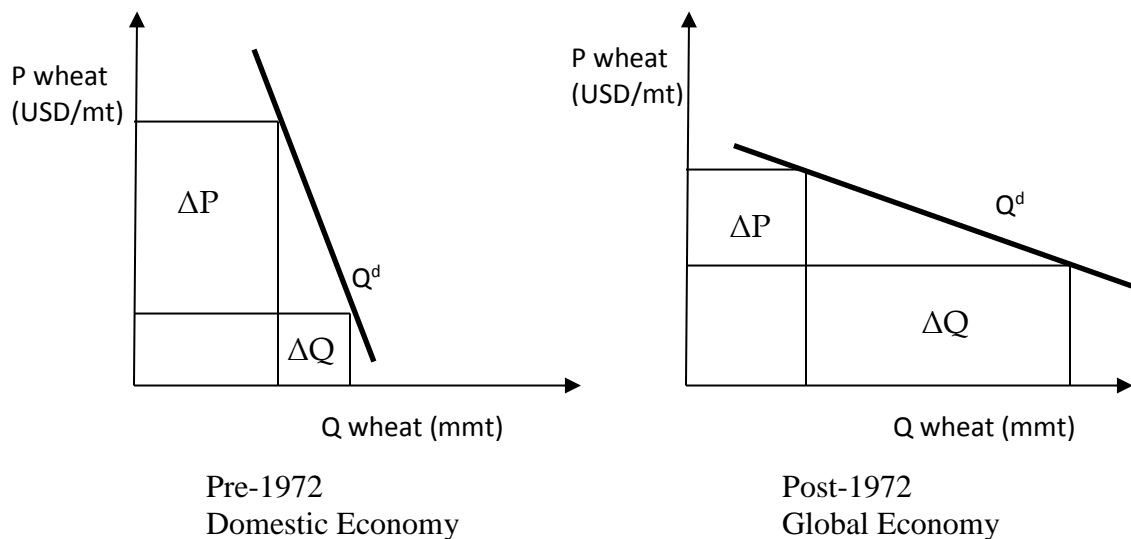


Figure 1.21 Price Elasticity and Price Policies

Prior to 1972, the United States was a domestic economy, with less food and agricultural trade. In this case, the demand for food was primarily domestic, and thus relatively inelastic (Figure 1.21).

Starting in 1933, agricultural price supports increased the price of wheat above the market equilibrium level. This policy worked well, as long as the surplus was

eliminated. One way to eliminate the surplus was through acreage restrictions, which limited the number of acres planted to wheat (ΔQ in the left panel of Figure 1.21). Acreage limitations and production quotas were used to decrease the quantity of wheat in the market. These policies worked well prior to 1972, since the US agricultural economy was primarily domestic, characterized by an inelastic demand curve. The decrease in quantity led to a larger increase in price, given the inelastic demand in a domestic economy.

In 1972, major changes in international exchange rate policies, together with poor weather in Asia, led to the globalization of US food and agricultural markets. A larger percentage of the US wheat crop was exported, and the inelastic demand that prevailed prior to 1972 became more elastic in the globalized environment (right panel, Figure 1.21). Although the wheat market became globalized, the policies did not. During the 1980s, the US maintained price supports and production controls in the seven basic commodities (can you list these?). These policies were counterproductive, as they priced the grain out of the world market. The US attempted to increase the market share of wheat trade, only to find that the US price was higher than the other major wheat exporters.

Figure 1.21 shows why the policies implemented in 1933 were hurting more than they were helping. Production controls were decreasing the quantity of wheat. In the domestic economy, this achieved the objectives of the policies: wheat producers were made better off, since the increase in price was greater than the decrease in quantity. This all changed in the globalized world after 1972. With an elastic demand, the decrease in quantity did not result in large price increases. Price supports raised the US price above the world price of wheat. These policies were not working, and in 1996, they were changed to make the US grain industry more competitive in the global market. Today, a large fraction of all grain produced in the US is exported.

In summary, policies intended to help producers are much different depending on the price elasticity of demand. In a domestic economy, the demand for food and agricultural products is typically inelastic. In this case, production controls and price supports will achieve the policy goal of helping producers: the price increases will be larger than the quantity decreases (left panel, Figure 1.21). In a global economy, the demand for food and agricultural goods is elastic: there are many nations that export grains (right panel, Figure 1.21). In this case the policy that helps producers the most is technological change, which will shift the supply curve to the right. With an elastic demand, the increase in quantity is larger than the decrease in price.

This is the same strategy that Walmart utilizes: everyday low prices. Sam Walton found that the increase in sales due to low prices more than offset the decrease in price. This is true in any market characterized by an elastic demand.

1.4.10 Calculation of Market Supply and Demand Elasticities

In Section 1.3.4 above, inverse supply and demand curves were used in the calculation of the equilibrium price and quantity of phones.

The inverse demand and supply functions were:

$$(1.18) \quad P = 100 - 2Q^d$$

$$(1.19) \quad P = 20 + 2Q^s$$

Where P is the price of phones in USD/unit, and Q is the quantity of phones in millions. By setting the two equations equal to each other, the intersection of the inverse supply and demand curves was found, yielding the equilibrium market price and quantity:

$$P^e = \text{USD } 60/\text{phones}$$

$$Q^e = 20 \text{ million phones.}$$

The graph of the phone market is replicated in Figure 1.22.

To calculate the own price elasticities of supply and demand, simple calculus provides an easy solution. Recall the definition of the own price elasticity of demand:

$$(1.20) \quad E_d = \% \Delta Q^d / \% \Delta P = (\Delta Q^d / \Delta P)(P / Q^d) = (dQ^d / dP)(P / Q^d)$$

The delta sign refers to a small change in a variable. This is the same as the derivative sign, "d." The difference is that the derivative indicates an infinitesimally small change, whereas the delta sign is a discrete change, which is the same idea, just larger.

Therefore, the delta signs can be replaced with the derivative signs in the equation that defines the price elasticity of demand.

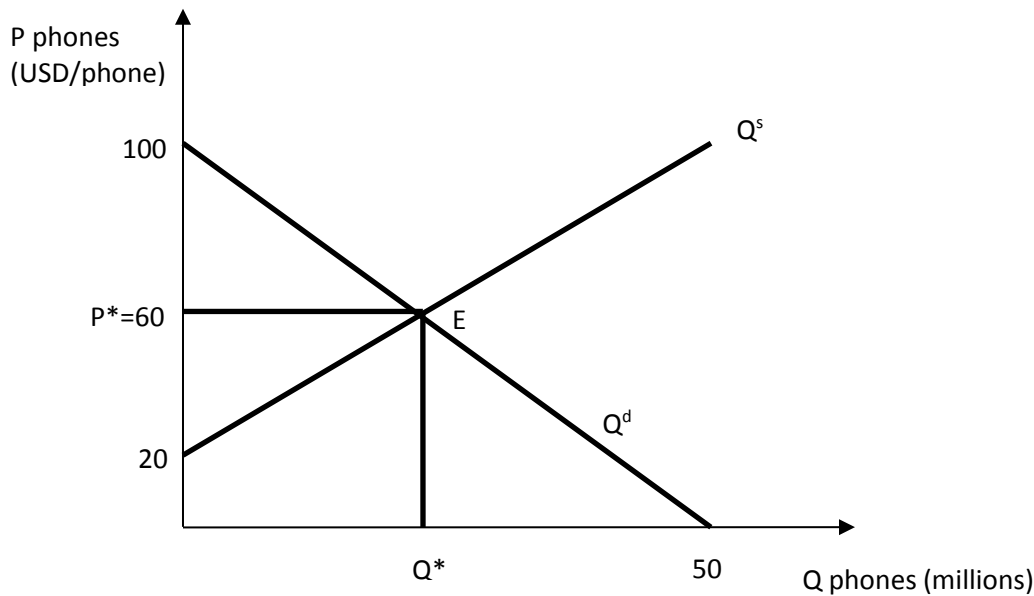


Figure 1.22 Phone Market Equilibrium

The last expression in the equation shows that to calculate E_d , use the derivative of quantity with respect to price, and the levels of P and Q . At the equilibrium point, the equilibrium levels of P and Q are known. To find the derivative, begin by taking the derivative of the inverse demand equation (Equation 1.18).

$$(1.21) \quad dP/dQ^d = -2$$

This is simply the power function rule from calculus [if $y = ax^b$, then $dy/dx = abx^{(b-1)}$]. Notice something important: the derivative of the inverse demand equation is the inverse of what is needed to calculate the price elasticity. This is due to the inverse demand function being, “price-dependent,” with P on the left hand side. To find the derivative dQ^d/dP , invert the derivative by dividing one by the derivative.

$$(1.22) \quad dQ^d/dP = -(1/2)$$

$$(1.23) \quad E_d = \% \Delta Q^d / \% \Delta P = (\Delta Q^d / \Delta P)(P / Q^d) = (dQ^d / dP)(P / Q^d) = (-1/2)(60/20) = -1.5$$

The absolute value of the own price elasticity of demand at the equilibrium point is: $|E_d| = 1.5$. The demand for phones is elastic: if the price were increased one percent, the decrease in phone purchases would be 1.5 percent.

The own price elasticity of supply can be found using the same procedure:

$$(1.24) E_s = \% \Delta Q^s / \% \Delta P = (\Delta Q^s / \Delta P)(P / Q^s) = (dQ^s / dP)(P / Q^s)$$

First, take the derivative of the inverse supply function.

$$(1.25) dP/dQ^s = + 2$$

Invert this derivative to provide the derivative needed to calculate the price elasticity of supply:

$$(1.26) dQ^s/dP = + (1/2).$$

Then plug in the ingredients of the own price elasticity of supply:

$$(1.27) E_d = \% \Delta Q^d / \% \Delta P = (\Delta Q^d / \Delta P)(P / Q^d) = (dQ^d / dP)(P / Q^d) = (1/2)(60/20) = 1.5$$

The price elasticity of supply is also elastic: a one percent increase in price results in a 1.5 percent increase in the quantity supplied of phones.

Two points are worth mentioning here. First, the price elasticities of supply and demand are not always symmetrical, as they are in this case (-1.5 and +1.5). This depends on the shape of the inverse supply and demand functions. The symmetry of the functions used here can be seen in Figure 1.22. When the inverse supply and demand functions are not symmetrical, the absolute values of the elasticities will be of different magnitudes.

The second important point is about the use of inverse supply and demand functions. The inverse functions are used to align with the “backwards” nature of the supply and demand graphs: price is the independent variable, but appears on the vertical axis. To find the derivative needed to calculate the price elasticities, the procedure above first took the derivative of the inverse function, then inverted it to achieve dQ/dP . This derivative could also be found by first, inverting the inverse function to get the quantity isolated on the left hand side, then taking the derivative. This alternative procedure will result in the same elasticity calculation as the one used above. To test your knowledge, try this procedure to double check your answers!

1.5 Welfare Economics: Consumer and Producer Surplus

1.5.1 Introduction to Welfare Economics

Welfare economics is concerned with how well off individuals and groups are. Welfare economics is not about government programs to assist the needy... that is a different type of welfare. In economics, welfare economics is used to see how the welfare, or well-being of individuals and groups changes with a change in policies, programs, or current events.

Welfare Economics = The study and calculation of gains and losses to market participants from changes in market conditions and economic policies.

1.5.2 Consumer Surplus and Producer Surplus

The two most important groups that are studied in welfare economics are producers and consumers. The concepts of **Consumer Surplus (CS)** and **Producer Surplus (PS)** are used to measure the well being of consumers and producers, respectively.

Consumer Surplus (CS) = A measure of how well off consumers are. Willingness to pay minus the price actually paid.

Producer Surplus (PS) = A measure of how well off producers are. Price received minus the cost of production.

The intuition of consumer surplus provides a good method of learning the concept. Suppose that I am on my way to the store to purchase a hammer, and I think to myself, "I am willing to pay six dollars for the hammer." When I arrive at the store, I find that the price of the hammer is four dollars. My consumer surplus is equal to two dollars: the willingness to pay minus the actual price paid. In this manner, we can add up all consumers in the market to measure consumer surplus for all consumers. This can be seen in Figure 1.23. If each point on the demand curve is considered an individual consumer, then CS is the difference between each point on the demand curve and the price line. The demand curve represents the consumers' willingness and ability to pay for a good. The CS area is a triangle, and equal to the level of consumer surplus in the market (Figure 1.23).

Similarly, the intuition of producer surplus is a good place to start. If a wheat producer can produce a bushel of wheat for four dollars, and she receives six dollars per bushel when she sells her wheat, then her level of producer surplus is equal to two dollars. Producer surplus is the price received minus the cost of production. In Figure 1.23, this is the difference between the price line and the supply curve. The market supply curve was derived by summing all individual firms' marginal cost curves. Therefore, the supply curve represents the cost of production. The PS area is the area identified in Figure 1.23.

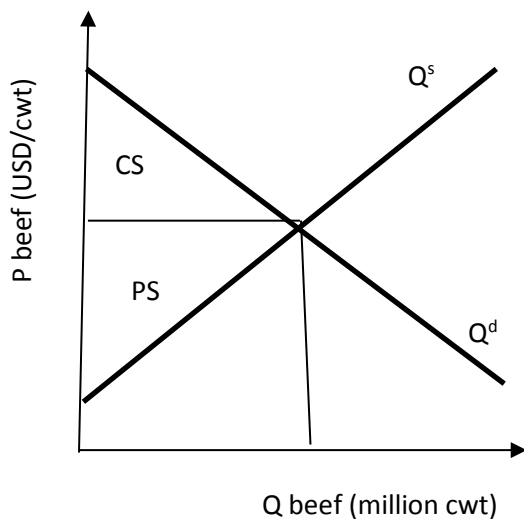


Figure 1.23 Welfare Economics of the Beef Market

These areas can be quantified to find the dollar value of consumer surplus and producer surplus. These measures place a dollar value on the well being of producers and consumers.

1.5.3 Mathematics of Consumer and Producer Surplus: Phone Market

Remember that the inverse supply and demand for phones was given by:

$$(1.28) \quad P = 100 - 2Q^d, \text{ and}$$

$$(1.29) \quad P = 20 + 2Q^s.$$

Where P is the price of phones in dollars/unit, and Q is the quantity of phones in millions. The equilibrium price and quantity of phones were calculated above in section 1.4.10:

$$P^e = \text{USD } 60/\text{phone}$$

$$Q^e = 20 \text{ million phones.}$$

These values, together with the supply and demand functions, allow us to measure the well-being of both consumers and producers. From geometry, the area of a triangle is one half base times height. To calculate CS and PS, multiply the base of the triangle times the height of the triangle in Figure 1.24, then multiply by one half (Equations 1.30 and 1.31).

$$(1.30) \quad CS = 0.5(100 - 60)(20) = 0.5(40)(20) = \text{USD } 400 \text{ million}$$

$$(1.31) \quad PS = 0.5(60 - 20)(20) = 0.5(40)(20) = \text{USD } 400 \text{ million}$$

We will use the concepts of consumer surplus and producer surplus extensively in what follows, where we will explore the consequences of policies in food and agriculture.

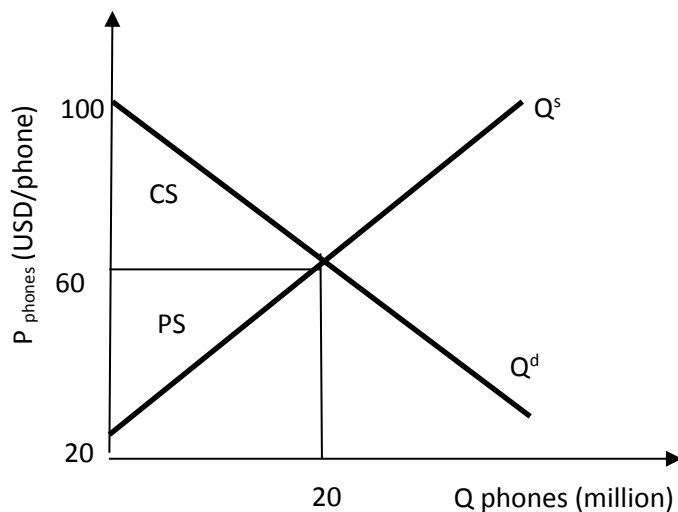


Figure 1.24 Consumer and Producer Surplus Calculations in the Phone Market

The units for both CS and PS are in terms of dollars (USD). These measures capture how well off consumers and producers are in dollars, or the dollar value of their happiness, or well-being. The units are price times quantity, or (USD/phone)*(million phones). The phone units are in both the numerator and denominator, so they are cancelled, leaving million dollars.

1.6 The Motivation for and Consequences of Free Trade

1.6.1 The Motivation for Free Trade and Globalization

Globalization and free trade result in enormous economic benefits to nations that trade. These benefits have led to high incomes in many nations throughout the world, particularly since 1950. As with all national policies, there are benefits and costs to international trade: there are winners and losers to globalization. When trade is voluntary, the gains are mutually beneficial, and the overall benefits are greater than the costs. There is a strong motivation to trade, and the nations of the world continue to become more globalized over time.

A nation's consumption possibilities are vastly increased with trade. In Northern countries such as the USA, Japan, EU, and China, fresh fruit and vegetables can be purchased during the winter from nations in the Southern hemisphere. In the United States, tropical products including coffee, sugar, bananas, cocoa, and pineapple are imported, since the costs of producing these goods are much lower in tropical climates.

The principle of comparative advantage provides large benefits to individuals, nations, and firms that specialize in what they do best, and trade for other goods. This process greatly expands the consumption possibilities of all nations, due to efficiency gains that arise from specialization and gains from trade. For example, if Canada specializes in wheat production, and Costa Rica produces bananas, both nations can be better off through specialization and trade.

A nation that does not trade with other nations is called a closed economy.

Closed Economy = A nation that does not trade. All goods and services consumed must be produced within the nation. There are no imports or exports.

Open Economy = A nation that allows trade. Imports and exports exist.

If a nation does not trade, then the closed economy must only consume what it produces. In this case, quantity supplied must equal quantity demanded ($Q^s = Q^d$). Trade allows this equality to be broken, providing the opportunity for imports ($Q^s < Q^d$) or exports ($Q^s > Q^d$). The concepts of **Excess Supply** and **Excess Demand** will be introduced to aid in understanding the motivation and consequences of free trade.

1.6.2 Excess Supply and Excess Demand

We will use wheat as an example to see how and why trade occurs. The USA is a wheat exporter. The left panel of Figure 1.25 shows the USA wheat market. At price P_e , domestic consumption (Q_d) is equal to domestic production (Q_s).

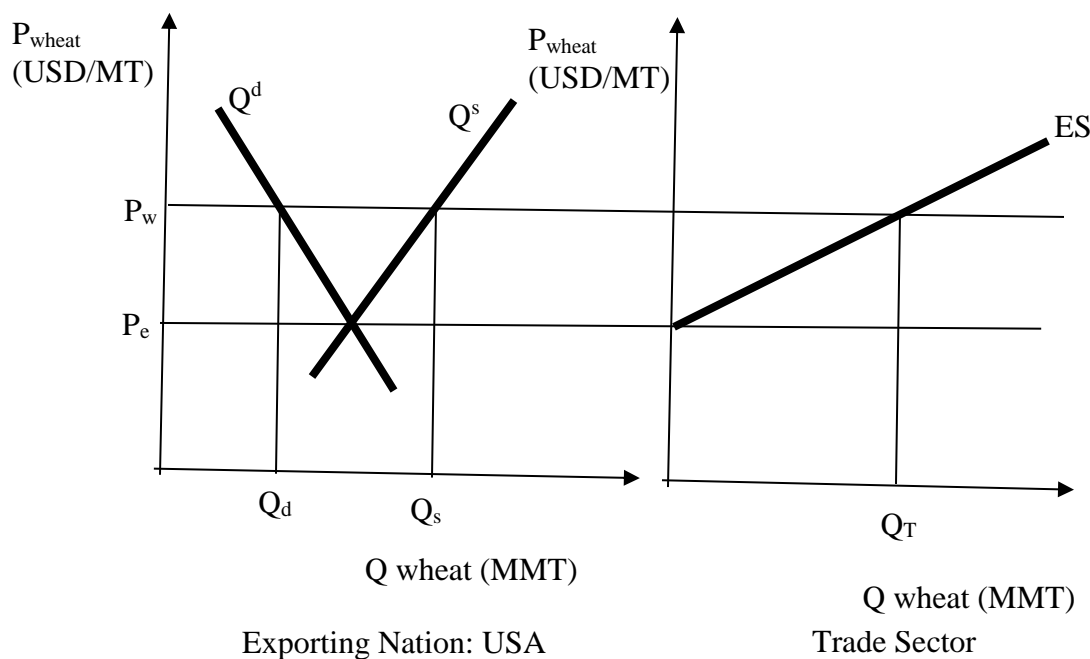


Figure 1.25 The Excess Supply of Wheat

Excess supply is defined to be the quantity of exportable surplus, or $Q^s - Q^d$. At prices higher than P_e , the quantity supplied becomes greater than the quantity demanded, and excess supply exists.

Excess Supply (ES) = Quantity supplied minus quantity demanded at a given price, $Q^s - Q^d$.

At prices higher than P_e , wheat producers increase quantity supplied along the supply curve Q^s due to the Law of Supply. Wheat consumers decrease purchases of wheat along the demand curve Q^d , due to the Law of Demand. The result is a surplus, or excess supply, at the higher price. In a closed economy, market forces would come into play to bring the higher price back down to the market equilibrium level, P_e . In an open economy, however, it is possible to maintain the high market price through exports. Free trade allows the USA to use its resource to produce more wheat than it consumes,

and export what is left over to enhance what producer revenues. Trade also provides the opportunity to buy imported goods from other nations.

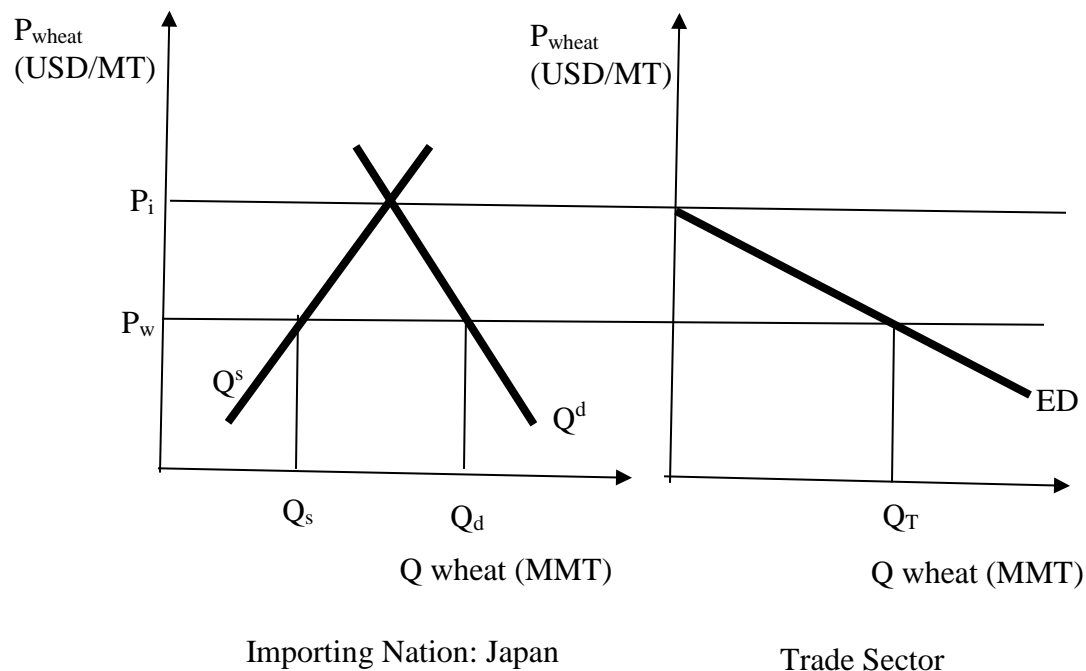


Figure 1.26 The Excess Demand of Wheat

An importing nation such as Japan is characterized by a price lower than the domestic market equilibrium price (P_i), where $Q^s = Q^d$ (Figure 1.26). In an importing nation, quantity demanded is greater than quantity supplied ($Q^s < Q^d$), and the price is lower than the market equilibrium price. If the price is lower than P_i in Figure 1.26, consumers increase purchases of the good due to the Law of Demand, and producers decrease production of the good, following the Law of Supply. This results in an Excess Demand for the good.

Excess Demand (ED) = Quantity demanded minus quantity supplied at a given price, $Q^d - Q^s$.

Note that any shift in either supply or demand of wheat in the importing nation will shift the ED curve. Domestic events in the markets for traded goods have international consequences. What happens in China has a large impact on USA wheat producers. Next, the exporting and importing nations will be linked through international trade.

1.6.3 Three Panel Diagram of Free Trade between Two Nations

Now consider the wheat exporting nation (USA) and wheat importing nation (Japan) in the same diagram, Figure 1.27. The wheat market in the exporting nation is shown in the left panel, and the wheat market in the importing nation is shown in the right panel (Figure 1.27). The trade sector is in the middle panel. Excess Demand (ED) is downward sloping, and is derived from the domestic supply and demand in the importing nation, Japan in this case. Excess Supply (ES) is upward sloping, derived from the supply and demand curves in the exporting nation, the USA. In reality, the right panel is composed of many nations, all wheat importers. For simplicity, the model here is for one importing nation and one exporting nation. As price decreases in Japan, quantity demanded increases and quantity supplied decreases, causing ED to have a negative slope. Similarly, price increases in the exporting nation (USA) result in a higher quantity supplied of wheat and a lower quantity demanded. Equilibrium in the global wheat market is found in the center panel at the point where $ED = ES$.

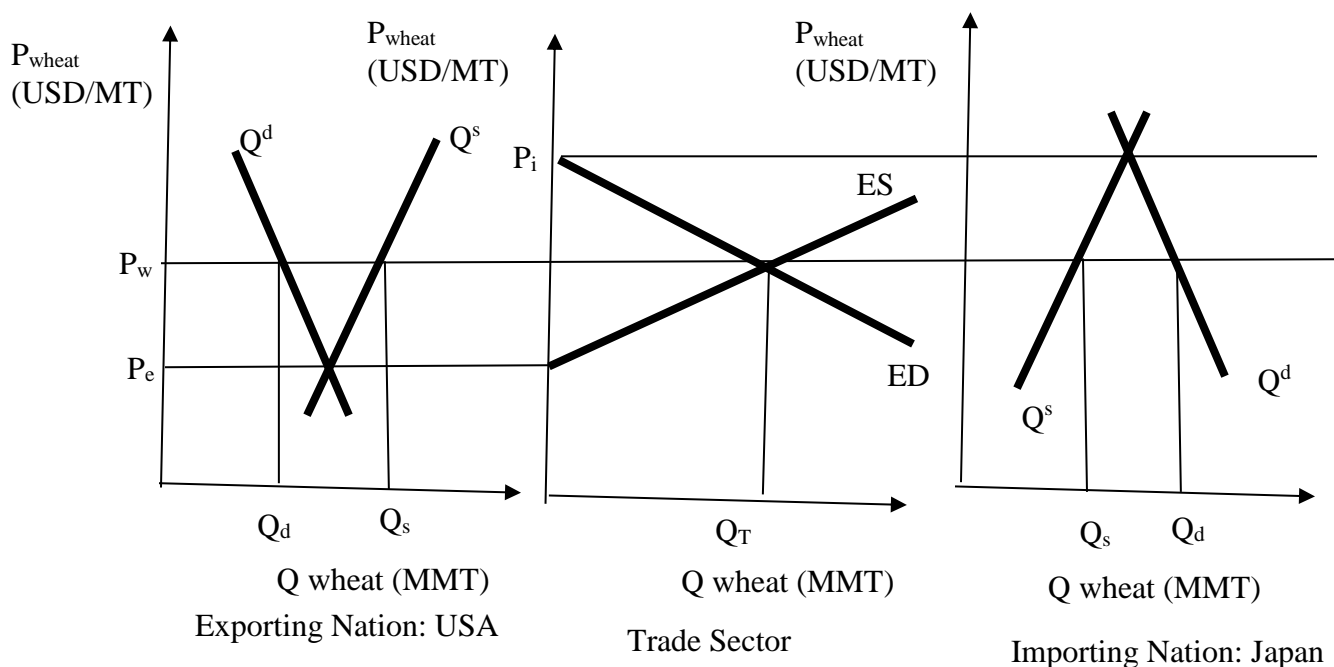


Figure 1.27 International Trade in Wheat

In a multi-nation model, this equilibrium would occur when the sum of all wheat supplied from all exporting nations is equal to the sum of all wheat demanded from all importing nations. The equilibrium quantity traded (Q_T) is equal to the quantity of wheat imported by Japan (Q_d) and the quantity of wheat exported by the USA (Q_s) since

exports must equal imports ($Q_T = \text{exports} = \text{imports}$). This equilibrium in the world market determines the world price (P_w), which is the price of wheat for all trading partners, Japan and the USA in this model.

The three-panel diagram demonstrates two important characteristics about free trade. First, the motivation for trade is simple: “buy low and sell high.” If a price difference exists between two locations, arbitrage provides profit opportunities for traders. A firm (or nation) that buys wheat at a lower price in the USA and sells the wheat at a higher price in Japan can earn profits. Note that this simple model ignores transportation costs and exchange rates. Second, anything that affects the supply or demand of wheat in either trading nation affects the global price and quantity of wheat. Therefore, all consumers and producers of a good are interconnected: the welfare of all wheat producers and consumers is affected by weather, growing conditions, food trends, and all other supply and demand determinants in all trading nations.

This point is enormously important in a globalized economy: the well-being of all producers and consumers depends on people, politicians, and current events all over the globe. The three-panel diagram is useful in understanding the determinants of food and agricultural exports: all supply and demand shifters in all wheat exporting and importing nations.

1.6.4 Welfare Impacts of International Trade

The welfare analysis of international trade can be conducted using the three-panel diagram (Figure 1.28). The welfare impacts on wheat consumers and producers can be calculated by measuring the changes in consumer surplus and producer surplus before trade (time $t=0$) and after trade (time $t=1$). The welfare changes for the exporting nation are shown in the left panel of Figure 1.28. Prior to trade, the closed economy price is P_e at the closed economy market equilibrium, where $Q_s = Q_d$. After trade, export opportunities allow the price to increase to the world price P_w . Quantity supplied increases and quantity demanded decreases. Consumers lose, since the price is now higher ($P_w > P_e$) and the quantity consumed lower. The loss in consumer surplus is equal to area A, the area between the two price lines and below the demand curve: $\Delta CS = -A$. Producers receive a higher price ($P_w > P_e$) and a larger quantity, and an increase in producer surplus equal to the area between the two price lines and above the supply curve: $\Delta PS = +A + B$.

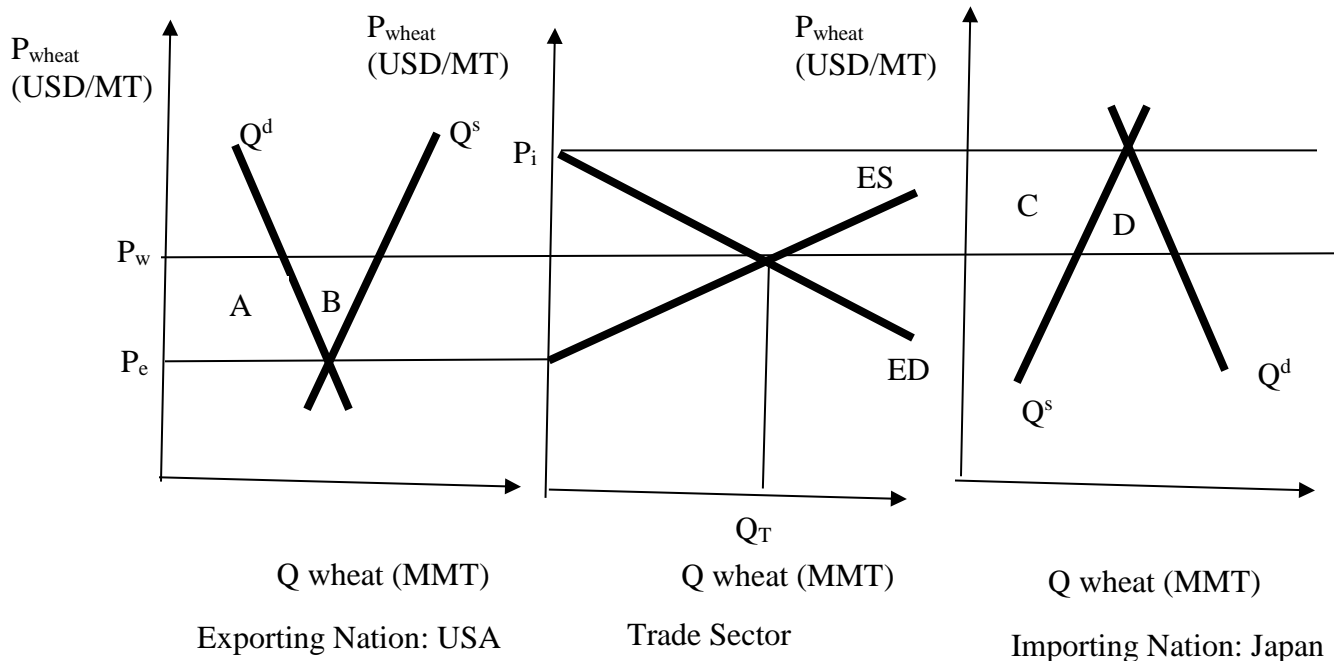


Figure 1.28 Welfare Impacts of International Trade in Wheat

The net gain to the exporting nation, or change in social welfare (SW) is: $\Delta SW = +B$, since area A represents a transfer of surplus from consumers to producers. Interestingly and importantly, the exporting nation is better off with international trade $\Delta SW > 0$, but not all individuals and groups are made better off with trade. Wheat producers in the exporting nation gain, but wheat consumers in the exporting nation lose.

In the importing nation, consumers win and producers lose from trade (right panel, figure 1.28). The pre-trade price in the importing nation is P_i , and trade provides the opportunity for imports ($Q_d > Q_s$). With imported wheat, the market price falls from P_i to the world price P_w . Quantity demanded increases and quantity supplied decreases. Consumers gain: $\Delta CS = +C + D$. Producers lose: $\Delta PS = -C$. The net gain to the importing nation, or change in social welfare (SW) is $\Delta SW = +D$. The area C represents a transfer of surplus from producers to consumers in the importing nation. As in the exporting nation, the net gains are positive, but not everyone is helped by trade. Producers in importing nations will oppose trade.

The results of the three-panel model clarify and explain the politics behind trade agreements. Politicians representing the entire nation will support the overall benefits from trade, brought about by efficiency gains from globalization. However, representatives of constituent groups who are hurt by trade will oppose new free trade

agreements. A large number of trade barriers are erected to protect domestic producers from import competition, including tariffs, quotas, and import bans.

The world is better off due to globalization and trade: the global economy gains areas B + D from producing wheat in nations that have superior grain production characteristics. These efficiency gains provide real economic benefits to both nations. However, globalization requires change, and many workers and resources will have to change jobs to achieve the potential gains. Labor with specific skills and other inflexibilities will have high adjustment costs to globalization. However, there have been huge increases in the incomes of trading nations due to moving resources from less efficient employments into more efficient employment over time.

The three panel diagram highlights who gains and who loses from trade. Producers in exporting nations and consumers in importing nations gain, in many cases enormously. Producers in importing nations and consumers in exporting nations lose, and in many cases lose a great deal. Industrial workers and textile workers in the USA and the EU used to be employed in one of the major sectors of the economy. Today, these jobs are in nations with low labor costs: China, Indonesia, and Viet Nam are examples.

Should a nation support free trade? The economic analysis provides an answer to this question: unambiguously yes. The overall benefits to society outweigh costs, with the net benefits equal to areas B and D in Figure 1.28. Economists have devised the Compensation Principle for situations when there are both gains and losses to a public policy. The Compensation Principle states that if the winners gain enough to compensate the losers, then the policy should be undertaken, from an economic point of view. The actual compensation can be difficult to achieve in the real world, but the net benefits of the program suggest that if society gain from the policy, it should be undertaken.

Agricultural producers in most high income nations are subsidized by the government. These subsidies can be viewed as compensation for the impacts of the adoption of labor-saving technological change over time. Technological change has made agriculture in the USA and the EU enormously productive. However, it has led to massive migration of labor out of agriculture. Subsidies can be viewed as the provision of compensation for the massive substitution of machines and chemicals for labor in agricultural production.

Chapter 2. Welfare Analysis of Government Policies

2.1 Price Ceiling

In some circumstances, the government believes that the free market equilibrium price is too high. If there is political pressure to act, a government can impose a maximum price on a market, also called a price ceiling.

Price Ceiling = A maximum price policy to help consumers.

A price ceiling is imposed to provide relief to consumers from high prices. In food and agriculture, these policies are most often used in low-income nations, where political power is concentrated in urban consumers. If food prices increase, there can be demonstrations and riots to put pressure on the government to impose price ceilings. In the United States, price ceilings were imposed on meat products in the 1970s under President Richard M. Nixon. Price ceilings were also used for natural gas during this period of high inflation. It was believed that the cost of living had increased beyond the ability of family earnings, and the market interventions were used to make beef, other meat, and natural gas more affordable.

2.1.1 *Welfare Analysis*

Welfare analysis can be used to evaluate the impacts of a price ceiling. In what follows, we will compare a baseline free market scenario to a policy scenario, and compare the benefits and costs of the policy relative to the baseline of free markets and competition. Consider the price ceilings imposed on the natural gas markets. The purpose, or objective, of this policy was to help consumers. We will see that the policy does help some consumers, but makes others worse off. The policy also hurts producers.

The baseline scenario for all policy analysis is free markets. Figure 2.1 shows the free market equilibrium for the natural gas market. The quantity of natural gas is in trillion cubic feet (tcf) and the price of natural gas is in dollars per million cubic feet (USD/mcf). Social welfare is maximized by free markets, because the size of the welfare area $CS + PS$ is largest under the free market scenario. As we will see, any government intervention into a market will necessarily reduce the level of surplus available to consumer and producers. All price and quantity policies will help some individuals and

groups, hurt others, and have a net loss to society. The two triangles CS and PS are as large as possible in Figure 2.1.

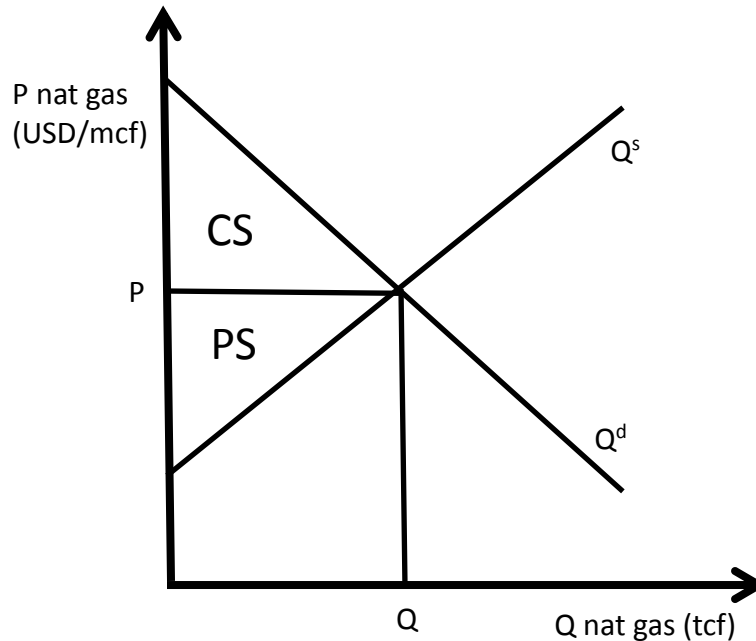


Figure 2.1 Natural Gas Market Baseline Scenario: Free Markets

The price ceiling policy is evaluated in Figure 2.2, where P' is the price ceiling. Here, the government has passed a law that does not allow natural gas to be bought or sold at any price higher than P' . For a price ceiling to have an impact, it must be set below the market price (P). If the price ceiling were to be set above P , it has no effect, since the good is bought and sold at the market price, which is below the price ceiling, and legally permissible. Such a law would not be binding on market transactions.

If the price ceiling is set at P' , then the equilibrium quantity is found at the minimum of quantity demanded and quantity supplied, as in Equation 2.1.

$$(2.1) \quad Q' = \min(Q^s, Q^d)$$

This condition states that the quantity at a nonequilibrium point will be the smallest of production or consumption. At the low price P' , producers decrease quantity supplied, and consumers increase quantity demanded, resulting in $Q' = Q^s$. This is the maximum

amount of natural gas placed on the market, although consumers desire a much larger amount.

The first step in the welfare analysis is to assign letters to each area in the price ceiling graph. Next, the letters corresponding to the baseline free market scenario are recorded (initial values have a subscript 0), followed by the surpluses under the price ceiling (ending values have a subscript 1). Finally, the change from free markets to the price policy are calculated to conclude the qualitative analysis of a price ceiling. If the supply and demand curves have numbers associated with them, a numerical analysis can be conducted.

The initial, free market values in the natural gas market at market equilibrium price P are:

$$CS_0 = A + B, \text{ and}$$

$$PS_0 = C + D + E.$$

Social welfare is defined as the total amount of surplus available in the market, $CS + PS$:

$$SW_0 = A + B + C + D + E.$$

After the price ceiling is put in place, the price is P' , and the quantity is Q' . New surplus values are found in the same way as under free markets. Consumer surplus is the willingness to pay minus price actually paid, or the area beneath the demand curve and above the price line at the new price P' ($A + C$). Producer surplus is the price received minus the cost of production, or the area above the supply curve and below the price line (E):

$$CS_1 = A + C,$$

$$PS_1 = E, \text{ and}$$

$$SW_1 = A + C + E.$$

The welfare analysis outcomes are found by calculating the changes in surplus:

$$\Delta CS = CS_1 - CS_0 = + C - B$$

$$\Delta PS = PS_1 - PS_0 = - C - D$$

$$\Delta SW = SW_1 - SW_0 = - B - D$$

The results are fascinating, since the sign of the change in consumer surplus is ambiguous, it depends on the relative magnitude of areas C and B . If demand is elastic,

and supply is inelastic, the price ceiling is more likely to yield a positive change in consumer surplus ($C > B$). The policy makes some consumers better off, and some worse off. The consumers located on the demand curve between the origin and Q' are made better off by area C, as they purchase natural gas at a lower price. Consumers located on the demand curve between Q' and Q have a lower willingness to pay, and are made worse off by the price ceiling (-B) as they are unable to purchase natural gas. The price ceiling created a shortage of natural gas, as natural gas producers reduce the quantity supplied in reaction to the legislated lower price. The decrease in quantity supplied of natural gas makes these consumers unable to buy the good.

Natural gas producers are made unambiguously worse off by the price ceiling: both the price (P) and the quantity (Q) are decreased, and the change in producer surplus due to the policy is negative (-C - D)

The term deadweight loss (DWL) is used to designate the loss in surplus to the market from government intervention, in this case a price ceiling. Deadweight loss is found by deleting the negative sign on the change in social welfare ($-\Delta SW$):

$$DWL = -\Delta SW = B + D.$$

The deadweight loss area BD is called the welfare triangle, and is typical for market interventions. Interestingly, and perhaps unexpectedly, all government interventions have deadweight loss to society. Free markets are voluntary, with no coercion. Any price or quantity restriction will necessarily reduce the surplus available to producers and consumers in a market.

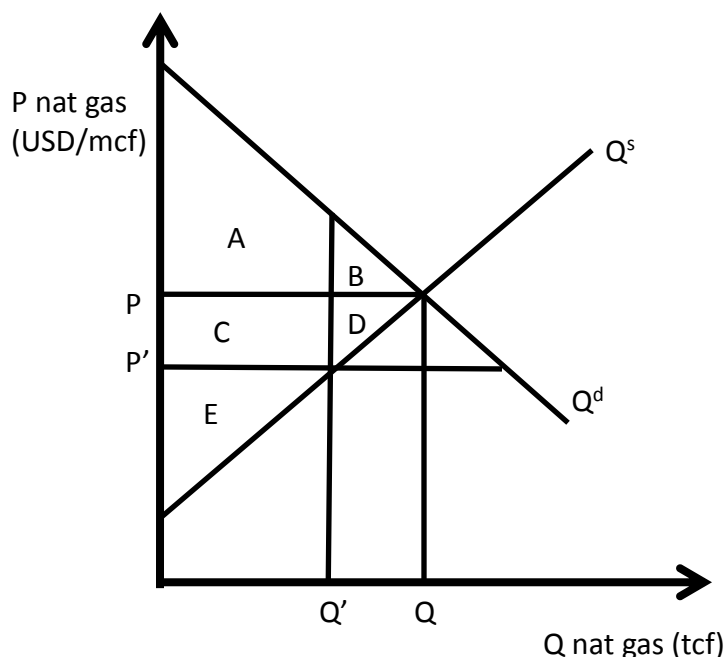


Figure 2.2 A Price Ceiling in the Natural Gas Market

As indicated above, price ceilings are most often used in low-income nations, such as in Asia and Sub-Saharan Africa. Price supports are most often used in high-income nations such as the US, EU, Japan, Australia, and Canada.

2.1.2 Quantitative Analysis

Suppose that beef producers lobby the government to pass a price ceiling on beef products. This happened in the USA in the 1970s, during a period of high inflation. Suppose that the inverse supply and demand for beef are given by:

$$(2.1) \quad P = 20 - 2Q^d, \text{ and}$$

$$(2.2) \quad P = 4 + 2Q^s.$$

Where P is the price of beef in USD/lb, and Q is the quantity of beef in million lbs. The equilibrium price and quantity of beef can be calculated by setting the inverse supply and demand equations equal to each other to achieve:

$P^e = \text{USD } 12/\text{lb}$ beef, and

$Q^e = 4$ million lbs beef.

These values, together with the supply and demand functions, allow us to measure the well-being of both consumers and producers before and after the price ceiling policy is implemented (Figure 2.3).

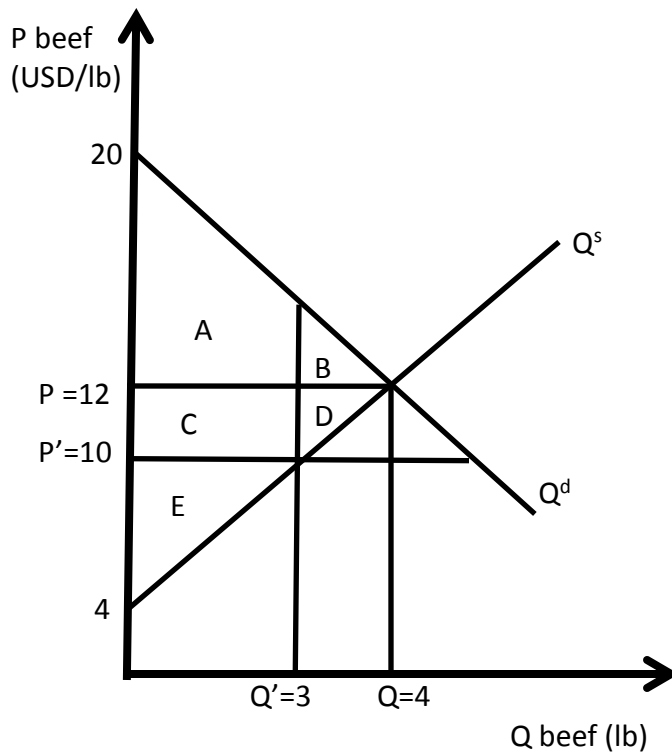


Figure 2.3 A Quantitative Price Ceiling in the Beef Market

The free-market equilibrium levels of CS and PS are designated with the subscript 0, calculated in equations 2.3 and 2.4.

$$(2.3) \quad CS_0 = A + B = 0.5(20 - 12)(4) = 0.5(8)(4) = \text{USD } 16 \text{ million}$$

$$(2.4) \quad PS_0 = C + D + E = 0.5(12 - 4)(4) = 0.5(8)(4) = \text{USD } 16 \text{ million}$$

The level of social welfare is the sum of all surplus in the market, as in equation 2.5.

$$(2.5) \quad SW_0 = A + B + C + D + E = 0.5(20 - 4)(4) = 0.5(16)(4) = \text{USD } 32 \text{ million}$$

Assume that the price ceiling is set at $P' = 10$ USD/lb beef. The quantity is found by finding the minimum of quantity supplied and quantity demanded. In the case of a binding price ceiling ($P' < P$), the quantity supplied will be the relevant quantity, since producers will produce only Q' lbs of beef. Consumers will desire to purchase a much larger amount, but are unable to at price P' , since production falls from Q to Q' . The quantity of Q' is found by substituting the new price into the inverse supply equation.

$$(2.6) \quad P = 4 + 2Q^s = 10 = 4 + 2Q^s \text{ therefore, } Q' = 3$$

This can be seen in Figure 2.3. Next, the levels of CS, PS, and SW are calculated at the price ceiling level. To find the surplus level of area A, split the shape into one triangle and one rectangle by substitution of $Q' = 3$ into the inverse demand curve to get $P = 14$. Area A is equal to: $0.5(20 - 14)3 + (14 - 12)3 = 9 + 6 = 15$ million USD. We are now ready to calculate the level of surplus for the price ceiling.

$$(2.7) \quad CS_1 = A + C = 15 + (12 - 10)(3) = 15 + 6 = \text{USD } 21 \text{ million}$$

$$(2.8) \quad PS_1 = E = 0.5(10 - 4)(3) = 0.5(6)(3) = \text{USD } 9 \text{ million}$$

$$(2.9) \quad SW_1 = A + C + E = 21 + 9 = \text{USD } 30 \text{ million}$$

The changes in welfare due to the price ceiling are:

$$(2.10) \quad \Delta CS = CS_1 - CS_0 = + C - B = 21 - 16 = \text{USD } + 5 \text{ million}$$

$$(2.11) \quad \Delta PS = PS_1 - PS_0 = - C - D = 9 - 16 = \text{USD } - 7 \text{ million}$$

$$(2.12) \quad \Delta SW = SW_1 - SW_0 = - B - D = 30 - 32 = \text{USD } - 2 \text{ million}$$

The Dead Weight Loss (DWL) of the price ceiling is the loss to social welfare, of the negative of the change in social welfare.

$$(2.13) \text{ DWL} = - \Delta \text{SW} = 2 \text{ USD million}$$

2.2 Price Support

This section continues the welfare analysis of price policies by investigating the welfare analysis of a price support, also called a minimum price. Price supports are intended to help producers. The outcome of the welfare analysis demonstrates that price supports can increase producer surplus, but at a cost to the rest of society. Figure 2.4 shows the impact of a price support in the wheat market (will this policy be used in a high-income nation or a low-income nation?).

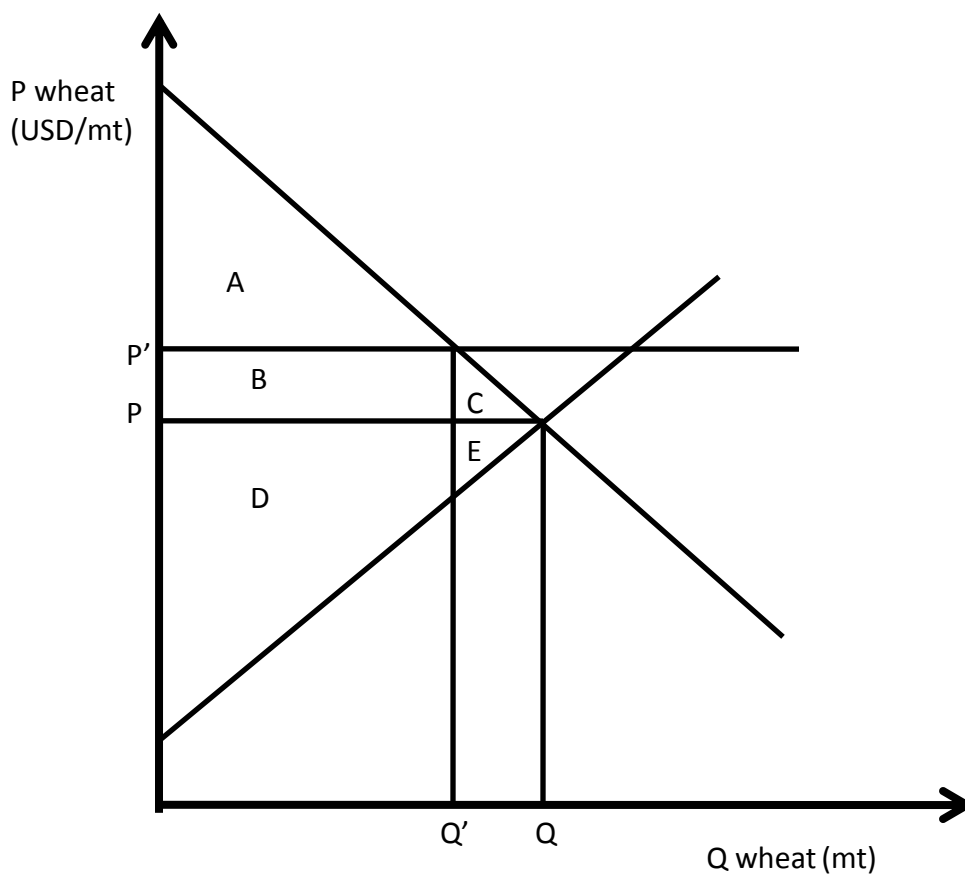


Figure 2.4 Case One: Price Support in Wheat Market, No Surplus

The price support mandates that all wheat be bought or sold at a minimum price of P' . If the price support were set at a level lower than the market equilibrium price ($P' < P$), it would have no effect. The quantity of wheat on the market depends on how the

policy works. There are three possibilities for how the price support is implemented: (1) no surplus exists, (2) the surplus exists, and (3) the government purchases the surplus.

2.2.1 Case One: Price Support with No Surplus

The first case is the simplest, but least realistic. In Case One, we assume that producers correctly forecast the quantity demanded, and produce only enough to meet demand. No surplus exists. In Figure 2.4, the price support is set at P' . Producers forego increasing quantity supplied along the supply curve to price P' , and instead produce only enough wheat to meet consumer needs, Q' :

$$Q' = \min(Q^s, Q^d).$$

In Case One, no surplus exists. The producers produce and sell only enough wheat to meet the low level of quantity demanded, Q' . The initial, free market surplus levels are:

$$CS_0 = A + B + C$$

$$PS_0 = D + E$$

$$SW_0 = A + B + C + D + E$$

After the price support is put in place, the new levels of surplus are;

$$CS_1 = A,$$

$$PS_1 = B + D, \text{ and}$$

$$SW_1 = A + B + D.$$

Changes in surplus from free markets to the price support with no surplus are:

$$\Delta CS = -B - C,$$

$$\Delta PS = +B - E,$$

$$\Delta SW = -C - E, \text{ and}$$

$$DWL = -\Delta SW = C + E.$$

Consumers are unambiguously worse off: price is higher and quantity is lower, relative to the free market case. Producers may or may not be better off, depending on the relative magnitude of areas B and E. If demand is inelastic and supply is elastic, it is more likely that producer surplus is higher with the price support ($B > E$). This reflects

the analysis of price support in the previous chapter. The producers with low production costs, located on the supply curve between the origin and Q' , are made better off since they receive a higher price for the wheat that they produce. The high-cost producers, located on the supply curve between Q' and Q , are made worse off, since they no longer produce wheat.

The deadweight loss (DWL) equals welfare triangle CE . The price support helps producers, if demand is sufficiently inelastic, but at the expense of the rest of society. In high-income nations such as the US, this policy transfers surplus from the average consumer to producers. Wheat producers have higher levels of income and wealth than the average consumers, so the policy represents a transfer of income to individuals who are better off than the consumers.

2.2.2 Case Two: Price Support When Surplus Exists

Case Two is more realistic than Case One. In Case Two, wheat producers increase quantity supplied to Q'' , found at the intersection of P' and the supply curve. This is shown in Figure 2.5. At the price support level P' , consumers purchase only Q' , so a surplus exists equal to $Q'' - Q'$. The initial values of surplus at free market levels are:

$$CS_0 = A + B + C,$$

$$PS_0 = D + E, \text{ and}$$

$$SW_0 = A + B + C + D + E.$$

After the price support is put in place, the new levels of surplus reflect the large costs of producing the surplus, with no buyers. The cost of producing the surplus is the area under the supply curve, between Q' and Q'' : GHI . The area GHI is the cost of producing the surplus, $Q'' - Q'$, since it is the area under the supply curve. The surplus levels with the price support, assuming that the surplus exists are:

$$CS_1 = A,$$

$$PS_1 = B + D - G - H - I, \text{ and}$$

$$SW_1 = A + B + D - G - H - I.$$

Changes in surplus from free markets to the price support with the surplus are:

$$\Delta CS = -B - C,$$

$$\Delta PS = +B - E - G - H - I,$$

$$\Delta SW = -C - E - G - H - I, \text{ and}$$

$$DWL = -\Delta SW = C + E + G + H + I.$$

The impact on consumers remains the same as in Case One, but the impact on producers is much costlier. The surplus is costly to produce, and does not have a buyer. If this policy were to be implemented, the government would have to do something with the surplus created by the policy, or market forces would put pressure on the wheat market to return to equilibrium.

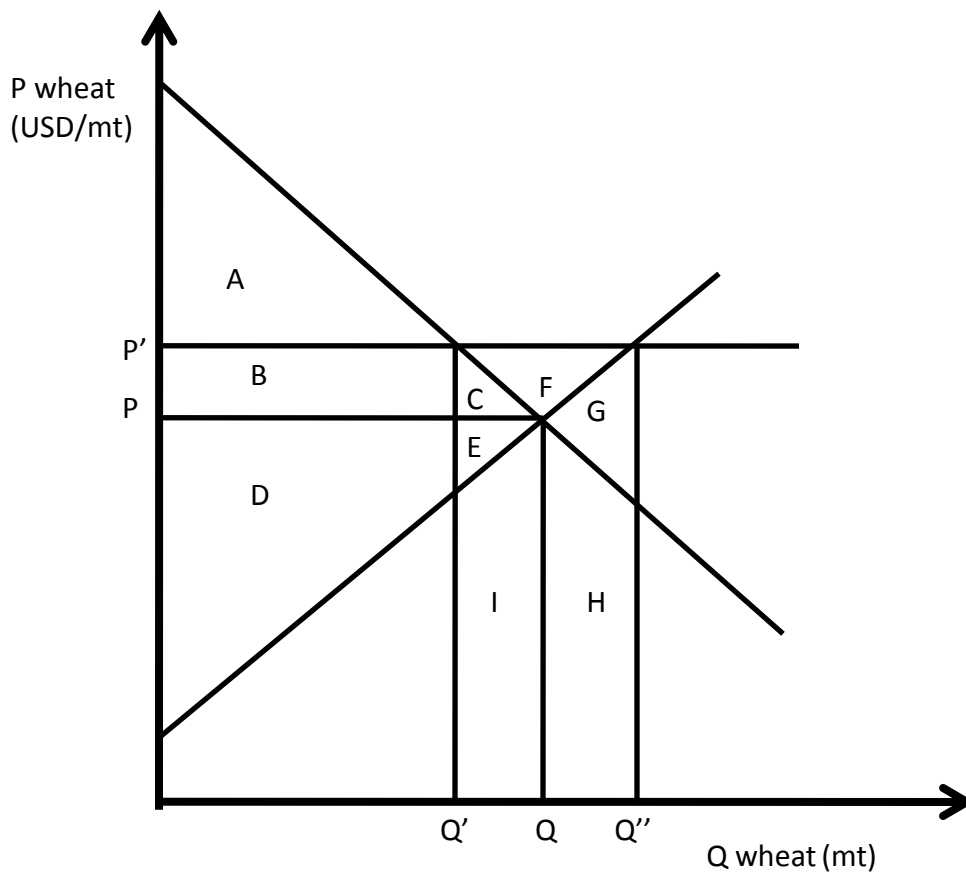


Figure 2.5 Case Two: Price Support in Wheat Market, Surplus Exists

2.2.3 Case Three: Price Support When Government Purchases Surplus

The surplus created by a price support is costly to producers, and if nothing is done to eliminate the surplus, the policy does not achieve the objective of helping producers. There are three methods for the government to eliminate the surplus:

1. Destroy the surplus,
2. Give the surplus away domestically, and
3. Give the surplus away internationally.

In all three cases, the government purchases the surplus at the price support level. This is the only way to maintain the price support. Without government purchases, the surplus would put downward pressure on the price of wheat. Destroying the surplus is not politically popular, since it involves eliminating food when there are hungry people in the world. The US did this in earlier decades by dumping surplus grain in the ocean, killing baby pigs, and dumping milk on the ground. This was not popular with consumers, producers, or politicians. The practice of destroying food is not used today.

Domestic food programs make more sense as a method of eliminating the surplus. School breakfast and school lunch programs make use of the surpluses by assisting those in need. Food aid and other forms of international assistance are also popular programs that help the US producers and the recipient consumers. Food aid can be controversial, since it lowers food prices in receiving nations, and can cause “dependency” of the recipient on the donor nation.

Case Three is shown in Figure 2.6, where the government purchases the surplus ($Q'' - Q'$).

The initial values of surplus at free market levels are:

$$CS_0 = A + B + C,$$

$$PS_0 = D + E,$$

$$G_0 = 0, \text{ and}$$

$$SW_0 = A + B + C + D + E.$$

Note that the government (G) is included in this welfare analysis. After the price support is put in place, the new levels of surplus reflect the large costs of the government buying the surplus. The cost of producing the surplus ($Q'' - Q'$) at the price support level equals $P'(Q'' - Q')$, which is equal to area CEFGHI. is the area under the

supply curve, between Q and Q'' : GHI . The surplus levels with the price support, assuming that the surplus exists are:

$$CS_1 = A,$$

$$PS_1 = B + C + D + E + F,$$

$$G_1 = -C - E - F - G - H - I, \text{ and}$$

$$SW_1 = A + B + D - G - H - I.$$

Changes in surplus from free markets to the price support with the surplus are:

$$\Delta CS = -B - C,$$

$$\Delta PS = +B + C + F,$$

$$\Delta G = -C - E - F - G - H - I,$$

$$\Delta SW = -C - E - G - H - I, \text{ and}$$

$$DWL = -\Delta SW = C + E + G + H + I.$$

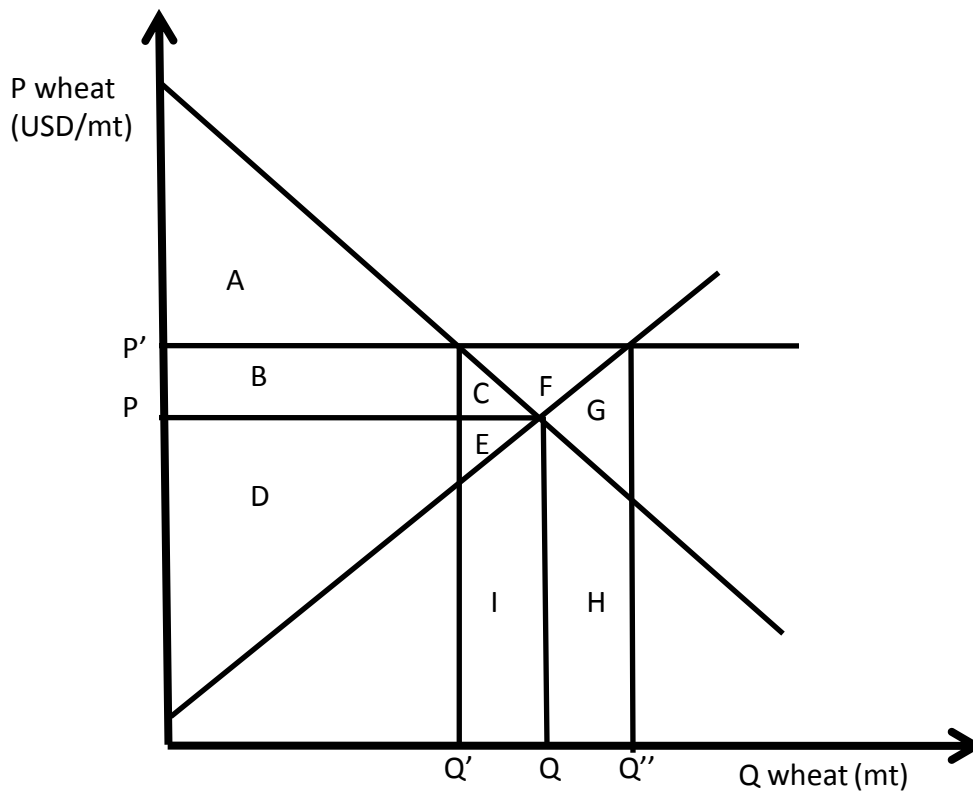


Figure 2.6 Case Three: Price Support in Wheat Market, Government Purchases Surplus

The overall societal surplus changes are identical in Cases 2 and 3: $DWL = CEGHI$ in both cases. The distribution of benefits is quite different, however. In Case 2, the

producers bear the large costs of overproduction: $-GHI$. The government has attempted to help producers, but has decreased producer surplus due to the unintended consequence of producing too much food at the high level of the price support. If the government does purchase the surplus as in Case 3, these high costs are shifted to taxpayers, and producers are helped by the price support program.

The price support does meet the objective of helping producers in Case 3, but at a high cost to society. As in the case of the price ceiling, the price support results in losses to society ($DWL > 0$). This is true of all government interventions into the market. The maximum level of surplus occurs with free markets and free trade. There are numerous cases of government intervention into markets, reflecting objectives other than maximizing social welfare.

2.2.4 Quantitative Analysis of a Price Support

Suppose that wheat producers are successful in their efforts to convince Congress to pass a law that authorizes a price support for wheat. Suppose that the inverse supply and demand for wheat are given by:

$$(2.1) \quad P = 10 - Q^d, \text{ and}$$

$$(2.2) \quad P = 2 + Q^s.$$

Where P is the price of wheat in USD/MT, and Q is the quantity of wheat in million metric tons (MMT). The equilibrium price and quantity of wheat are calculated by setting the inverse supply and demand equations equal to each other to achieve:

$$P^e = \text{USD } 6/\text{MT wheat, and}$$

$$Q^e = 4 \text{ MMT wheat.}$$

These values, together with the supply and demand functions, allow us to measure the changes in surpluses for both consumers and producers due to the price support (Figure 2.7).

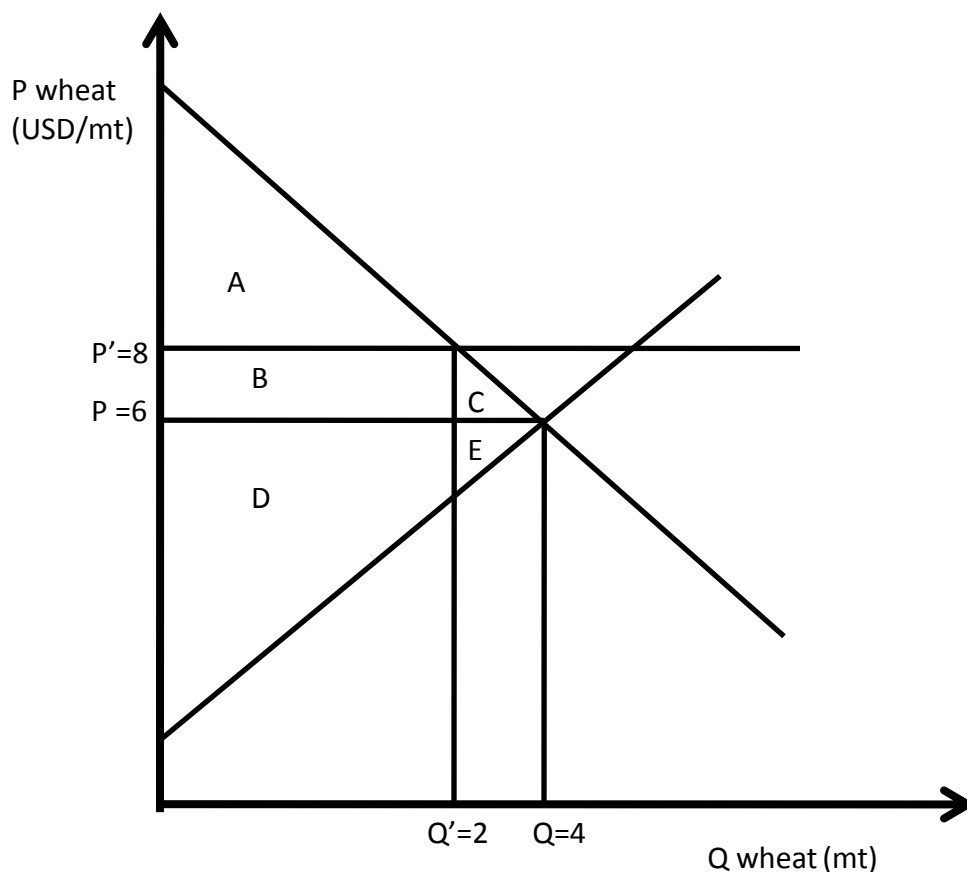


Figure 2.7 Case One: Quantitative Price Support in Wheat Market, No Surplus

The calculations will proceed by directly determining the changes in surplus, rather than calculating the initial and ending values of surplus, as we did for the price ceiling. To find the dollar values of the areas in Figure 2.7, proceed by recalling that you can always find a price or quantity by substitution of a P or Q into the inverse supply or inverse demand curve. There is always enough information provided to find the areas.

Assume that the price support is set at $P' = 8$ USD/MT wheat. The quantity is found by: $\min(Q^s, Q^d)$. Therefore, the quantity is Q' , the quantity demanded. Surplus changes are:

$$\Delta CS = -B - C = -4 - 2 = -6 \text{ USD million}$$

$$\Delta PS = +B - E = +4 - 2 = +2 \text{ USD million}$$

$$\Delta G = 0$$

$$\Delta SW = -C - E = -2 - 2 = -4 \text{ USD million}$$

$$DWL = -\Delta SW = C + E = +4 \text{ USD million}$$

The government does nothing in Case One, and producers supply only enough wheat to the market to meet consumer demand. Case Two is shown in Figure 2.8. In Case Two, producers produce a large amount of wheat (Q'') due to the high price P' . There is a large surplus created, but in this case there is no intervention by the government. Wheat producers have very large costs, as they produce 6 million metric tons, and consumers only purchase 2 million metric tons (Figure 2.8).

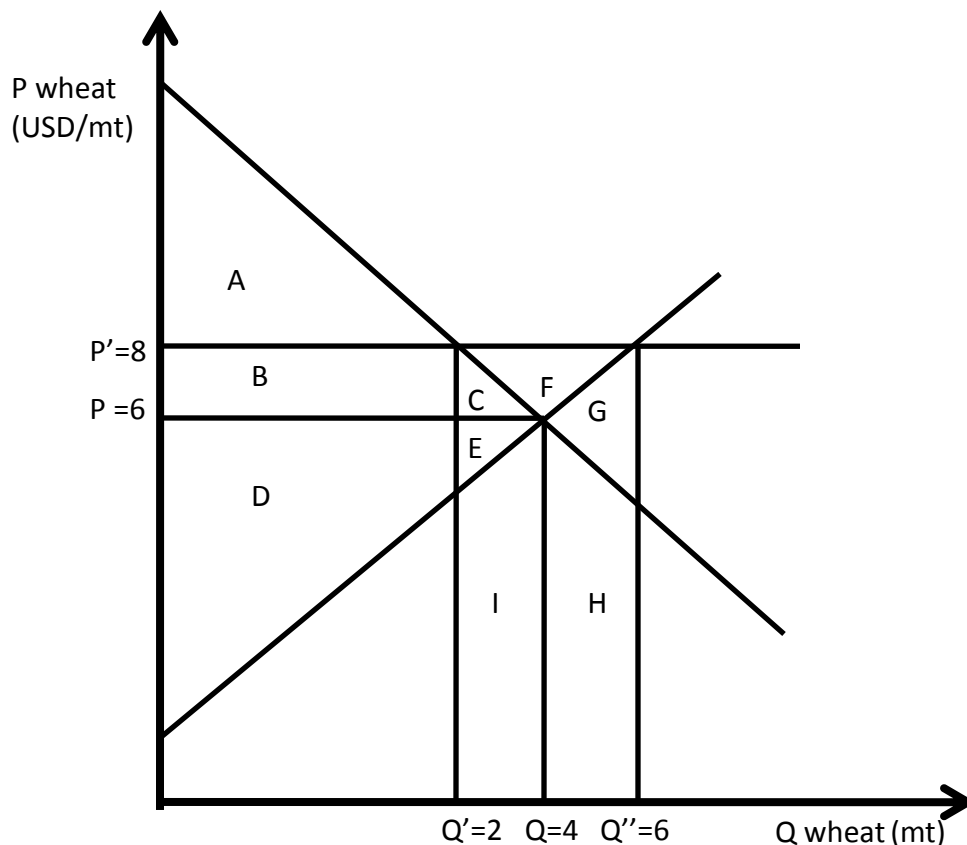


Figure 2.8 Case Two: Quantitative Price Support in Wheat Market, Surplus Exists

$$\Delta CS = -B - C = -4 - 2 = -6 \text{ USD million}$$

$$\Delta PS = +B - E - G - H - I = +4 - 26 = -22 \text{ USD million}$$

$$\Delta G = 0$$

$$\Delta SW = -C - E - G - H - I = -28 \text{ million USD million}$$

$$DWL = -\Delta SW = C + E + G + H + I = +28 \text{ USD million}$$

In Case Three, the government intervenes and buys the surplus. This allows the price to stay at the price support level, P' . Quantity supplied and quantity demanded are at the same levels as in Case Two, but the government's expenses are large, and wheat producers benefit from the high price and larger quantity sold (Figure 2.9).

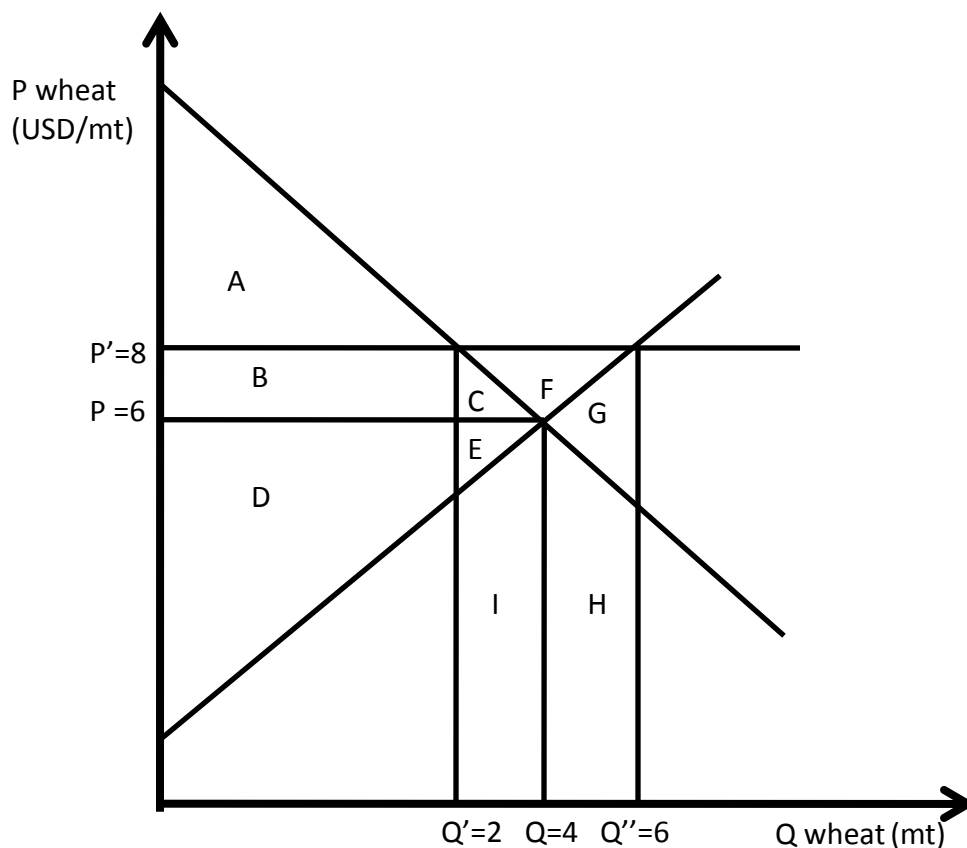


Figure 2.9 Case Three: Quantitative Wheat Price Support, Government Buys Surplus

$$\Delta CS = -B - C = -4 - 2 = -6 \text{ USD million}$$

$$\Delta PS = +B + C + F = 4 + 2 + 4 = +10 \text{ USD million}$$

$$\Delta G = -C - E - F - G - H - I = -32 \text{ USD million}$$

$$\Delta SW = -C - E - G - H - I = -28 \text{ USD million}$$

$$DWL = -\Delta SW = C + E + G + H + I = +28 \text{ USD million}$$

In Case Three, the price support has large costs, paid for by the government. One benefit that is not explicitly included is the food aid provided to domestic and foreign consumers. These benefits provide noneconomic gains, but no added surplus value to the program. Price supports can increase producer surplus, but at a cost. Government interventions often have unintended consequences, such as the surplus in this case.

2.3 Quantitative Restriction

Governments in high income nations often subsidize agricultural producers. A price support is one public policy intended to increase producer surplus. The unintended consequence of the price support is a large surplus that is costly to either producers, the government, or both. Another policy intended to help producers is a quantitative restriction, also called output control or supply control. The idea of supply control is to decrease output in order to increase the price. The analysis of elasticity in Chapter One demonstrated that this policy would work only if the demand for the good is inelastic.

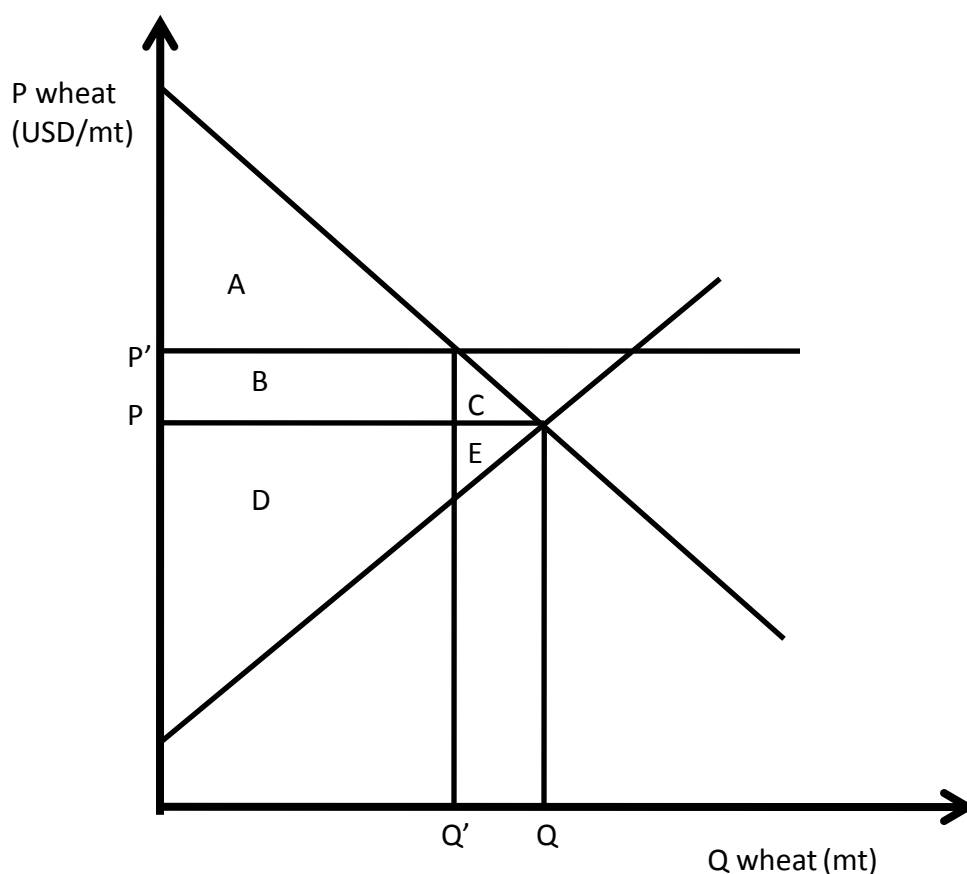


Figure 2.10 Quantitative Restriction in Wheat Market

A quantitative restriction in the wheat market is shown in Figure 2.10. Wheat output is restricted to Q' , resulting in a higher price P' . The welfare analysis of this policy is identical to that of a price support: if wheat output is reduced by an amount that raises

the price to P' , the policy is equivalent to Case One of the Price Support analyzed in the previous section. The welfare analysis of the quantitative restriction in Figure 2.10 is:

$$\Delta CS = -B - C,$$

$$\Delta PS = +B - E,$$

$$\Delta SW = -C - E, \text{ and}$$

$$DWL = -\Delta SW = C + E.$$

The magnitudes of these welfare changes depend on the elasticities of supply and demand. Note that producers only gain if the demand curve is sufficiently inelastic. If the demand is sufficiently inelastic, then $B > E$, and the change in producer surplus is positive. However, if the demand is sufficiently elastic relative to the elasticity of supply, then $B < E$, and producers lose. This result emphasizes one of the important agricultural policy conclusions of this course: in a global economy, the demand for agricultural goods is elastic due to global competition, and price supports and supply control will hurt producers more than they will help them. The welfare analysis of the quantitative restriction highlights this.

The benefit of the quantitative restriction is the lack of a surplus, which is a costly weakness of price supports. One difficulty with supply control is administration and enforcement. Wheat producers will not be free to choose how much wheat that they produce. Instead, the government will allow only a certain amount of wheat produced by each farmer, called a quota. This can be accomplished through acreage controls also, where wheat producers can only plant a percentage of their total acreage to wheat. This is an imperfect policy, since producers could increase yield per acre on the acres that they are allowed to plant. If the output is restricted, it is difficult to enforce the policy, and if overproduction occurs, it is difficult to remove the surplus.

Although government programs and policies are well intended, they often cause unintended problems. Price supports and quantitative restrictions can help producers, but at the expense of consumers.

2.4 Import Quota

The benefits of free trade have been emphasized in this course. Free markets and free trade are based on voluntary, mutually-beneficial transactions that make both trading partners better off. The global economic gains from free trade have been enormous, as they enhance efficiency of resource use. Comparative advantage and gains from trade allow each individual, firm, or nation to “do what they do best, and trade for the rest.”

Not everyone wins from trade, however. The overall net benefits are positive, but there are winners and losers from trade. Specifically, producers in importing nations and consumers in exporting nations lose due to price changes that negatively affect them. Like all public policies, free trade has winners and losers.

Trade barriers are most often erected to protect domestic producers from imports. Sugar is produced in the United States, but at higher production costs than sugar production in tropical climates found in Cuba, the Dominican Republic, and Haiti. If free trade prevailed, all sugar consumed in the USA would be imported, since it is cheaper to buy sugar than to produce it domestically. Sugar producers are interested in maintaining sugar production in the USA, as this is how they make their living. Agricultural trade policy has limited sugar imports to a much smaller amount than the free trade level, through a sugar quota, demonstrated in Figure 2.11.

In a closed economy, market forces ensure that supply and demand are equal ($Q^s = Q^d$). If the USA were a closed economy, the price of sugar would be very high, well above the world market price of sugar P_w . Suppose that the USA is a “small nation” purchaser of sugar: this means that the USA is a “price taker,” facing a constant world price of sugar for all quantities purchased. This is represented as a horizontal line at P_w in Figure 2.11. At the world price of P_w , the USA would produce Q^s domestically and consume Q^d . The difference between quantity demanded and quantity supplied is imports ($Q^d - Q^s$). The equality of domestic supply and demand has been broken by the ability to import less expensive sugar from other nations.

Domestic sugar producers lobby the government for protection, and receive it in the form of a sugar quota, meaning a maximum amount of sugar imports. The right to import sugar is auctioned off to the highest bidder, who pay for the right to import sugar. Suppose that the quota is set at $Q^d - Q^s$. This level of imports is the horizontal distance between Q^d and Q^s in Figure 2.11. At this quota level, the price of sugar increases to P' , since the quantity of sugar in the market is reduced from free market

levels. At this high price (P'), quantity supplied increases from Q^s to $Q^{s'}$, and quantity demanded decreases from Q^d to $Q^{d'}$. These changes are due to the quota, which decreases the amount of sugar allowed into the country. Sugar producers are pleased with this policy, since the price is higher and domestic quantity supplied larger.

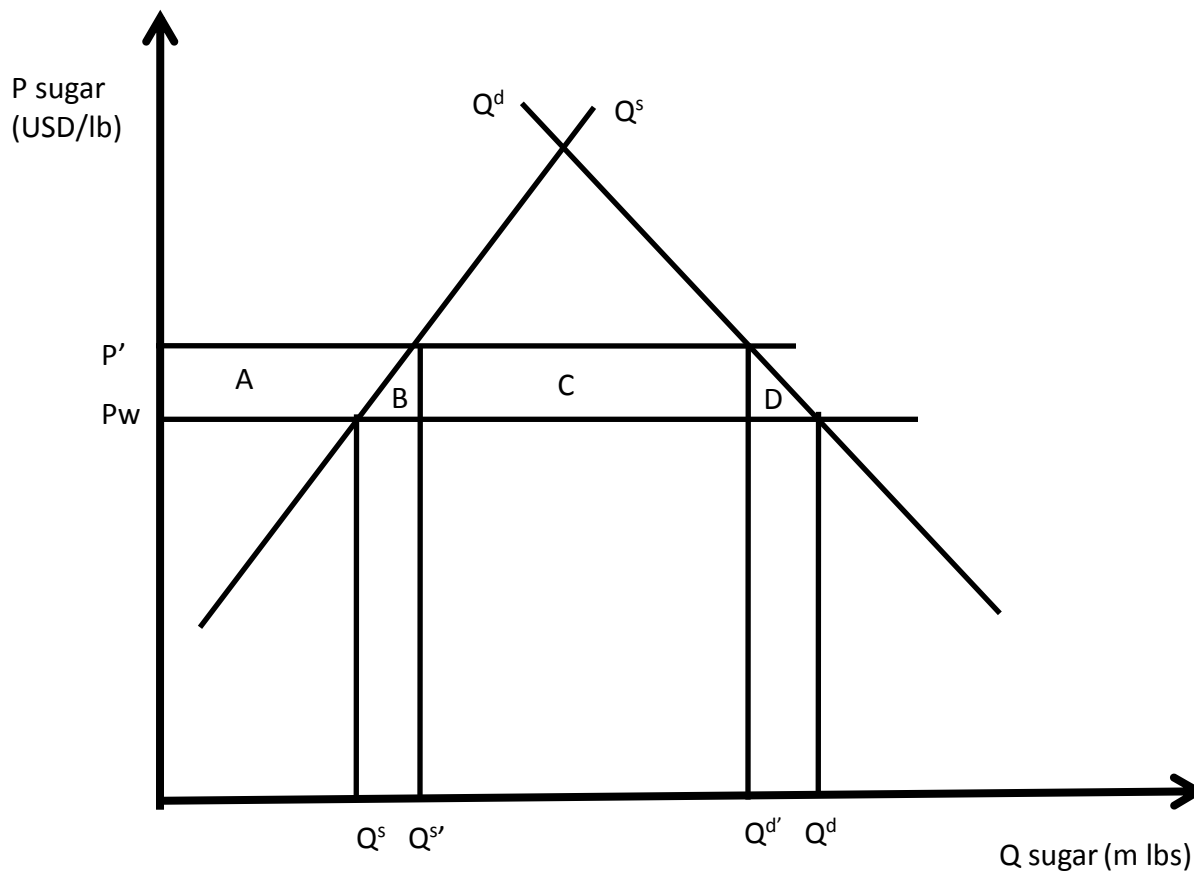


Figure 2.11 Sugar Import Quota

2.4.1 Welfare Analysis of an Import Quota

The welfare analysis of the import quota identifies the changes in economic surplus of producers, consumers, and the government. The government gains from selling the import quota permits to the sugar importers. These firms will compete with each other to win the right to import sugar. The firms will bid up the price in an auction until the price is equal to the market value of the quota. In this case, the market value is equal to $(P' - P_w)$, since this is the gain from importing one pound of sugar into the USA. The complete welfare analysis is:

$$\Delta CS = -A - B - C - D,$$

$$\Delta PS = +A,$$

$$\Delta G = +C,$$

$$\Delta SW = -B - D, \text{ and}$$

$$DWL = B + D.$$

Producers gain, but at large costs to consumers. The government gains from the sale of the quota permits to sugar importers. Sugar consumers are made much worse off from this policy. The area B is called the “production loss” of the policy. This area is equal to the losses of using scarce resources to produce sugar in the USA instead of buying it at the world price. Area B represents the production costs, since it is the area under the supply curve, and above the price. These resources could be more efficiently used producing something other than sugar. Area D is called the “consumption loss” of the import quota. This is the area under the demand curve and above the world price, which represents the extra dollars spent by US consumers buying domestic sugar instead of low-cost imported sugar. Areas B and D represent the loss in social welfare, or the deadweight loss of the government intervention. Free markets and free trade would provide efficiency of resource use and lower costs to consumers.

In the USA, sugar prices are typically one to two times higher than the world price, resulting in billions of dollar losses to sugar consumers. This policy also has an interesting unintended consequence. High fructose corn syrup (HFCS) is a perfect substitute in consumption for sucrose (sugar made from sugar cane or sugar beets). Corn producers lobby to maintain the sugar import quota, to keep the price of sugar high. When sugar price is high, buyers of sugar (Coca Cola, Pepsi, Mars, etc.) switch out of sucrose and into fructose. Corn farmers are among the largest supporter of the sugar import quota!

2.4.2 Quantitative Welfare Analysis of an Import Quota

Suppose that the inverse demand and supply of sugar are given by:

$$P = 100 - Q^d, \text{ and}$$

$$P = 10 + Q^s,$$

Where P is the price of sugar in USD/lb, and Q is the quantity of sugar in million pounds. Suppose also that the world price of sugar is given by $P_w = 20$ USD/lb, as shown in Figure 2.12. In a closed economy, market equilibrium would be found where supply equals demand:

$$Q^e = 45 \text{ million pounds of sugar and } P^e = 55 \text{ USD/lb.}$$

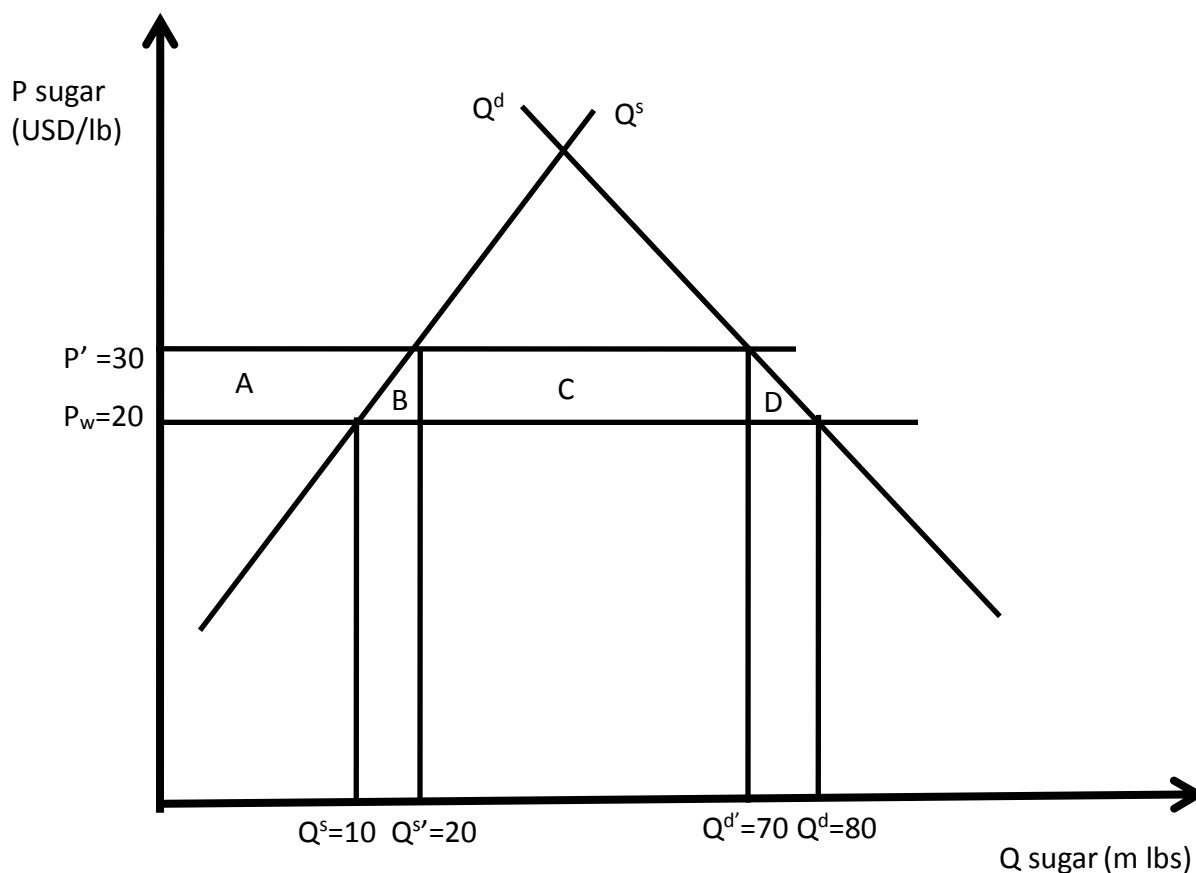


Figure 2.12 Quantitative Sugar Import Quota

This is a high price of sugar relative to the world price. If imports are allowed, the USA can break the equality of production and consumption through imports of less expensive sugar. If we assume that the USA is a “small nation” in sugar trade, then the USA is a price taker, and can import as much or as little sugar as it desires at the world price. Note that a “large nation” means that a country is a price maker, and has enough market power to influence the price of the imported good.

The free market equilibrium in an open economy can be calculated by substitution of the world price into the inverse supply and demand functions. At the world price, $Q^s = 10$ m lbs sugar and $Q^d = 80$ m lbs sugar. Imports are equal to $Q^s - Q^d = 70$ m lbs sugar. Social welfare is maximized at this free trade equilibrium, since sugar is produced by the lowest cost producers. Ten m lbs are produced by domestic producers along the supply curve below the world price, and 70 m lbs are produced by foreign sugar producers at the world price of 20 USD/lb.

Now assume that a sugar import quota is implemented, equal to 50 m lbs of sugar. Since this is less than the free trade import level, it will decrease the amount of sugar available in the USA, and cause price to increase. The sugar price that results from the quota (P') can be calculated using the inverse supply and demand curves and the import quota:

$$Q^d - Q^s = 50,$$

$$P' = 100 - Q^d, \text{ and}$$

$$P' = 10 + Q^s.$$

Rearranging the first equation: $Q^d = 50 + Q^s$. Substitution of the first equation into the inverse demand equation yields:

$$P' = 100 - (50 + Q^s) = 50 - Q^s.$$

This equation can be set equal to the inverse supply equation:

$$P' = 50 - Q^s = 10 + Q^s.$$

Solving for Q^s :

$$2Q^s = 50 - 10, \text{ or } Q^s = 40/2 = 20 \text{ m lbs sugar.}$$

Substituting this into the import equation and the inverse supply function yield:

$$P' = 30 \text{ USD/lb, and}$$

$$Q^d = 70 \text{ m lbs sugar.}$$

These values are all shown in Figure 2.12. Notice that quantity supplied has increased and quantity demanded has decreased due to the import quota and the resulting higher price. The welfare analysis can now be conducted by calculation of the areas in the graph.

$$\Delta CS = -A - B - C - D = -750 \text{ USD million}$$

$$\Delta PS = +A = +150 \text{ USD million}$$

$$\Delta G = +C = +500 \text{ million}$$

$$\Delta SW = -B - D = -100 \text{ USD million}$$

$$DWL = B + D = +100 \text{ million}$$

The government gains area C by auctioning off the permits that allow firms to import sugar. Taxes are analyzed in the next section.

2.5 Taxes

Taxes are often imposed to provide government revenue. The government also uses taxes to decrease the consumption of a good such as alcohol or tobacco. These taxes are called “sin taxes,” on goods that are not favored by society. These goods often have inelastic demands, which allows the government to apply a tax and earn revenues. Taxes can also be used to meet environmental objectives, or other societal goals: goods such as gasoline and coal emissions are taxed.

There are two types of tax: (1) specific tax, and (2) ad valorem tax.

Specific Tax = A tax imposed per-unit of the good to be taxed.

Ad Valorem Tax = A tax imposed as a percentage of the good to be taxed.

Both types of tax have the same qualitative effects, so we will study a specific, or per-unit tax ($t = \text{USD/unit}$). Taxes result in price changes for both buyers and sellers of a good. The welfare analysis of a tax provides important results on who pays for the tax: the buyers or sellers? The term, tax incidence refers to how a tax is divided between buyers and sellers. Let P_b be the buyer’s price, and P_s be the seller’s price. In markets without a tax, buyers and sellers both pay the same equilibrium market price ($P_b = P_s$). In a market for a taxed good, however, this equality is broken. With a tax, the buyer’s price is higher than the seller’s price by the amount of the tax:

$$P_b = P_s + t$$

Economists say that the tax drives a wedge between the buyer’s price and the seller’s price, as shown in Figure 2.13. The specific tax (t) is equal to the vertical distance between P_b and P_s . The tax incidence, or who pays for the tax, depends of the elasticities of supply and demand.

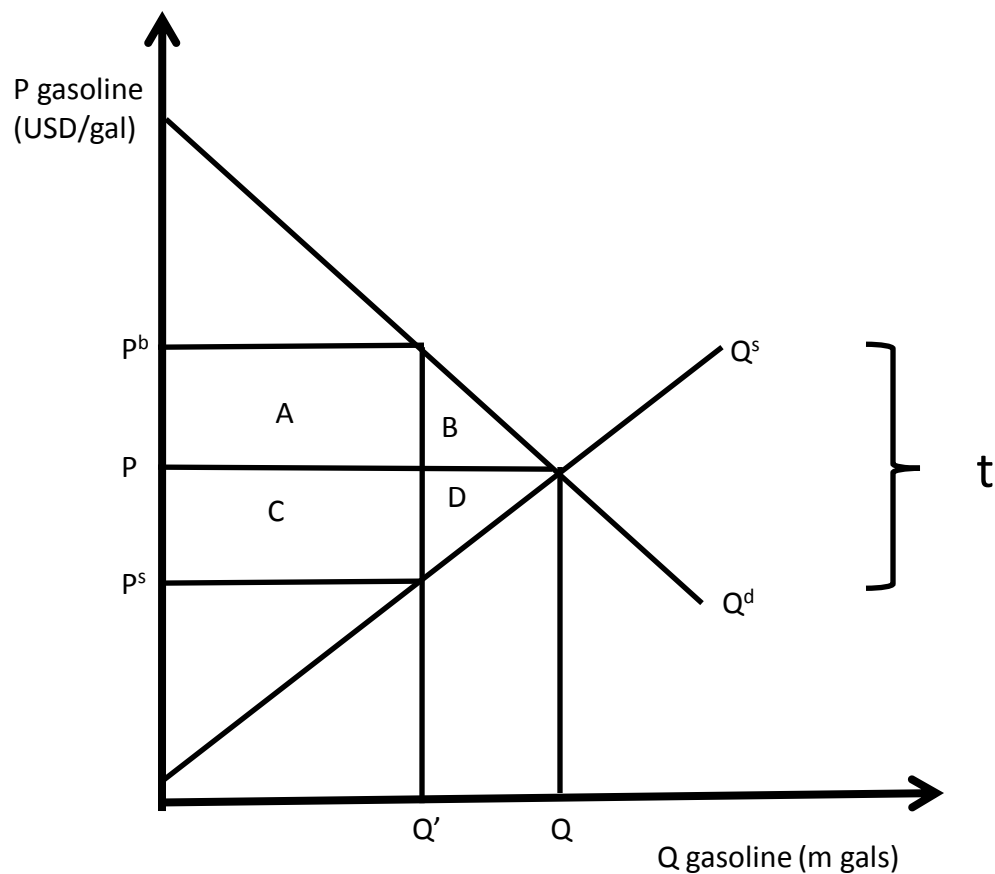


Figure 2.13 Tax on Gasoline

2.5.1 Welfare Analysis of a Tax

The welfare analysis of the tax compares the initial market equilibrium with the post-tax equilibrium.

$$\begin{aligned} \Delta CS &= -A - B, \\ \Delta PS &= -C - D, \\ \Delta G &= +A + C, \\ \Delta SW &= -B - D, \text{ and} \\ \text{DWL} &= B + D. \end{aligned}$$

In Figure 2.13, the incidence of the tax is equal between buyers and sellers of gasoline. This is because the supply and demand curves are drawn symmetrically. In the real world, the tax incidence will depend on the supply and demand elasticities. The pass

through fraction is the percentage of the tax “passed through” from producers to consumers.

$$\text{Pass Through Fraction} = E^s / (E^s - E^d)$$

We will calculate this for the gasoline market in the next section.

2.5.2 Quantitative Welfare Analysis of a Tax

Suppose that the inverse demand and supply of gasoline are given by:

$$P_b = 8 - Q^d, \text{ and}$$

$$P_s = 2 + Q^s,$$

Where P is the price of gasoline in USD/gal, and Q is the quantity of gasoline in million gallons. Market equilibrium is found where supply equals demand: $Q^e = 3$ million gallons of gasoline and $P^e = P_b = P_s = 5$ USD/gal of gasoline (Figure 2.14).

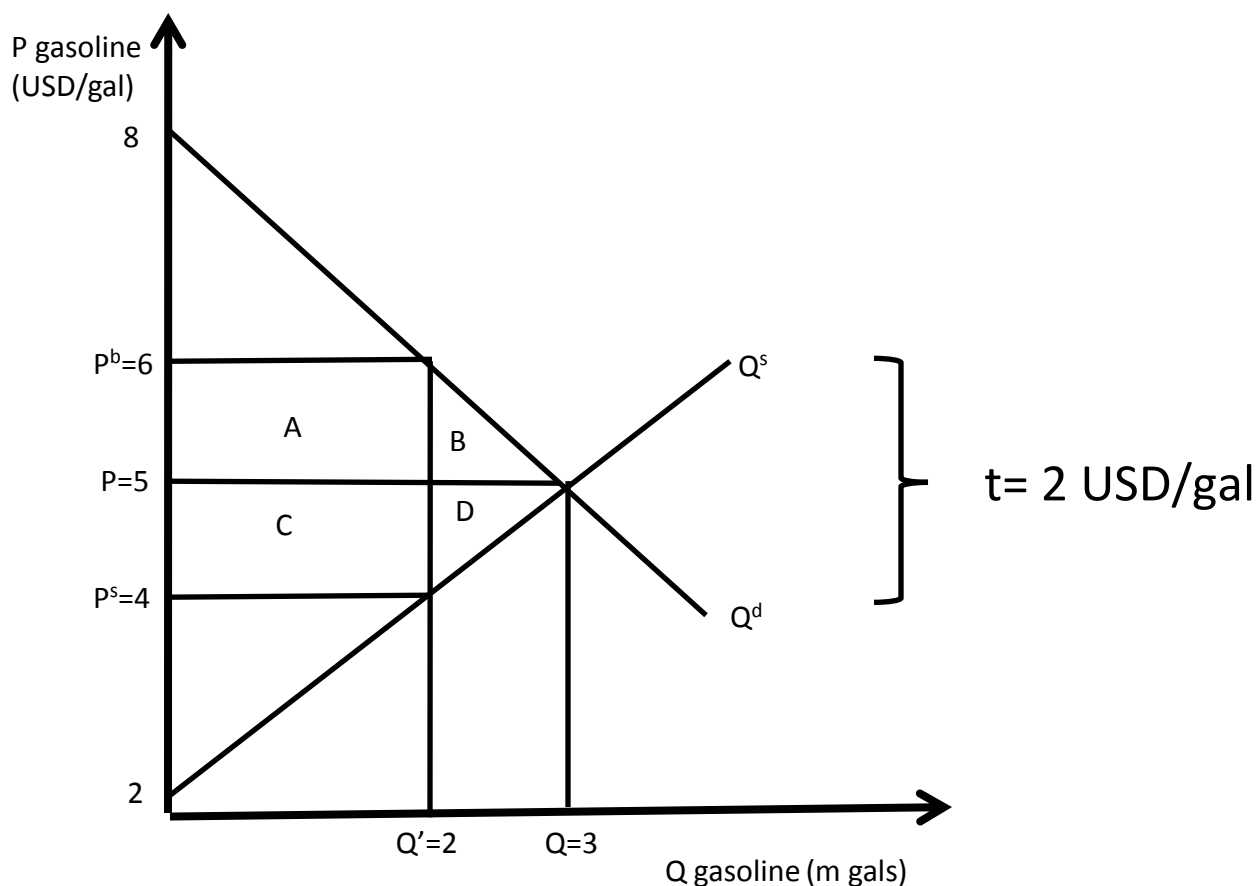


Figure 2.14 Tax on Gasoline

With the tax, the price relationship is given by:

$$P_b = P_s + t.$$

Assume that the government sets the tax equal to 2 USD/gal ($t = 2$). Substitution of the inverse supply and demand equations into the price equation yields:

$$8 - Q^d = 2 + Q^s + 2$$

Since $Q^d = Q^s = Q'$ after the tax:

$$4 = 2Q'$$

$Q' = 2$ million gallons of gasoline.

The quantity can be substituted into the inverse supply and demand equations to find the buyer's and seller's prices.

$P_b = 6$ USD/gal, and

$P_s = 4$ USD/gal.

These prices are shown in Figure 2.14. The welfare analysis is:

$$\Delta CS = -A - B = -2.5 \text{ USD million}$$

$$\Delta PS = -C - D = -2.5 \text{ USD million}$$

$$\Delta G = +A + C = +4 \text{ USD million}$$

$$\Delta SW = -B - D = -1 \text{ USD million}$$

$$DWL = B + D = +1 \text{ USD million}$$

Note that the change in social welfare equals the sum of the welfare changes due to the tax: $\Delta SW = \Delta CS + \Delta PS + \Delta G$.

The pass through fraction can now be calculated to find the tax incidence.

$$PTF = E_s / (E_s - E_d)$$

The elasticity of demand at the market equilibrium is equal to $-5/3$, and the supply elasticity is $+5/3$ [See Section 1.4.10 above if you need help remembering how to calculate elasticities!]. This yields:

$$PTF = E_s / (E_s - E_d) = (5/3) / (5/3 - -5/3) = (5/3) / (10/3) = 0.5.$$

This result shows that consumers pay for exactly one half of the tax, and producers pay for one half of the tax. The next section will discuss subsidies.

2.6 Subsidies

The policy objective of a subsidy is to help producers, or encourage the use of a good. The seller's price is higher than the buyer's price by the amount of the subsidy (s).

$$P_s = P_b + s$$

The subsidy is the vertical distance between the seller's price and the buyer's price, as shown in Figure 2.15.

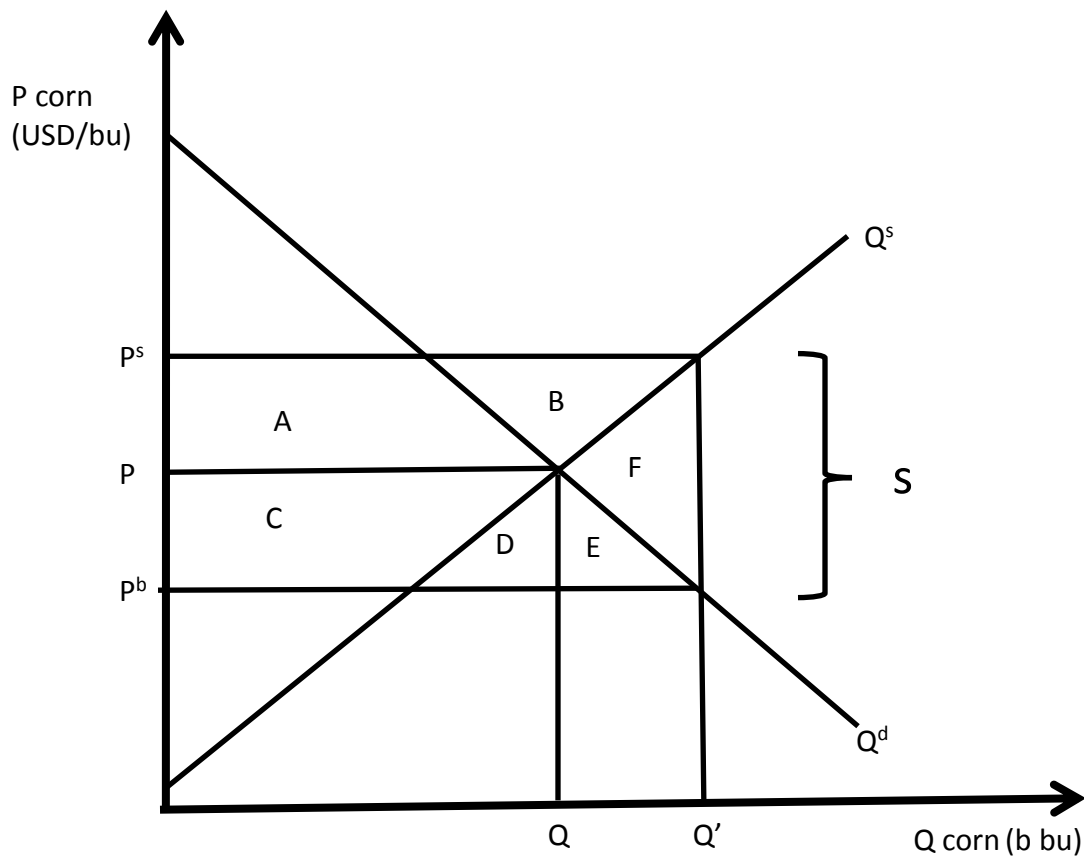


Figure 2.15 Corn Subsidy

2.6.1 Welfare Analysis of a Subsidy

The welfare analysis of the subsidy compares the initial market equilibrium with the post-subsidy equilibrium.

$$\Delta CS = +C + D + E,$$

$$\Delta PS = +A + B,$$

$$\Delta G = -A - B - C - D - E - F,$$

$$\Delta SW = -F, \text{ and}$$

$$DWL = F.$$

Both consumers and producers gain from the subsidy, but at a large cost to tax payers (the government).

2.6.2 Quantitative Welfare Analysis of a Subsidy

Suppose that the inverse demand and supply of corn are given by:

$$P_b = 12 - 2Q^d, \text{ and}$$

$$P_s = 2 + 2Q^s,$$

Where P is the price of corn in USD/bu, and Q is the quantity of corn in billion bushels. Market equilibrium is found where supply equals demand: $Q^e = 2.5$ billion bu of corn and $P^e = P_b = P_s = 7$ USD/bu of corn (Figure 2.16).

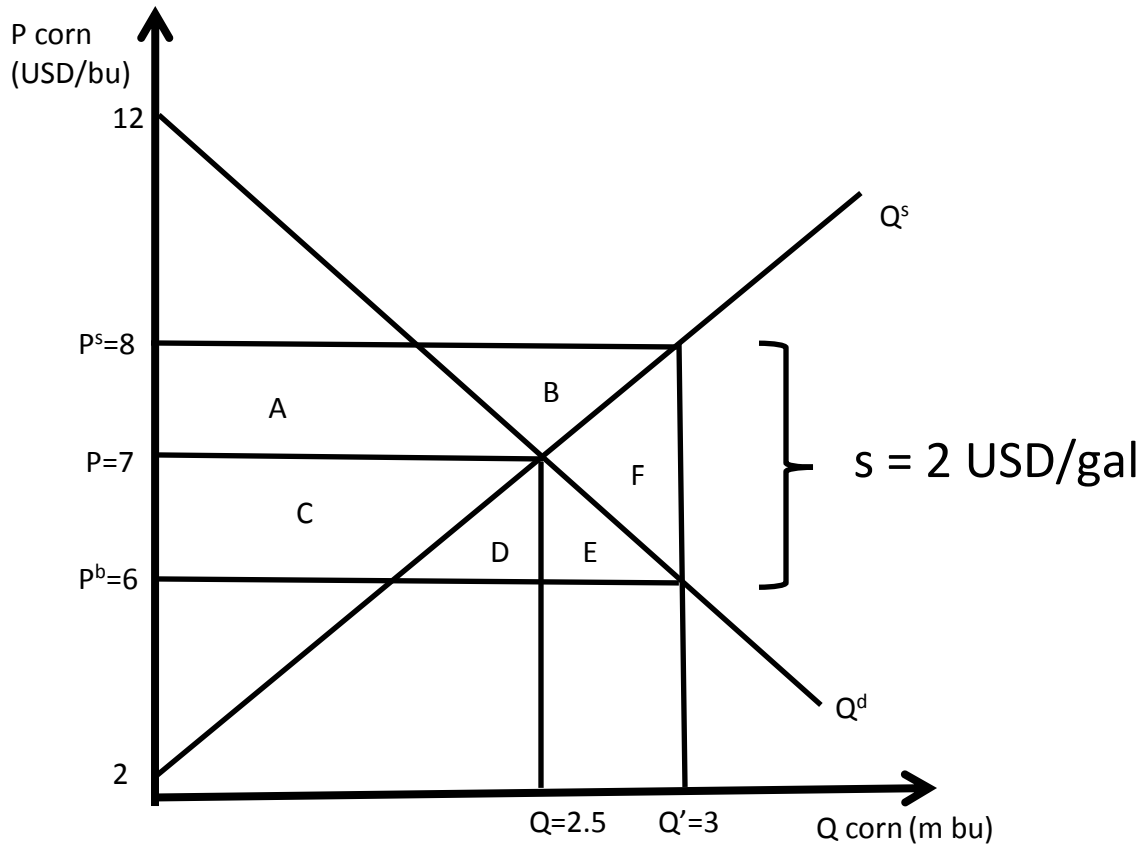


Figure 2.16 Corn Subsidy

With the subsidy, the price relationship is given by:

$$P_s = P_b + s.$$

Assume that the government sets the corn subsidy equal to 2 USD/bu. Substitution of the inverse supply and demand equations into the price equation yields:

$$2 + 2Q^s = 12 - 2Q^d + 2$$

Since $Q^d = Q^s = Q'$ after the tax:

$$4Q' = 12$$

$Q' = 3$ billion bushels of corn.

The quantity can be substituted into the inverse supply and demand equations to find the buyer's and seller's prices.

$P_b = 6$ USD/bu, and

$P_s = 8$ USD/bu.

These prices are shown in Figure 2.14. The welfare analysis is:

$$\Delta CS = + C + D + E = + 2.75 \text{ USD billion}$$

$$\Delta PS = + A + B = + 2.75 \text{ USD billion}$$

$$\Delta G = - A - B - C - D - E - F = - 6 \text{ USD billion}$$

$$\Delta SW = - F = - 0.5 \text{ USD billion}$$

$$DWL = F = + 0.5 \text{ USD billion}$$

Note again that the change in social welfare equals the sum of the welfare changes due to the tax: $\Delta SW = \Delta CS + \Delta PS + \Delta G$. Although the deadweight loss is not large, the government cost is large, making subsidies effective in helping producers and encouraging consumption of the good, but expensive for society.

Chapter 3. Monopoly and Market Power

3.1 Market Power Introduction

This chapter will explore firms that have market power, or the ability to set a price for their good.

Market Power = Ability of a firm to set a price for a good.

A monopoly is defined as a single firm in an industry with no close substitutes.

Monopoly = A single firm in an industry with no close substitutes.

The phrase, “no close substitutes” is important, since there are many firms that are the sole producer of a good. Consider McDonalds Big Mac hamburgers. McDonalds is the only provider of Big Macs, yet it is not a monopoly because there are many close substitutes available: Burger King Whoppers, for example.

Market power is also called monopoly power. A competitive firm is a “price taker,” so has no ability to change the price of a good. Each competitive firm is small relative to the market, so has no influence on price. Firms with market power are also called “price makers.”

Price Taker = A competitive firm with no ability to set the price of a good.

Price Maker = A noncompetitive firm with the ability to set the price of a good.

A monopolist is considered to be a price maker, and can set the price of the product that it sells. However, the monopolist is constrained by consumer willingness and ability to purchase the good, also called demand. For example, suppose that an agricultural chemical firm has a patent for an agricultural chemical used to kill weeds, a herbicide. The patent is a legal restriction that permits the patent holder to be the only seller of the herbicide, as it was invented by the company through their research program. In Figure 3.1, an agricultural chemical firm faces an inverse demand curve equal to: $P = 100 - Q^d$,

where P is the price of the agricultural chemical in dollars per ounce, and Q^d is the quantity demanded of the chemical in million ounces.

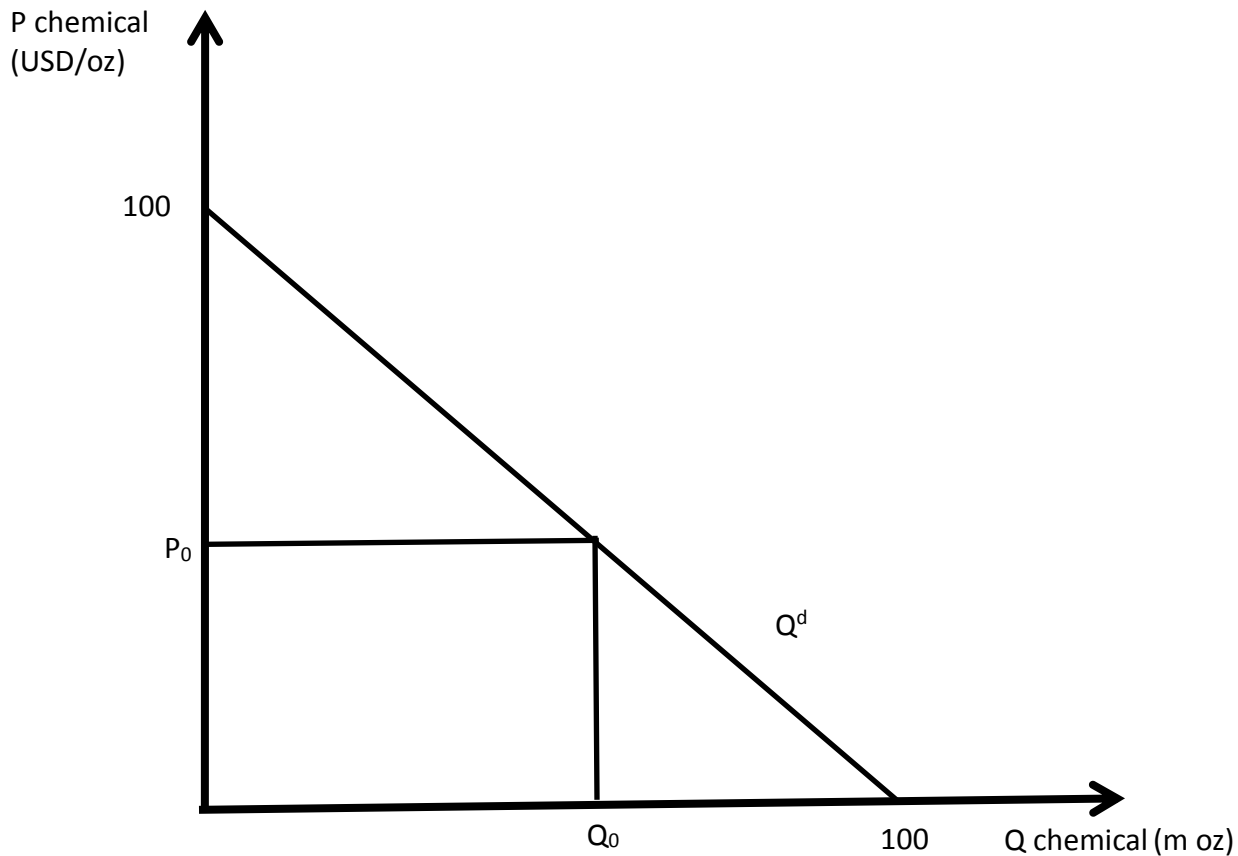


Figure 3.1 Demand facing a Monopolist: Agricultural Chemical

The monopolist can set a price, but the resulting quantity is determined by the consumers' willingness to pay, or the demand curve. If the price is set at P_0 , consumers will purchase Q_0 . The monopolist could set quantity at Q_0 , but consumers would be willing to pay P_0 for the chemical. Thus, a monopolist has the ability to set any price that it would like to, but with important consequences: the monopolist is constrained by consumer willingness to pay for the product.

3.2 Monopoly Profit-Maximizing Solution

The profit-maximizing solution for the monopolist is found by locating the biggest difference between total revenues and total costs, as in Equation 3.1.

$$(3.1) \max \pi = TR - TC$$

3.2.1 Monopoly Revenues

Revenues are the money that a firm receives from the sale of a product.

Total Revenue [TR] = The amount of money received when the producer sells the product. $TR = PQ$

Average Revenue [AR] = The average dollar amount receive per unit of output sold $AR = TR/Q$

Marginal Revenue [MR] = the addition to total revenue from selling one more unit of output. $MR = \Delta TR/\Delta Q = \partial TR/\partial Q$.

$$TR = PQ \quad (\text{USD})$$

$$AR = TR/Q = P \quad (\text{USD/unit})$$

$$MR = \Delta TR/\Delta Q = \partial TR/\partial Q \quad (\text{USD/unit})$$

For the agricultural chemical company:

$$TR = PQ = (100 - Q)Q = 100Q - Q^2$$

$$AR = P = 100 - Q$$

$$MR = \partial TR/\partial Q = 100 - 2Q$$

Total revenues for the monopolist are shown in Figure 3.2 Total Revenues are in inverted parabola. The maximum value can be found by taking the first derivative of TR, and setting it equal to zero. The first derivative of TR is the slope of the TR function, and when it is equal to zero, the slope is equal to zero.

$$(3.2) \max TR = PQ \quad \partial TR/\partial Q = 100 - 2Q = 0 \quad Q^* = 50$$

Substitution of Q^* back into the TR function yields $TR = \text{USD } 2500$, the maximum level of total revenues.

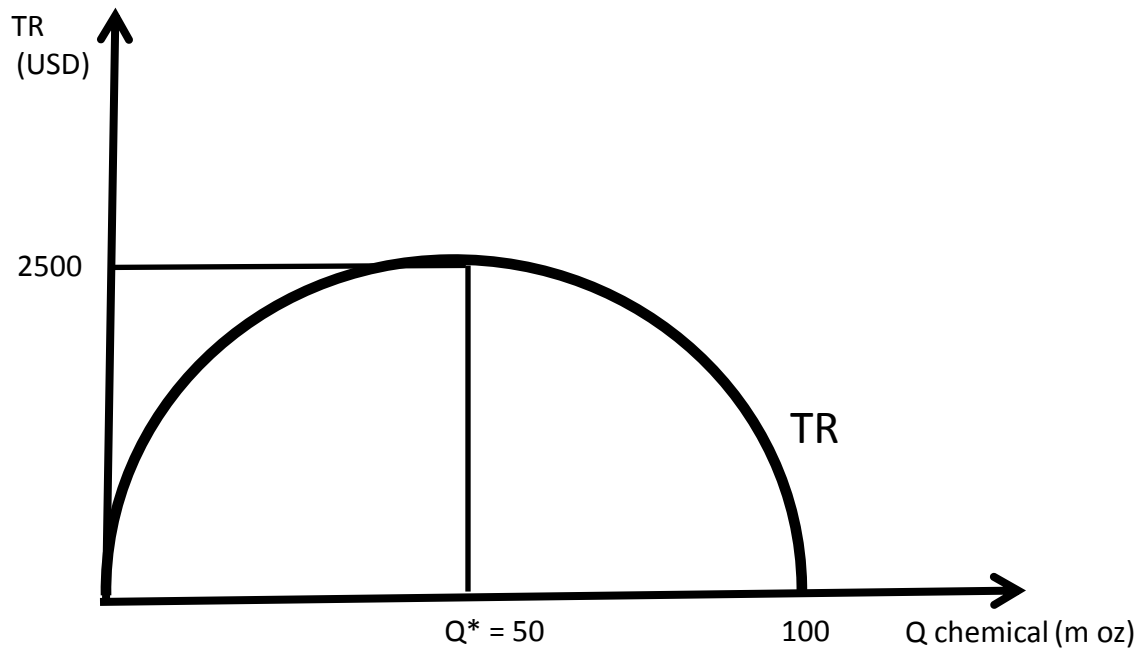


Figure 3.2 Total Revenues for a Monopolist: Agricultural Chemical

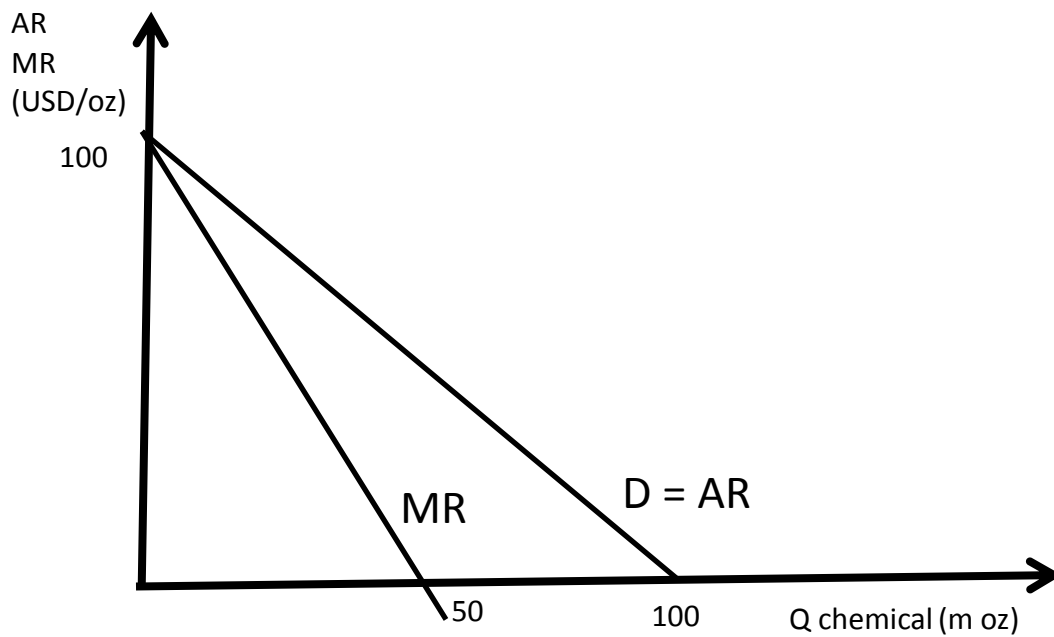


Figure 3.3 Per-Unit Revenues for a Monopolist: Agricultural Chemical

It is important to point out that the optimal level of chemical is not this level. The optimal level of chemical to produce and sell is the profit-maximizing level, which is revenues minus costs. If the monopolist were to maximize revenues, it might cost too much relative to the gain in revenue. Profits include both revenues and costs.

Average and marginal revenue are shown in Figure 3.3. The marginal revenue curve has the same y-intercept and twice the slope as the average revenue curve. This is always true for linear demand (average revenue) curves.

3.2.2 Monopoly Costs

The costs for the chemical include total, average, and marginal costs.

Total Costs [TC] = The sum of all payments that a firm must make to purchase the factors of production. The sum of Total Fixed Costs and Total Variable Costs. $TC = C(Q) = TFC + TVC$.

Average Costs [AC] = total costs per unit of output. $AC = TC/Q$. Note that the terms, Average Costs and Average Total Costs are interchangeable.

Marginal Costs [MC] = the increase in total costs due to the production of one more unit of output. $MC = \Delta TC/\Delta Q = \partial TC/\partial Q$.

$$TC = C(Q) \quad (\text{USD})$$

$$AC = TC/Q \quad (\text{USD/unit})$$

$$MC = \Delta TC/\Delta Q = \partial TC/\partial Q \quad (\text{USD/unit})$$

Suppose that the agricultural chemical firm is a constant cost industry. This means that the per-unit cost of producing one more ounce of chemical is the same, no matter what quantity is produced. Assume that the cost per unit is ten dollars per ounce.

$$TC = 10Q$$

$$AC = TC/Q = 10$$

$$MC = \Delta TC/\Delta Q = \partial TC/\partial Q = 10$$

The total costs are shown in Figure 3.4, and the per-unit costs are in Figure 3.5.

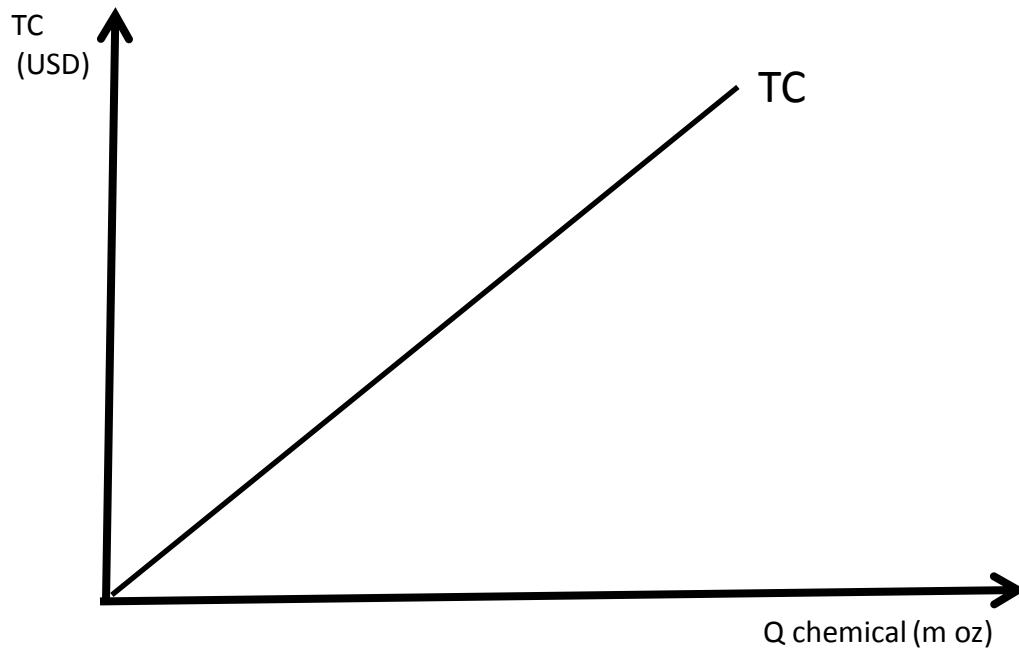


Figure 3.4 Total Costs for a Monopolist: Agricultural Chemical

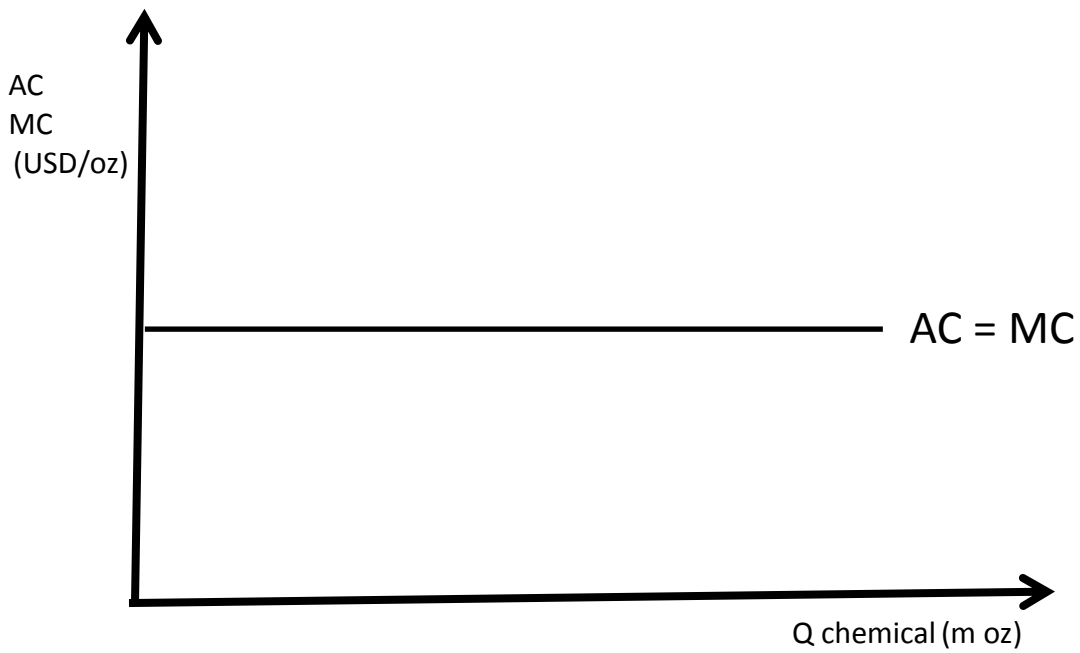


Figure 3.5 Per-Unit Costs for a Monopolist: Agricultural Chemical

3.2.3 Monopoly Profit-Maximizing Solution

There are three ways to communicate economics: verbal, graph, and math. The firm's profit maximizing solution is one of the major features of economics. The verbal explanation is that a firm should continue any activity as long as the additional (marginal) benefits are greater than the additional (marginal) costs. The firm should continue the activity until the marginal benefit is equal to the marginal cost. This is true for any activity, and for profit maximization, the firm will find the optimal, profit maximizing level of output where marginal revenues equal marginal costs.

The graphical solution takes advantage of pictures that tell the same story, as in Figures 3.6 and 3.7.

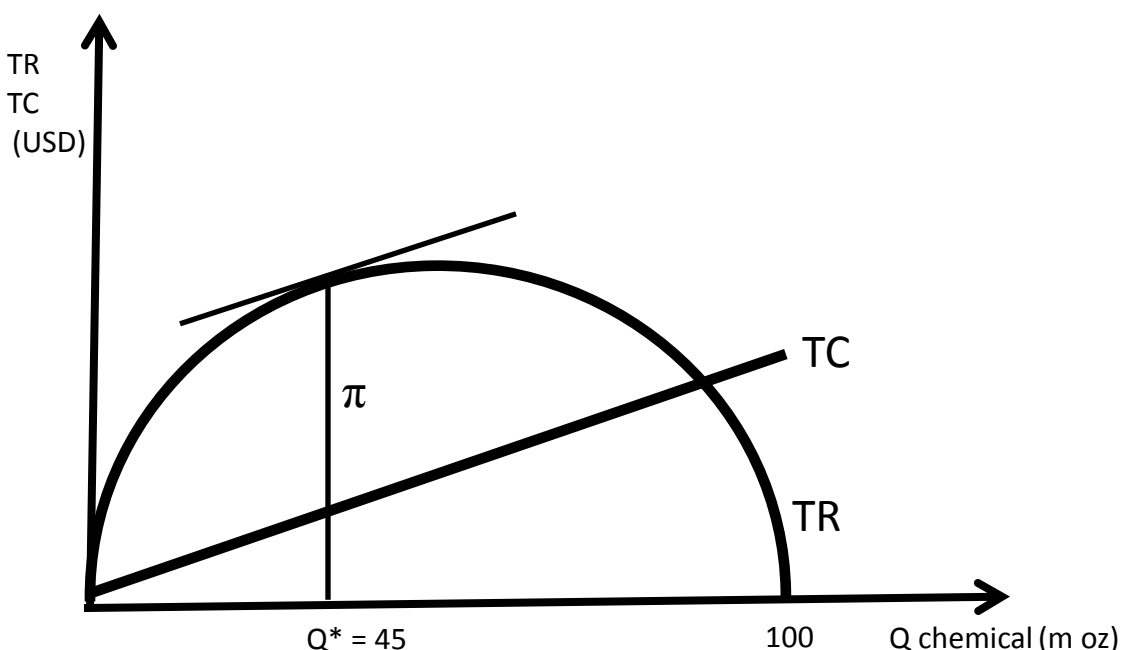


Figure 3.6 Total Profit Solution for a Monopolist: Agricultural Chemical

Figure 3.6 shows the profit maximizing solution using total revenues and total costs. The profit-maximizing level of output is found where the distance between TR and TC is largest: $\pi = TR - TC$. The solution is found by setting the slope of TR equal to the slope of TC: this is where the rates of change are equal to each other ($MR = MC$).

The same solution can be found using the marginal graph (Figure 3.7). The firm sets MR equal to MC to find the profit-maximizing level of output (Q^*), then substitutes Q^* into the consumers' willingness to pay (demand curve) to find the optimal price (P^*). The profit level is an area in Figure 3.7, defined by TR and TC. Total revenues are equal to price times quantity, so TR are equal to the rectangle from the origin to P^* and Q^* . Total

costs are equal to the rectangle defined by the per-unit cost of ten dollars per ounce times the quantity produced, Q^* . If the TC rectangle is subtracted from the TR rectangle, the shaded profit rectangle remains: profits are the residual of revenues after all costs have been paid.

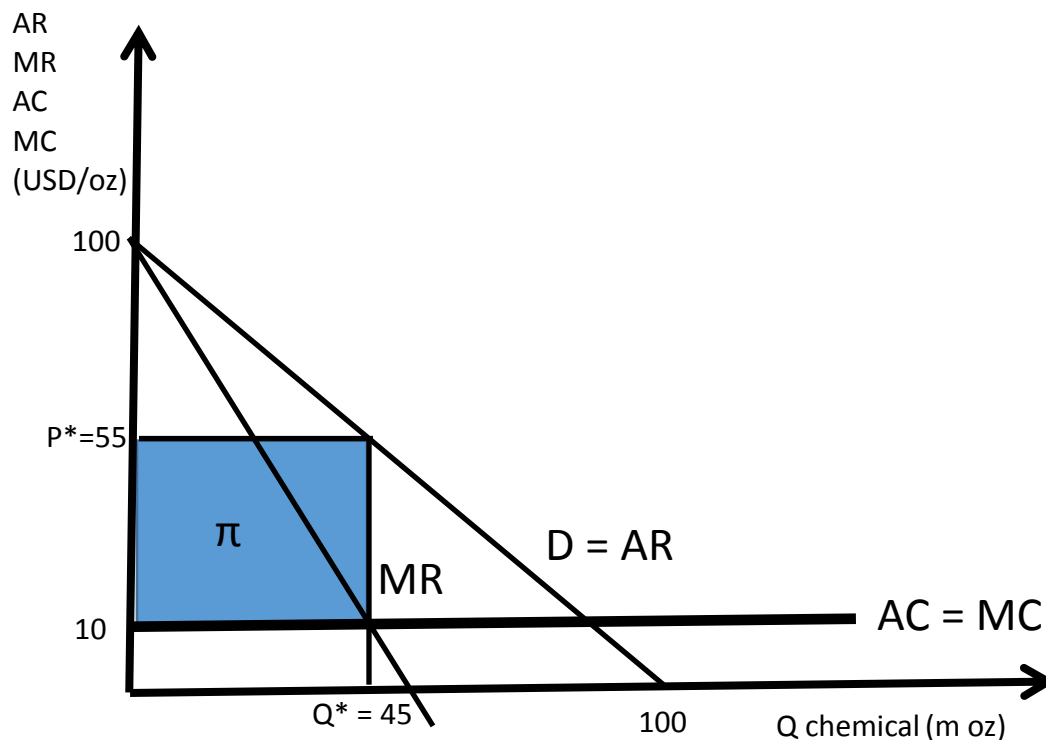


Figure 3.7 Marginal Profit Solution for a Monopolist: Agricultural Chemical

The math solution for profit maximization is found by using calculus. The maximum level of a function is found by taking the first derivative and setting it equal to zero. Recall that the inverse demand function facing the monopolist is $P = 100 - Qd$, and the per unit costs are ten dollars per ounce.

$$\begin{aligned}
 \max \pi &= TR - TC \\
 &= P(Q)Q - C(Q) \\
 &= (100 - Q)Q - 10Q \\
 &= 100Q - Q^2 - 10Q
 \end{aligned}$$

$$\begin{aligned}
 \partial\pi/\partial Q &= 100 - 2Q - 10 = 0 \\
 2Q &= 90 \\
 Q^* &= 45 \text{ million ounces of agricultural chemical}
 \end{aligned}$$

The profit-maximizing price is found by substituting Q^* into the inverse demand equation:

$$P^* = 100 - Q^* = 100 - 45 = 55 \text{ USD/ounce of agricultural chemical.}$$

The maximum profit level can be found by substitution of P^* and Q^* into the profit equation:

$$\pi = TR - TC = P(Q)Q - C(Q) = 55 \cdot 45 - 10 \cdot 45 = 45 \cdot 45 = 2025 \text{ million USD.}$$

This profit level is equal to the distance between the TR and TC curves at Q^* in Figure 3.6, and the profit rectangle identified in Figure 3.7. The profit-maximizing level of output and price have been found in three ways: verbal, graphical, and mathematical.

3.3 Marginal Revenue and the Elasticity of Demand

We have located the profit-maximizing level of output and price for a monopoly. How does the monopolist know that this is the correct level? How is the profit-maximizing level of output related to the price charged, and the price elasticity of demand? This section will answer these questions.

3.3.1 The Monopolist's Tradeoff between Price and Quantity

What happens to revenues when output is increased by one unit? The answer to this question reveals useful information about the nature of the pricing decision for firms with market power, or a downward sloping demand curve. Consider what happens when output is increased by one unit in Figure 3.8.

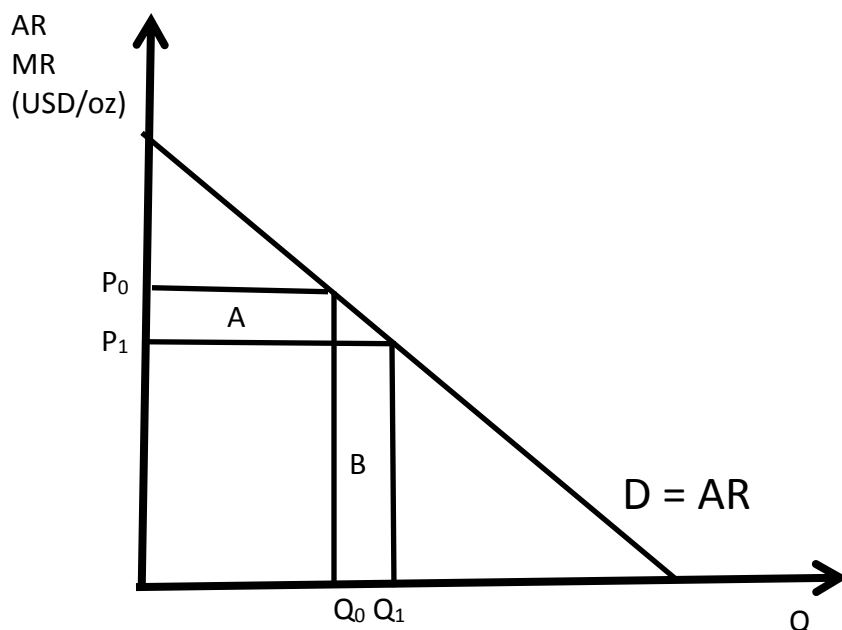


Figure 3.8 Per-Unit Revenues for a Monopolist: Agricultural Chemical

Increasing output by one unit from Q_0 to Q_1 has two effects on revenues: the monopolist gains area B, but loses area A. The monopolist can set price or quantity, but not both. If the output level is increased, consumers' willingness to pay decreases, as the good becomes more available. If quantity increases, price falls. The benefit of increasing output is equal to $\Delta Q \cdot P_1$, since the firm sells one additional unit at the price P_1 (area B).

The cost associated with increasing output by one unit is equal to ΔP^*Q_0 , since the price decreases for all units sold (area A). The monopoly cannot increase quantity without causing the price to fall for all units sold. If the benefits outweigh the costs, the monopolist should increase output: if $\Delta Q^*P_1 > \Delta P^*Q_0$, increase output.

3.3.2 The Relationship between MR and E^d

There is a useful relationship between marginal revenue (MR) and the price elasticity of demand (E^d). It is derived by taking the first derivative of the total revenue (TR) function. The product rule from calculus is used. The derivative of an equation with two functions is equal to the derivative of the first function times the second, plus the derivative of the second function times the first function, as in Equation 3.3.

$$(3.3) \partial(yz)/\partial x = (\partial y/\partial x)z + (\partial z/\partial x)y$$

The product rule is used to find the derivative of the TR function. Price is a function of quantity for a firm with market power. Recall that $MR = \partial TR/\partial Q$, and the equation for the elasticity of demand:

$$E^d = (\partial Q/\partial P)P/Q$$

This will be used in the derivation below.

$$TR = P(Q)Q$$

$$\partial TR/\partial Q = (\partial P/\partial Q)Q + (\partial Q/\partial Q)P$$

$$MR = (\partial P/\partial Q)Q + P$$

divide and multiply by P:

$$MR = [(\partial P/\partial Q)Q/P]P + P$$

$$MR = [1/E^d]P + P$$

$$MR = P(1 + 1/E^d)$$

This is a useful equation for a monopoly, as it links the price elasticity of demand with the price that maximizes profits. The relationship can be seen in Figure 3.9.

(3.4)

$$MR = P(1 + 1/E^d)$$

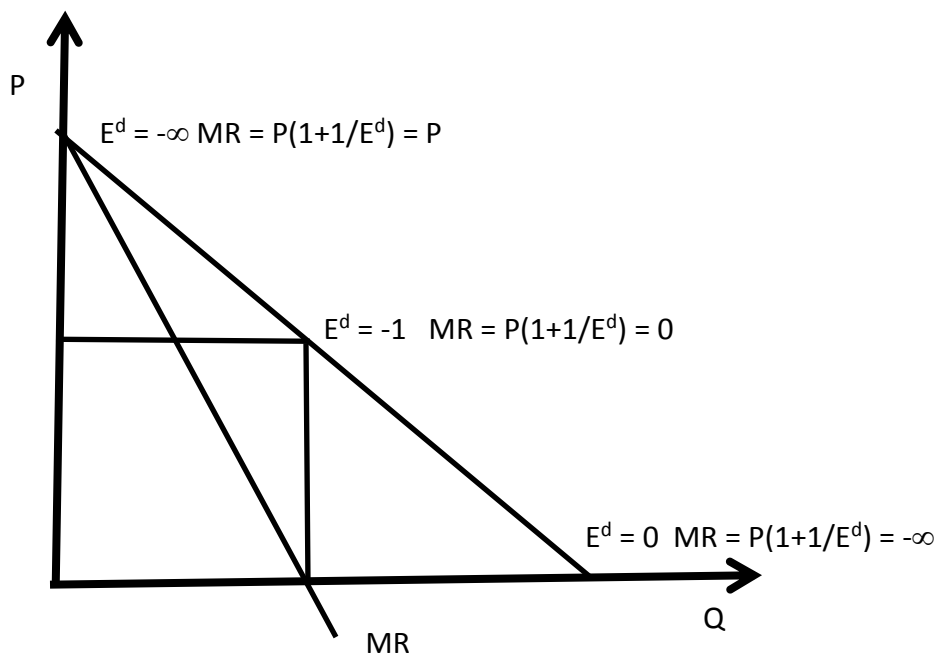


Figure 3.9 The Relationship between MR and E^d

At the vertical intercept, the elasticity of demand is equal to negative infinity (section 1.4.8). When this elasticity is substituted into the MR equation, the result is $MR = P$. The MR curve is equal to the demand curve at the vertical intercept. At the horizontal intercept, the price elasticity of demand is equal to zero, resulting in MR equal to negative infinity. If the MR curve were extended to the right, it would approach minus infinity as Q approached the horizontal intercept. At the midpoint of the demand curve, P is equal to Q , the price elasticity of demand is equal to -1, and $MR = 0$. The MR curve intersects the horizontal axis at the midpoint between the origin and the horizontal intercept.

This highlights the usefulness of knowing the elasticity of demand. The monopolist will want to be on the elastic portion of the demand curve, to the left of the midpoint, where marginal revenues are positive. The monopolist will avoid the inelastic portion of the demand curve by decreasing output until MR is positive.

3.3.3 Pricing Rule One

The useful relationship between MR and E^d in Equation 3.4 will be used to derive a pricing rule.

$$MR = P(1 + 1/E^d)$$

$$MR = P + P/E^d$$

Assume profit maximization [MR = MC]

$$MC = P + P/E^d$$

$$-P/E^d = P - MC$$

$$-1/E^d = (P - MC)/P$$

$$(P - MC)/P = -1/E^d$$

This pricing rule relates the price markup over the cost of production ($P - MC$) to the price elasticity of demand.

(3.5)

$$(P - MC)/P = -1/E^d$$

A competitive firm is a price taker. The price is fixed and given, no matter what quantity the firm sells. The demand curve facing a competitive firm is perfectly elastic: it is horizontal at the market equilibrium price, as in Figure 3.10. The price elasticity of demand for a competitive firm is equal to negative infinity: $E^d = -\infty$. When substituted into Equation 3.5, this yields $(P - MC)P = 0$, since dividing by infinity equals zero. This demonstrates that a competitive firm cannot increase price above the cost of production: $P = MC$. If a competitive firm increases price, it loses all customers: they have perfect substitutes available from numerous other firms.

Monopoly power, also called market power, is the ability to set price. Firms with market power face a downward sloping demand curve. Assume that a monopolist has a demand curve with the price elasticity of demand equal to negative two: $E^d = -2$. When this is substituted into Equation 3.5, the result is: $(P - MC)/P = 0.5$. Multiply both sides of this equation: $(P - MC) = 0.5P$, or $0.5P = MC$, which yields: $P = 2MC$. The markup for this firm is two times the cost of production. The size of the optimal, profit-maximizing markup is dictated by the elasticity of demand. Firms with responsive consumers, or elastic demands, will not want to charge a large markup. Firms with inelastic demands are able to charge a higher markup, as their consumers are less responsive to price changes.

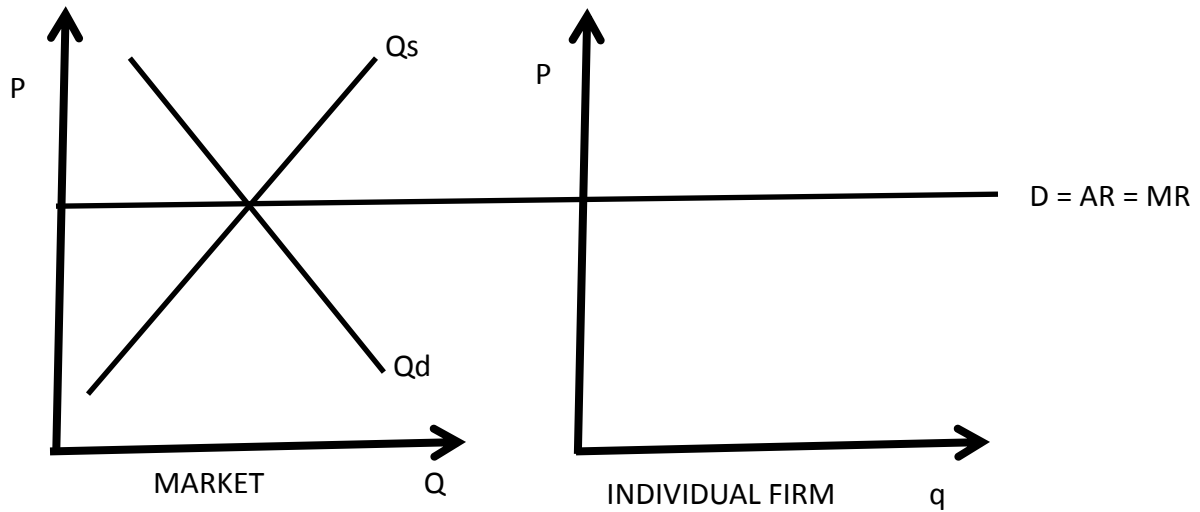


Figure 3.10 The Demand Curve of a Competitive Firm

In the next section, we will discuss several important features of a monopolist, including the absence of a supply curve, the effect of a tax on monopoly price, and a multiplant monopolist.

3.4 Monopoly Characteristics

3.4.1 The Absence of a Supply Curve for a Monopolist

There is no supply curve for a monopolist. This differs from a competitive industry, where there is a one-to-one correspondence between price (P) and quantity supplied (Q^s). For a monopoly, the price depends on the shape of the demand curve, as shown in figure 3.11. This graph shows that there is more than one price for each quantity. At quantity Q_0 , for demand curve D_1 , the monopolist maximizes profits by setting $MR_1 = MC$, which results in price P_1 . However, for demand curve D_2 , the monopolist would set $MR_2 = MC$, and charge a lower price, P_2 . Since there is more than one price associated with a single quantity (Q_0), there is no one-to-one correspondence between price and quantity supplied, and no supply curve for a monopolist.

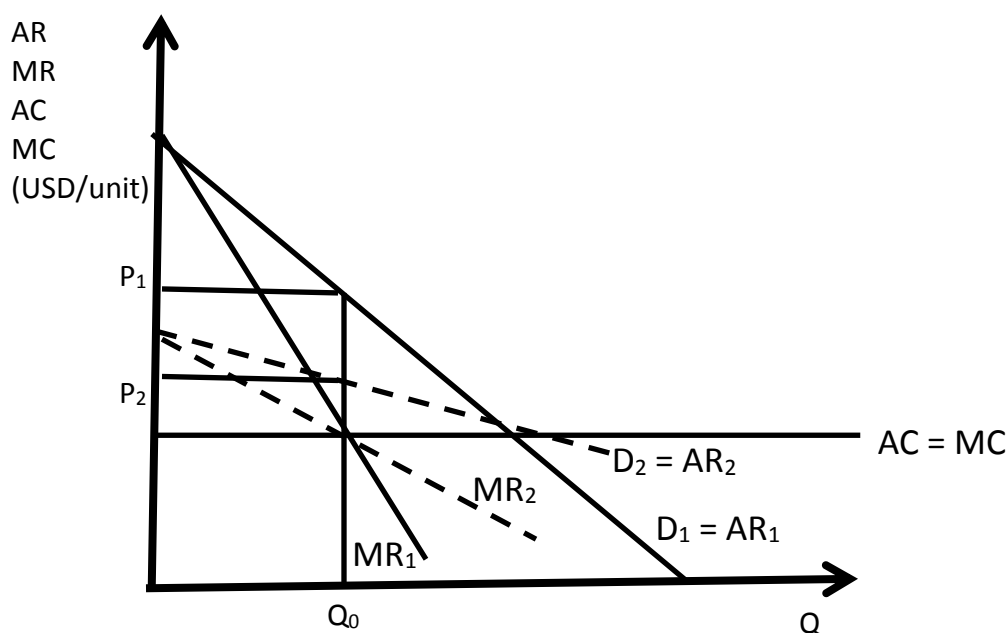


Figure 3.11 Absence of a Supply Curve for a Monopolist

3.4.2 The Effect of a Tax on a Monopolist's Price

In a competitive industry, a tax results in an increase in price that is a fraction of the tax, based on the incidence of the tax, which depends on the elasticities of supply and demand. In a monopoly, it is possible that the price increase from a tax is greater than the tax itself, as shown in Figure 3.12.

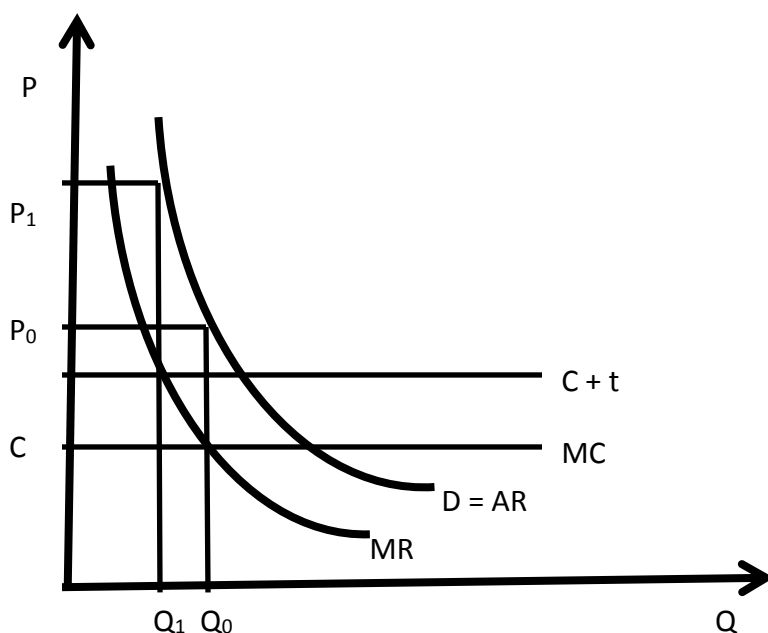


Figure 3.12 The Effect of a Tax on a Monopolist's Price

Before the tax, the monopolist sets $MR = MC$ at Q_0 , and sets price at P_0 . After the tax is imposed, the marginal costs increase to $C + t$. The monopolist sets $MR = MC = C + t$, and produces quantity Q_1 , and charges price P_1 . The increase in price ($P_1 - P_0$) is larger than the tax rate (t), the vertical distance between the $C + t$ and MC lines. In this case, consumers of the monopoly good are paying more than 100 percent of the tax rate. This is because of the shape of the demand curve: it is profitable for the monopoly to reduce quantity produced to increase the price.

3.4.3 Multiplant Monopolist

Suppose that a monopoly has two or more plants (factories). How does the monopolist determine how much output should be produced at each plant? Profit-maximization suggests two guidelines for the multiplant monopolist.

(1) Set MC equal across all plants: $MC_1 = MC_2 = \dots = MC_n$, and

(2) Set $MR = MC$ in all plants.

A mathematical model of a multiplant monopolist demonstrates profit-maximization for the monopolist. The result is interesting and important, as it shows that multiplant firms will not always close older, less efficient plants. This is true even if the older plants have higher production costs than newer, more efficient plants.

Suppose that a monopolist has two plants, and total output (Q_T) is the sum of output produced in plant 1 (Q_1) and plant 2 (Q_2).

$$(3.6) \quad Q_1 + Q_2 = Q_T$$

The profit-maximizing model for the two plant monopolist yields the solution. The costs of producing output in each plant differ. Assume that the old plant (plant 1) is less efficient than the new plant (plant 2): $C_1 > C_2$.

$$\max \pi = TR - TC$$

$$= P(Q_T)Q_T - C_1(Q_1) - C_2(Q_2)$$

$$\partial\pi/\partial Q_1 = \partial TR/\partial Q_1 - C_1'(Q_1) = 0$$

$$\partial\pi/\partial Q_2 = \partial TR/\partial Q_2 - C_2'(Q_2) = 0$$

The profit-maximizing solution is:

$$(3.7) \quad MR = MC_1 = MC_2$$

The multiplant monopolist solution is shown in Figure 3.13. The marginal cost curve for plant 1 is higher than the marginal cost curve for plant 2, reflecting the older, less efficient plant. Rather than shutting the less efficient plant down, the monopolist should produce some output in each plant, and set the MC of each plant equal to MR, as shown in the graph. The profit maximizing quantity (Q_T) is found by setting MR equal to MC_T . At the profit maximizing quantity (Q_T), the monopolist sets price equal to P, found by plugging Q_T into the consumers' willingness to pay, or the demand curve (D).

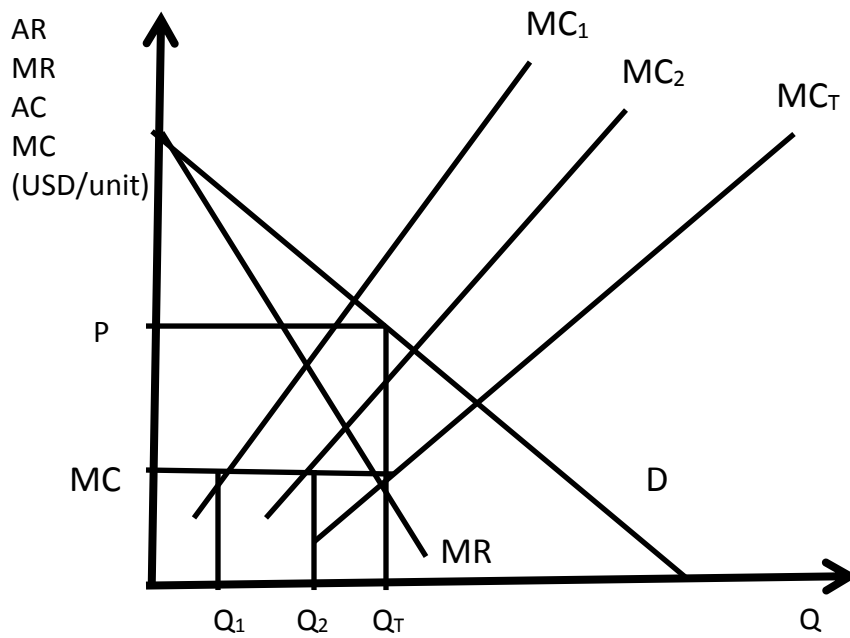


Figure 3.13 Multiplant Monopolist

To find the quantity to produce in each plant, the firm sets $MC_1 = MC_2 = MC_T$. The outcome of the multiplant monopolist yields useful conclusions for any firm: continue using any input, plant, or resource until marginal costs equal marginal revenues. Less efficient resources can be usefully employed, even if more efficient resources are available. The next section will explore the determinants and measurement of monopoly power, also called market power.

3.5 Monopoly Power

In this section, the determinants and measurement of monopoly power are examined.

3.5.1 The Lerner Index of Monopoly Power

Economists use the Lerner Index to measure monopoly power, also called market power. The index is the percent markup of price over marginal cost.

$$(3.8) L = (P - MC)/P$$

The Lerner Index is a positive number ($L \geq 0$), increasing in the amount of market power. A perfectly competitive firm has a Lerner Index equal to zero ($L = 0$), since price is equal to marginal cost ($P = MC$). A monopolist will have a Lerner Index greater than zero, and the index will be determined by the amount of market power that the firm has. A larger Lerner Index indicates more market power. In Section 3.3.3, a Pricing Rule was derived: $(P - MC)/P = -1/E^d$, where E^d is the price elasticity of demand. Substitution of this pricing rule into the definition of the Lerner Index provides the relationship between the percent markup and the price elasticity of demand.

$$(3.9) L = (P - MC)/P = -1/E^d$$

An example of a Lerner Index might be Big Macs. There are substitutes available for Big Macs, so if the price increases, consumers can buy a competing brand such as Whoppers. In this case, the price elasticity of demand is larger (more elastic), causing the percent markup to be smaller: the Lerner Index is relatively small. A monopoly is defined as a single seller in an industry with no close substitutes. Therefore, a monopoly will have a higher Lerner Index.

A second pricing rule can be derived from equation (3.9), if we assume that the firm maximized profits ($MR = MC$). In that case, the relationship between price and marginal revenue is equal to: $MR = P(1 + 1/E^d)$. If profit-maximization is assumed, then:

$$(3.10) \quad MC = P(1 + 1/E^d)$$

Rearranging:

$$(3.11) \quad P = MC/(1 + 1/E^d)$$

This is a useful equation, as it relates price to marginal cost. For example, a perfectly competitive firm has a perfectly elastic demand curve ($E^d = \text{negative infinity}$). Substitution of this elasticity into the pricing rule yields $P = MC$. For a monopoly that has a price elasticity equal to -2, $P = 2 MC$. The price is two times the production costs in this case. To summarize:

- (1) if E^d is large, the firm has less market power, and a small markup
- (2) if E^d is small, the firm has more market power, and a large markup.

A monopoly example is useful to review monopoly and the Lerner Index. Suppose that the inverse demand curve facing a monopoly is given by: $P = 500 - 10Q$. The monopoly production costs are given by: $C(Q) = 10Q^2 + 100Q$. Profit-maximization yields the optimal monopoly price and quantity.

$$\begin{aligned} \max \pi &= TR - TC \\ &= P(Q)Q - C(Q) \\ &= (500 - 10Q)Q - (10Q^2 + 100Q) \\ &= 500Q - 10Q^2 - 10Q^2 - 100Q \end{aligned}$$

$$\begin{aligned} \partial\pi/\partial Q &= 500 - 20Q - 20Q - 100 = 0 \\ 40Q &= 400 \\ Q^* &= 10 \text{ units} \\ P^* &= 500 - 10Q^* = 500 - 100 = 400 \text{ USD/unit.} \end{aligned}$$

To calculate the value of the Lerner Index, price and marginal cost are needed.

$$MC = C'(Q) = 20Q + 100.$$

$$MC^* = 20(10) + 100 = 300 \text{ units}$$

$$L = (P - MC)/P = (400 - 300)/400 = 100/400 = 0.25$$

This result can be checked with the pricing rule: $(P - MC)/P = -1/E^d$.

$$E^d = (\partial Q/\partial P)(P/Q)$$

For this monopoly, $\partial P/\partial Q = -10$. This is the first derivative of the inverse demand function. Therefore, $\partial Q/\partial P = -1/10$.

$$E^d = (\partial Q/\partial P)(P/Q) = (-1/10)(400/10) = -400/100 = -4.$$

$$L = (P - MC)/P = -1/E^d = -1/-4 = 0.25.$$

The same result was achieved using both methods, so the Lerner Index for this monopoly is equal to 0.25.

3.5.2 Welfare Effects of Monopoly

The welfare effects of a market or policy change are summarized as, “who is helped, who is hurt, and by how much.” To measure the welfare impact of monopoly, the monopoly outcome is compared with perfect competition. In competition, the price is equal to marginal cost ($P = MC$), as in Figure 3.14. The competitive price and quantity are P_c and Q_c . The monopoly price and quantity are found where marginal revenue equals marginal cost ($MR = MC$): P_M and Q_M . The graph indicates that the monopoly reduces output from the competitive level in order to increase the price ($P_M > P_c$ and $Q_M < Q_c$). The welfare analysis of a monopoly relative to competition is straightforward.

$$\Delta CS = - AB$$

$$\Delta PS = +A -C$$

$$\Delta SW = - BC$$

$$DWL = BC$$

Consumers are losers, and the benefits of monopoly depend on the magnitudes of areas A and C. Since a monopolist faces an inelastic supply curve (no close substitutes), area A is likely to be larger than area C, making the net benefits of monopoly positive.

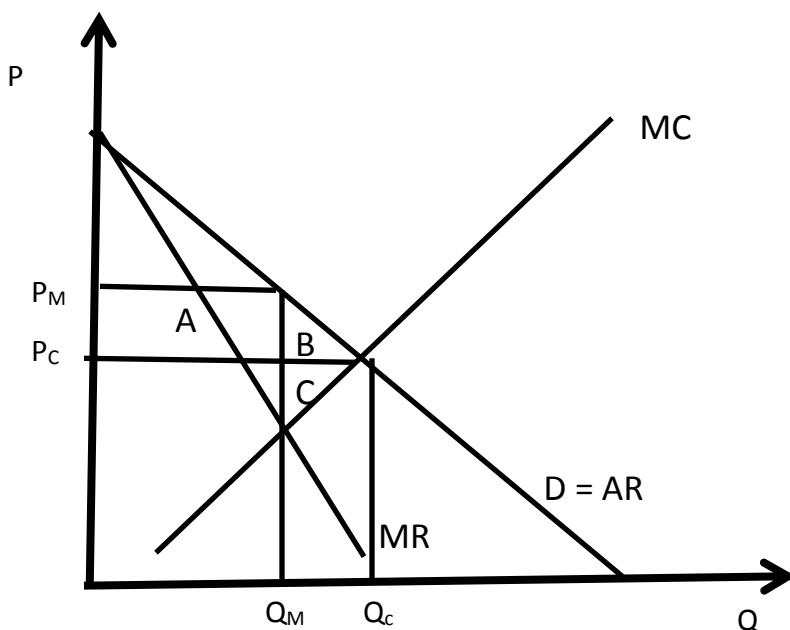


Figure 3.14 Welfare Effects of Monopoly

The monopoly example shows the magnitude of the welfare changes. From above, the inverse demand curve is given by $P = 500 - 10Q$, and the costs are given by $C(Q) = 10Q^2 + 100Q$. In this case, $P_M = 400$ USD/unit and $Q_M = 10$ units (see above). The competitive solution is found where the demand curve intersects the marginal cost curve.

$$500 - 10Q = 20Q + 100$$

$$30Q = 400$$

$$Q_c = 13.3 \text{ units}$$

$$P_c = 500 - 10(13.3) = 500 - 133 = 367 \text{ USD/unit}$$

$$\Delta CS = - AB = -(400 - 367)10 - (0.5)(400 - 367)(13.3 - 10) = -330 - 54.5 = -384.5 \text{ USD}$$

$$\Delta PS = +A - C = +330 - (0.5)(367 - 300)(13.3 - 10) = +330 - 110.5 = +219.5 \text{ USD}$$

$$\Delta SW = - BC = (0.5)(100)(3.3) = -165 \text{ USD}$$

$$DWL = BC = 165 \text{ USD}$$

The welfare analysis of monopoly has been used to justify breaking up monopolies into smaller, competing firms. In food and agriculture, many individuals and groups are opposed to large agribusiness firms. One concern is that these large firms have monopoly power, which results in a transfer of welfare from consumers to producers, and deadweight loss to society. It will be shown below that making monopolies illegal has both benefits and costs. There is some economic justification for large firms due to economies of scale and natural monopoly, as will be explored below. First, the sources of monopoly power will be listed and explained.

3.5.3 Sources of Monopoly

There are three major sources of monopoly power:

- (1) the price elasticity of demand (E^d),
- (2) the number of firms in a market, and
- (3) interaction among firms.

The price elasticity of demand is the most important determinant of market power, due to the pricing rule: $L = (P - MC)/P = -1/E^d$. When the price elasticity is large ($|E^d| > 1$), the demand is relatively elastic, and the firm has less market power. When the price elasticity is small ($|E^d| < 1$), the demand is relatively inelastic, and the firm has more market power.

The price elasticity of demand depends on how large the firm is relative to the market. The firm's price elasticity of demand is more elastic than the market demand:

$$|E^d_{\text{firm}}| < |E^d_{\text{market}}| .$$

If the price of the firm's output is increased, consumers can substitute into outputs produced by other firms. However, if all firms in the market increase the price of the good, consumers have no close substitutes, so must pay the higher price (Figure 3.15).

Therefore, the firm's price elasticity of demand is more elastic than the market demand. The firm's price elasticity of demand depends on how large the firm is relative to the other firms in the market.

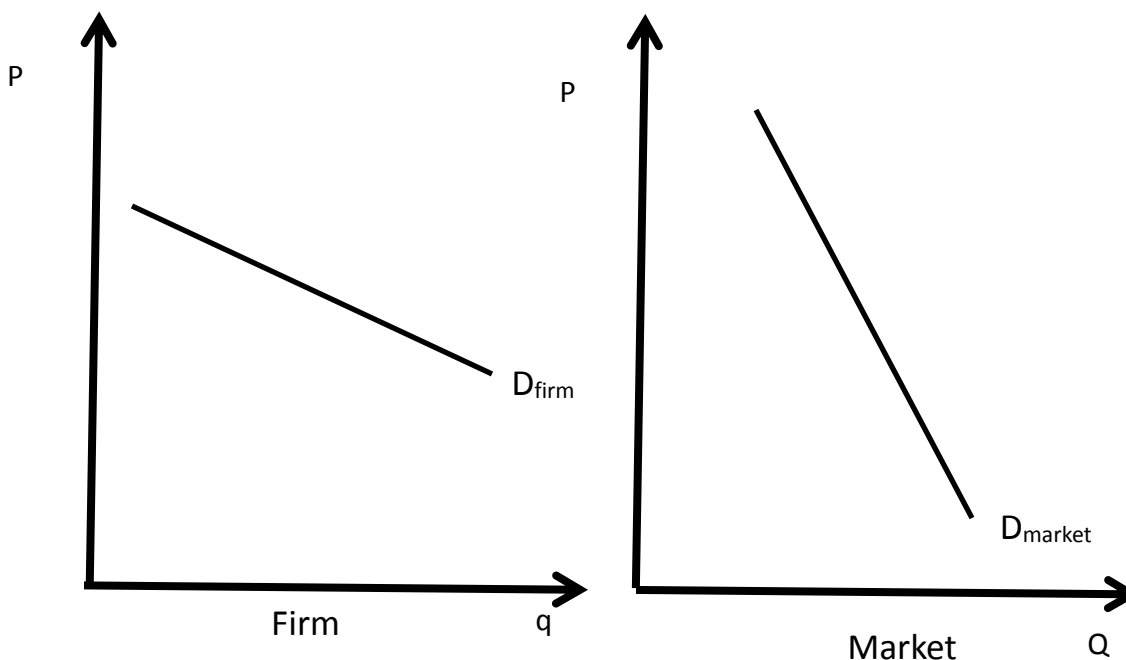


Figure 3.15 Price Elasticity of Demand for Firm and Industry

The second determinant of market power is the number of firms in an industry. This is related to Figure 3.15. If a firm is the only seller in an industry, then the firm is the same as the market, and the price elasticity of demand is the same for both the firm and the market. The more firms there are in a market, the more substitutes a consumer has, making the price elasticity of demand more elastic as the number of firms increases. In the extreme case, a perfectly competitive firm has numerous other firms in the industry, causing the demand curve to be perfectly elastic, $P = MC$, and $L = 0$. To summarize, the more firms there are in an industry, the less market power the firm has.

The number of firms in an industry is determined by the ease or difficulty of entry. This market feature is captured by the concept of, "Barriers to Entry." Barriers to entry include:

- (1) patents,
- (2) copyrights,

- (3) contracts,
- (4) economies to scale (natural monopoly),
- (5) excess capacity, and
- (6) licenses.

Each of these barriers to entry increases the difficulty of entering a market when positive economic profits exist. Economies to scale and natural monopoly are defined and described in the next section.

The number of firms is important, but the number of “major firms” is also important. Some industries are characterized by one or two dominant firms. These large firms often exert market power.

The third source of market power is interaction among firms. This will be extensively discussed in Chapter 5 Oligopoly. If firms compete aggressively with each other, less market power results. On the other hand, if firms cooperate and act together, the firms can have more market power. When firms join together, they are said to “collude,” or act as if they were a single firm. These strategic interactions form the heart of the discussion in Chapter 5.

3.5.4 Natural Monopoly

A natural monopoly is a firm characterized by large fixed costs. Recall that total costs are the sum of total variable costs and total fixed costs ($TC = TVC + TFC$). The fixed costs are those costs that do not vary with the level of output. When fixed costs are high, then average total costs are declining, as seen in Figure 3.16.

Another way of describing high fixed costs is the term, “economies of scale:”

Economies of Scale = When the per-unit costs of production decrease when output is increased.

Figure 3.16 shows the defining characteristic of a natural monopoly: declining average costs (AC). This means that the demand curve intersects the AC curve while it is declining. At some point, the average costs will increase, but for firms characterized by economies of scale, the relevant range of the AC curve is the declining portion, of the left side of a typical “U-shaped” cost function.

The reason for the name, “natural monopoly” can also be found in Figure 3.16. The demand curve has a portion above the AC curve, so positive profits are possible. Suppose that the monopoly was making positive economic profits, and attracted a competitor into the industry. The second firm would cause the demand facing each of the two firms to be cut in half. This possibility can be seen in Figure 3.16: if two firms served the customers, each firm would have a demand curve equal to the MR curve. This is because for a linear demand curve, the MR curve has the same y-intercept and twice the slope. Notice the position of the MR curve for a natural monopoly: it lies everywhere below the AC curve. Therefore, positive profits are not possible for two firms serving this market. The demand is not large enough to cover the fixed costs.

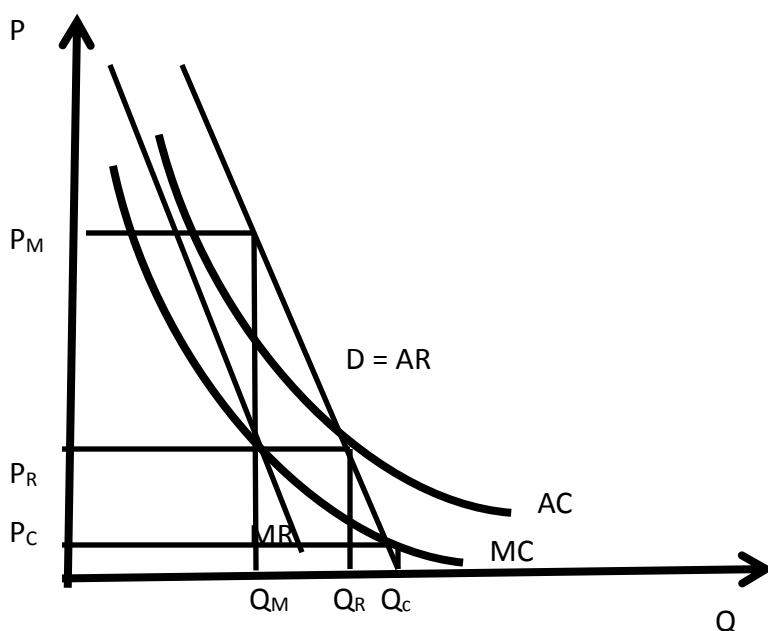


Figure 3.16 Natural Monopoly

The fixed costs are typically large investments that must be made before the good can be sold. For example, an electricity company must build both a huge generating plant and a distribution network that connects all residences and businesses to the power grid. These enormous costs do not vary with the level of output: they must be paid whether the firm sells zero kilowatt hours or one million kilowatt hours. The average fixed costs decline as they are spread out over larger quantities ($AFC = TFC/Q$). As the

output increases, average costs decline. This feature is true for many large businesses, and provides economic justification for large firms: the per-unit costs of production are smaller, providing lower costs to consumers. There is a tradeoff for consumers who purchase goods from large firms: the cost is lower due to economies of scale, but the firm may have market power, which can result in higher prices. This tradeoff makes the economic analysis of large firms both fascinating and important to society.

Natural monopolies have important implications for how large businesses provide goods to consumers, as is explicitly shown in Figure 3.16. The industry in Figure 3.16 is a natural monopoly, since demand intersects average costs while they are declining. If a single firm was in the depicted industry, it would set marginal costs equal to marginal revenues ($MR = MC$), and produce and sell Q_M units of output at a price equal to P_M . The price is high: consumers lose welfare and society is faced with deadweight losses.

If competition were possible, price would be set at marginal cost ($P = MC$). The resulting price and quantity under competition would be P_C and Q_C (Figure 3.16). This is a desirable outcome for the consumers. However, there is a major problem with this outcome: price is below average costs, and any business firm that charged the competitive price P_C would be forced out of business. The natural monopoly is considered a “market failure” since there is no good market-based solution. A single monopoly firm could earn enough revenue to stay in business, but consumers would pay a high monopoly price. If competition occurred, the consumers would pay the cost of production, but the firms would not cover their costs.

One solution to a natural monopoly is government regulation. If the government intervened, it could set the regulated price equal to average costs ($P_R = AC$), and the regulated quantity equal to Q_R . This solves the problem of natural monopoly with a compromise: consumers pay a price just high enough to cover the firm’s average costs. This analysis explains why the government regulates many public utilities for electricity, natural gas, water, sewer, and garbage collection.

The next section will investigate monopsony, or a single buyer with market power.

3.6 Monopsony

A monopsony is defined as a market characterized by a single buyer.

Monopsony = single buyer of a good.

Monopsony power is market power of buyers. A firm with monopsony power is a buyer that is large enough relative to the market to influence the price of a good. Competitive firms are price takers: prices are fixed and given, no matter how little or how much they buy. In food and agriculture, beef packers are often accused of having market power, and pay lower prices for cattle than the competitive price. This section will explore the causes and consequences of monopsony power.

3.6.1 Terminology of Monopsony

Consider any decision from an economic point of view. Thinking like an economist results in comparing the benefits and costs of any decision. This section will apply economic thinking to the quantity and price of a purchase. It will follow the same economic approach that has been emphasized, but will define new terminology to distinguish the buyer's decision from the seller's decision. It is useful to recall the meaning of supply and demand curves. The demand curve represents the consumers' willingness and ability to pay for a good. The demand curve is downward sloping, reflecting scarcity: larger quantities are less scarce, and thus less valuable. The supply curve represents the producers' cost of production, and is upward sloping. As more of a good is produced, the marginal costs of production increase, since it requires more resources to produce larger quantities. These economic principles will be useful in what follows, an analysis of a buyer's decision to purchase a good.

The economic approach to the purchase of a good is to employ marginal decision making by continuing to purchase a good as long as the marginal benefits outweigh the marginal costs. The following terms are defined to aid in our analysis of buyer's market power.

Marginal Value (MV) = The additional benefits of buying one more unit of a good.

Marginal Expenditure (ME) = The additional costs of buying one more unit of a good.

Average Expenditure (AE) = The price paid per unit of a good.

A review of competitive buyers and sellers is a good starting point for our analysis.

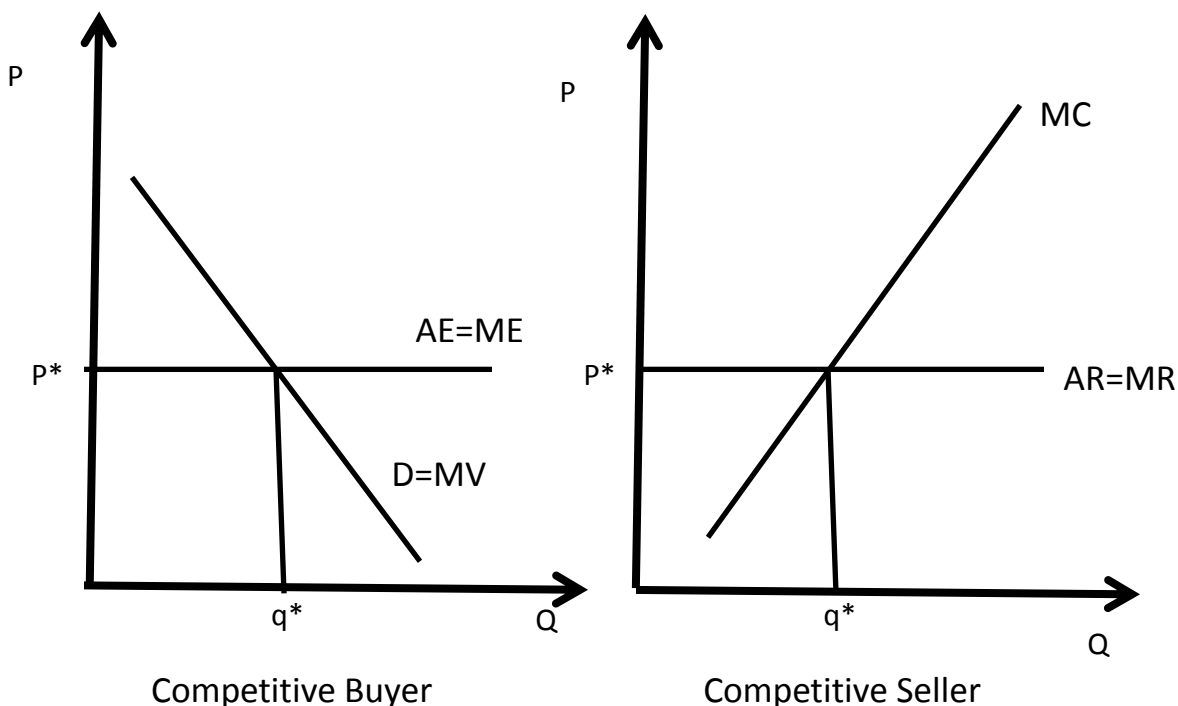


Figure 3.17 Competitive Buyer and Seller

Figure 3.17 demonstrates the competitive solution for a competitive buyer and a competitive seller. The competitive buyer faces a price that is fixed and given (P^*). The price is constant because the buyer is so small relative to the market that her purchases do not affect the price. Average expenditures (AE) and marginal expenditures (ME) for this buyer are constant and equal ($AE = ME$). The buyer will continue purchasing the good until the marginal benefits, defined to be the marginal value (MV) are equal to marginal expenditures (ME) at q^* , the optimal, profit-maximizing level of good to purchase.

A competitive seller takes the price as fixed and given (P^*). The price is constant because the seller is so small relative to the market that his sales do not affect the price. Average revenues (AR) and marginal revenues (MR) for this seller are constant and equal ($AR = MR$). The seller will continue producing the good until the marginal

benefits, defined to be the marginal revenues (MR) are equal to marginal cost (MC) at q^* , the optimal, profit-maximizing level of good to produce.

A monopsony uses the same decision making framework, comparing marginal benefits and marginal costs. The distinction is that a monopsony is large enough relative to the market to influence the price. Thus, the monopsony faces an upward-sloping supply curve: as the monopsony purchases more of the good, it drives the price up (Figure 3.18).

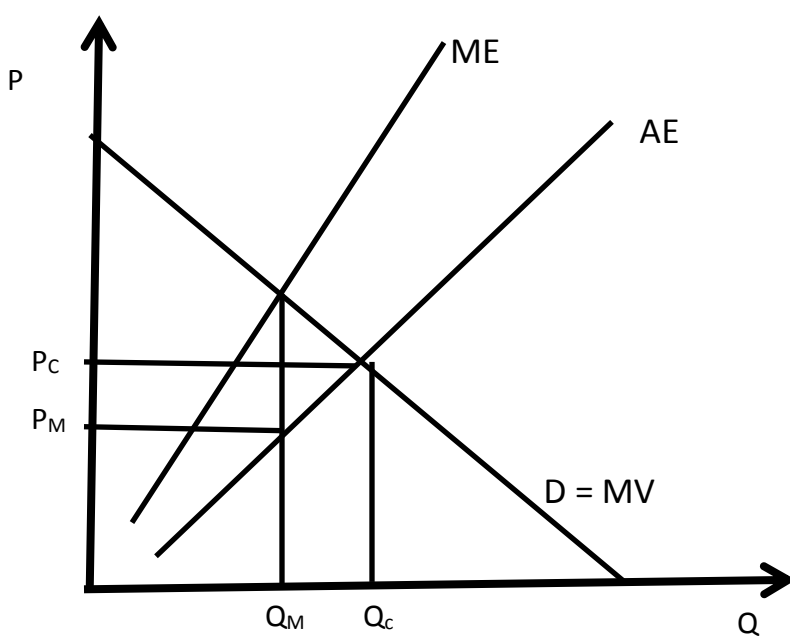


Figure 3.18 Monopsony

Since the firm is large, when it purchases more of a good, it drives the price higher. The average expenditure (AE) curve is the supply curve of the good faced by a monopsony. An example might be Ford Motor Company. When Ford purchases more steel (or glass or tires), the firm is so large relative to the market for steel that it drives the price up. Steel companies will need to buy more resources to produce more steel, and it will cost them more, since Ford is so large a buyer in the steel market.

The profit-maximizing solution is found by setting $MV = ME$, and purchasing the corresponding quantity Q_M . Note that the monopsony is restricting quantity, as a monopoly restricts output to drive the price up. However, a monopsony restricts

quantity in order to drive the price down to P_M . The monopsony is buying less than the competitive output (Q_C) and paying a price lower than the competitive price (P_C).

It is worth answering the question, “why is $ME > AE$?” The monopsony faces an upward-sloping supply curve (AE). This reflects the higher cost of bringing more resources into the production of the good purchased by the monopsony. This can be seen in Figure 3.19. Next, the relationship between AE and ME is derived. This derivation will be familiar, as it is the same as the relationship between AR and MR from section 3.3.2 above.

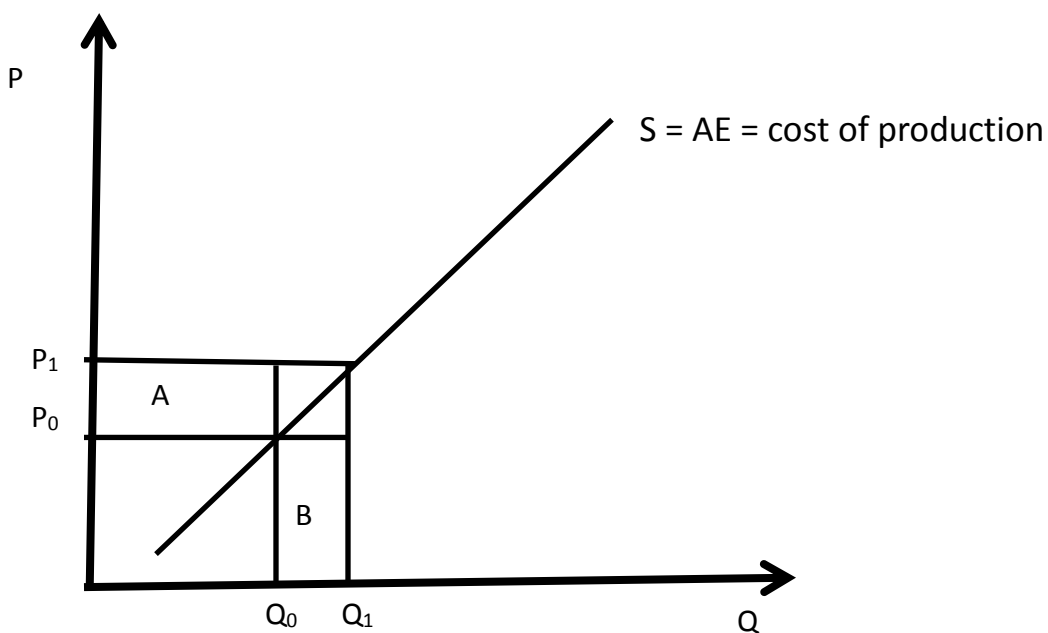


Figure 3.19 Monopsony Supply Curve

$$AE = P(Q)$$

$$TE = P(Q)Q$$

$$ME = \partial TE / \partial Q = (\partial P / \partial Q)Q + P$$

$$ME = AE + (\partial P / \partial Q)Q$$

The first term in the expression for ME is AE , which corresponds to area B in Figure 3.19. Average expenditure is equal to P_0 at quantity Q_0 . The second term, $(\partial P / \partial Q)Q$, is equal to area A in the diagram. This area represents the change in price given a small change in quantity ($\partial P / \partial Q$), multiplied by the quantity (Q). For a competitive firm, $(\partial P / \partial Q) = 0$, since the competitive firm is a price taker. For a competitive firm, $AE = ME$, as shown in the left of Figure 3.17. For a monopsony, the firm pays the initial price plus

the increase in price caused by an increase in output. The monopsony must pay this new price (P_1 in Figure 3.19) for all units purchased (Q). This causes ME to be above AE .

It is instructive to view the monopoly graph next to the monopsony graph (Figure 3.20).

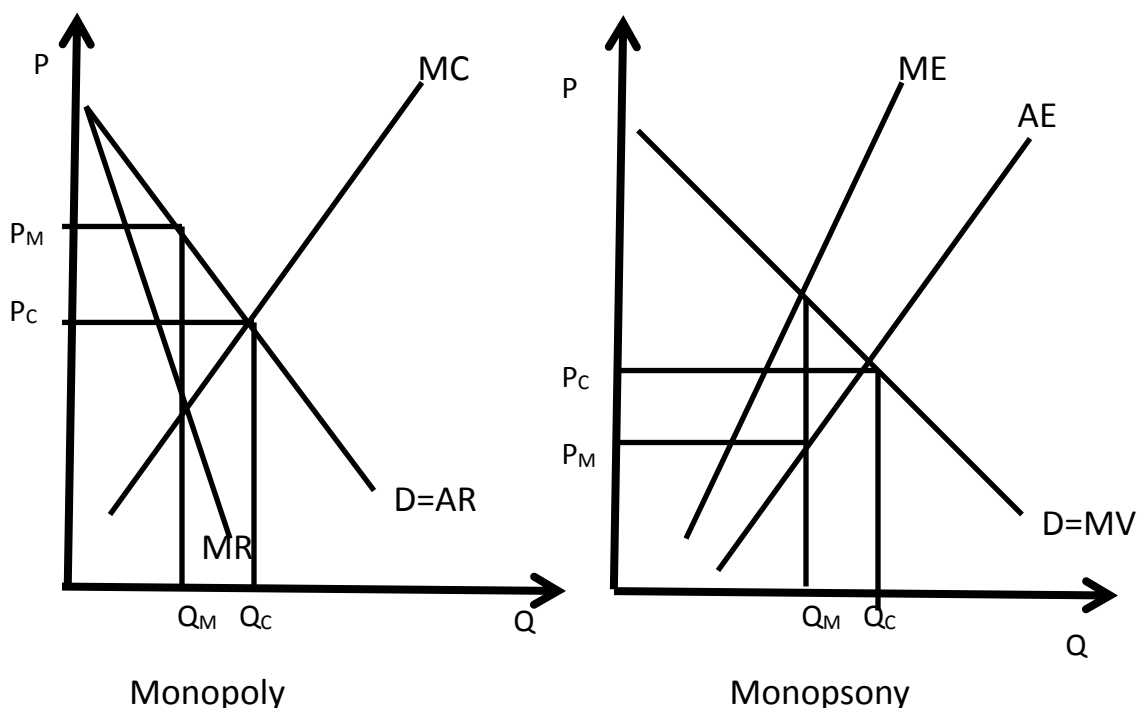


Figure 3.20 Monopoly and Monopsony

The monopoly restricts output to drive up the price. The monopoly output is less than the competitive output ($Q_M < Q_C$), and the monopoly price is higher than the competitive price ($P_M > P_C$). The monopsony restricts output to drive down the price ($P_M < P_C$). Both firms are maximizing profit by using the market characteristics that they face.

3.6.2 Welfare Effects of Monopsony

To measure the welfare impact of monopsony, the monopsony outcome is compared with perfect competition. In competition, the price is equal to marginal cost ($P = MC$), as in Figure 3.21. The competitive price and quantity are P_c and Q_c . The monopsony price and quantity are found where marginal value (MV) equals marginal expenditure ($MV = ME$): P_M and Q_M . The graph indicates that the monopsony reduces output from the competitive level in order to decrease the price ($P_M < P_c$ and $Q_M < Q_c$). The welfare analysis of a monopsony relative to competition is straightforward.

$$\Delta CS = +A - B$$

$$\Delta PS = -AC$$

$$\Delta SW = -BC$$

$$DWL = BC$$

Consumers are winners, and the benefits of monopsony depend on the magnitudes of areas A and B.

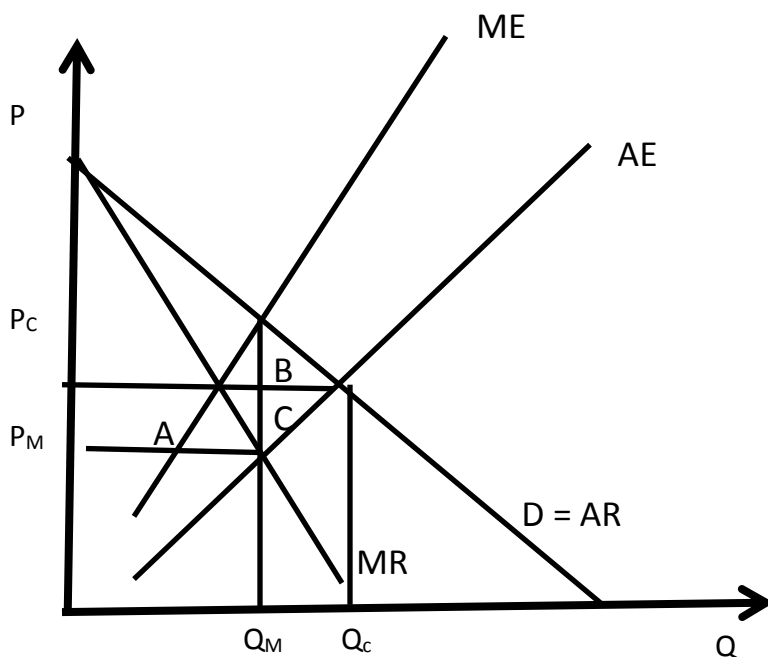


Figure 3.21 Welfare Effects of Monopsony

3.6.3 Sources of Monopsony Power

There are three major sources of monopsony power, analogous to the three determinants of monopoly power:

- (1) the price elasticity of market supply (E^s),
- (2) the number of buyers in a market, and
- (3) interaction among buyers.

The price elasticity of supply is the most important determinant of monopsony power, and the monopsony benefits from an inelastic supply curve. When the price elasticity is large ($E^s > 1$), the supply is relatively elastic, and the firm has less market power. When the price elasticity is small ($E^s < 1$), the demand is relatively inelastic, and the firm has more market power.

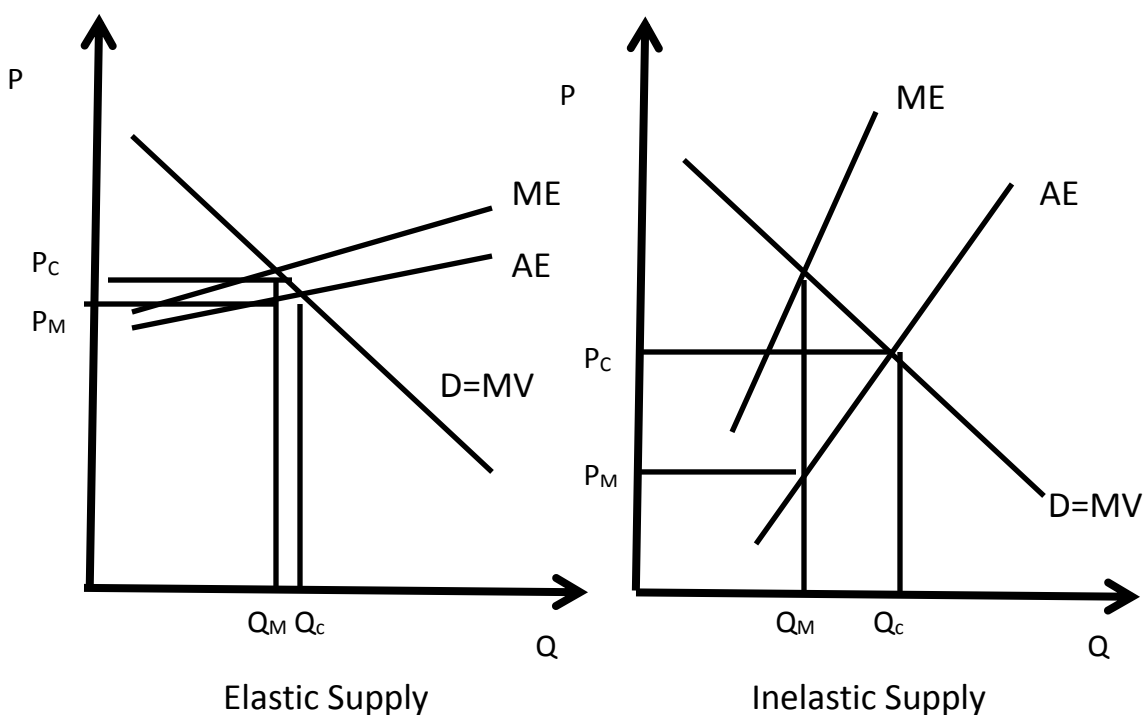


Figure 3.22 Price Elasticity of Supply Impact on Monopsony

The second determinant of monopsony power is the number of firms in an industry. If a firm is the only buyer in an industry, the firm is a monopsony, and has market power.

The more firms there are in a market, the more competition the firm faces, and the less market power.

The third source of monopsony power is interaction among firms. If firms compete aggressively with each other, less monopsony power results. On the other hand, if firms cooperate and act together, the firms can have more monopsony power.

Chapter 4. Pricing with Market Power

4.1 Introduction to Pricing with Market Power

In economics, the firm's objective is assumed to be to maximize profits. Firms with market power do this by capturing consumer surplus, and converting it to producer surplus. In Figure 4.1, a monopoly finds the profit-maximizing price and quantity by setting MR equal to MC. This strategy maximizes profits for a firm setting a single price and charging all customers the same price. In some situations, it is possible for a monopolist to increase profits beyond the monopoly solution. Figure 4.1 shows that there are two sources of consumer willingness to pay that the monopoly has not taken advantage of by producing a quantity of Q_M and selling it at price P_M .

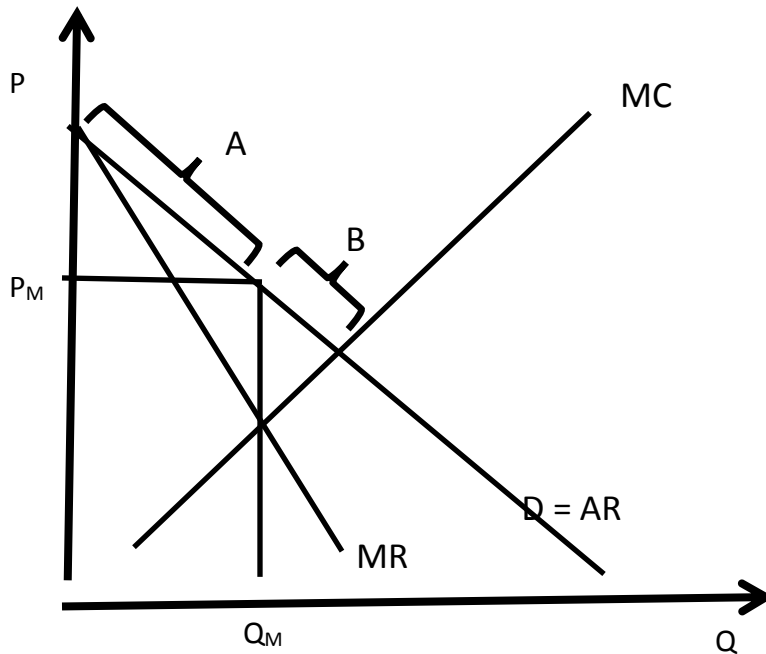


Figure 4.1 Pricing Strategy for Firms with Market Power

Area A along the demand curve represents consumers with a higher willingness to pay than the monopoly price P_M . Area B represents consumers who have been priced out of the market, since the monopoly price is higher than their willingness to pay. These two

groups of consumers represent two areas of untapped consumer surplus for a monopoly.

The monopoly price P_M represents the profit-maximizing price if the monopolist is constrained to set only a single price, and charge all customers the same single price. However, if the monopolist could charge more than one price, it may be able to capture more consumer surplus (willingness to pay) and convert it into producer surplus (profits). This Chapter describes and explains several pricing strategies for firms with market power. These strategies enhance profits over and above the single price profit level shown in Figure 4.1. The strategies include price discrimination, peak-load pricing, and two-part pricing.

4.2 Price Discrimination

Price discrimination is the practice of charging different prices to different customers. There are three forms of price discrimination, defined and explained in what follows.

Price Discrimination = charging different prices to different customers.

4.2.1 First Degree Price Discrimination

First degree price discrimination is the extreme form of charging different prices to different consumers, and makes use of the concept of “reservation price.” A consumer’s maximum willingness to pay is defined to be their reservation price.

Reservation Price = the maximum price that a consumer is willing to pay for a good.

First Degree Price Discrimination = Charging each consumer her reservation price.

First degree price discrimination is shown in Figure 4.2, where the initial levels of consumer surplus (CS_0) and producer surplus (PS_0) are defined for the competitive equilibrium. The competitive quantity is Q_C , and the competitive price is P_C . A monopoly could charge a price P_M at quantity Q_M to maximize profits with a single price.

Each individual’s willingness to pay is given by a point on the demand curve. If the firm knows each consumer’s maximum willingness to pay, or reservation price, it can transfer all consumer surplus to producer surplus. The firm extracts every dollar of surplus available in the market by charging each consumer the maximum price that they are willing to pay. First degree price discrimination results in levels of producer surplus and consumer surplus PS_1 and CS_1 , as shown in equation 4.1.

$$(4.1) PS_1 = PS_0 + CS_0; CS_1 = 0.$$

Every dollar of consumer surplus has been transferred to the firm. First degree price discrimination is also called, “Perfect Price Discrimination.”

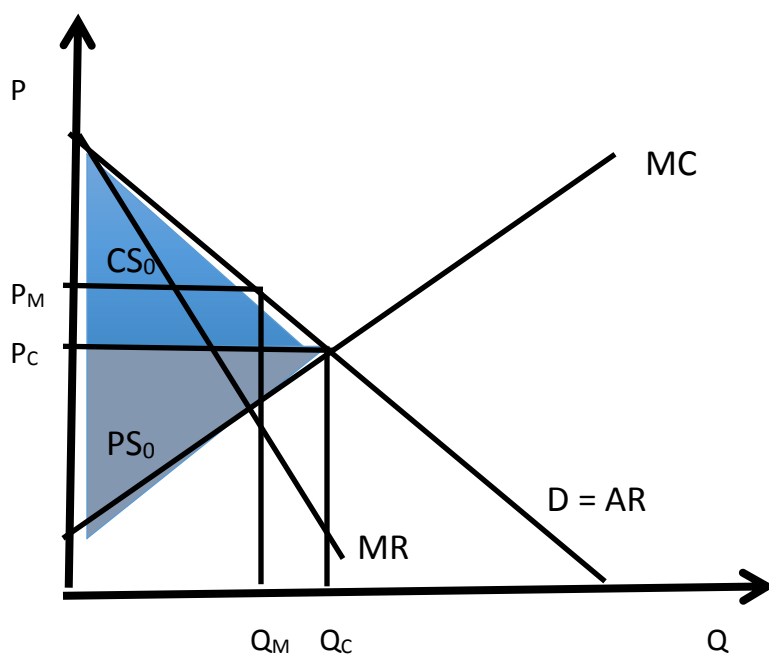


Figure 4.2 First Degree Price Discrimination

In most circumstances, it is difficult for the firm to practice first degree price discrimination. First, it is difficult to charge different prices to different consumers. In many cases, it is illegal to charge different prices to different people. Second, it is difficult and costly to elicit reservation prices from every consumer. Therefore, first degree price discrimination is an extreme, idealized case of charging different prices to different consumers. It is rare in the real world.

“Imperfect Price Discrimination” is a term used to describe markets that approach perfect price discrimination. Examples of imperfect price discrimination include car sales and college tuition rates for students in college. Car dealerships often post a “sticker price” and then lower the actual price depending on how much the consumer is willing to pay. Successful car sales persons are often those who have exceptional abilities to discern exactly how much each consumer is willing to pay, or their reservation price. Colleges and universities use imperfect price discrimination by offering scholarships and financial aid packages to students based on their willingness to enroll and attend an institution.

Imperfect price discrimination is shown in Figure 4.3, where different groups of consumers are charged different prices based on their willingness to pay. Price P_1 is a high price to capture consumers with high willingness to pay, price P_2 is the monopoly

price, and price P_3 is the competitive price. If a firm can distinguish different consumer groups' willingness to pay, it can enhance profits through this form of price discrimination.

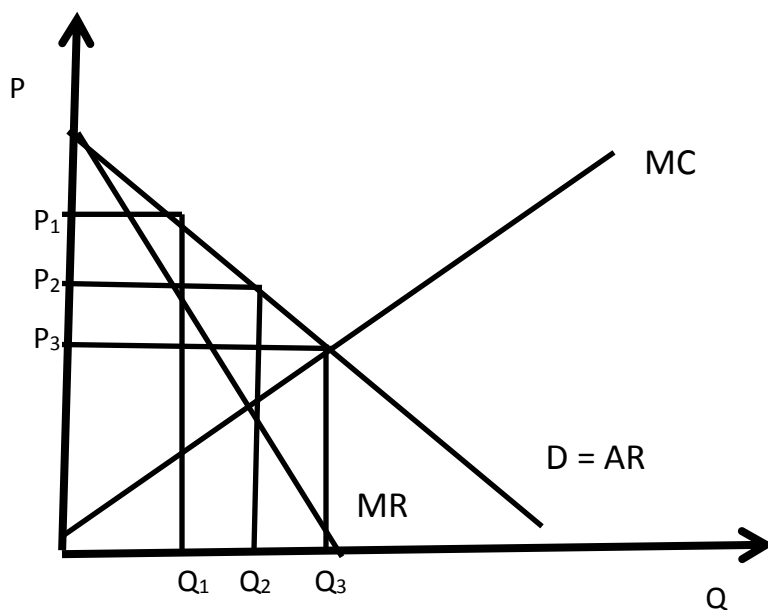


Figure 4.3 Imperfect Price Discrimination

4.2.2 Second Degree Price Discrimination

Second Degree Price Discrimination is a quantity discount.

Second Degree Price Discrimination = charging different per-unit prices for different quantities of the same good.

Second degree price discrimination is a common form of pricing and packaging. Consider an example of two different sized packages of salsa with different prices per unit. Suppose that consumers have different preferences for different sized salsa packages, and different demand curves reflect this.

For simplicity, assume that there are two consumers and two choices of package size (A and B).

A: 8 oz jar, price = 2 USD, price per unit = 0.25 USD/oz

B: 32 oz jar, price = 4.80 USD, price per unit = 0.15 USD/oz

Figure 4.4 shows consumer demand for each of the two consumers.

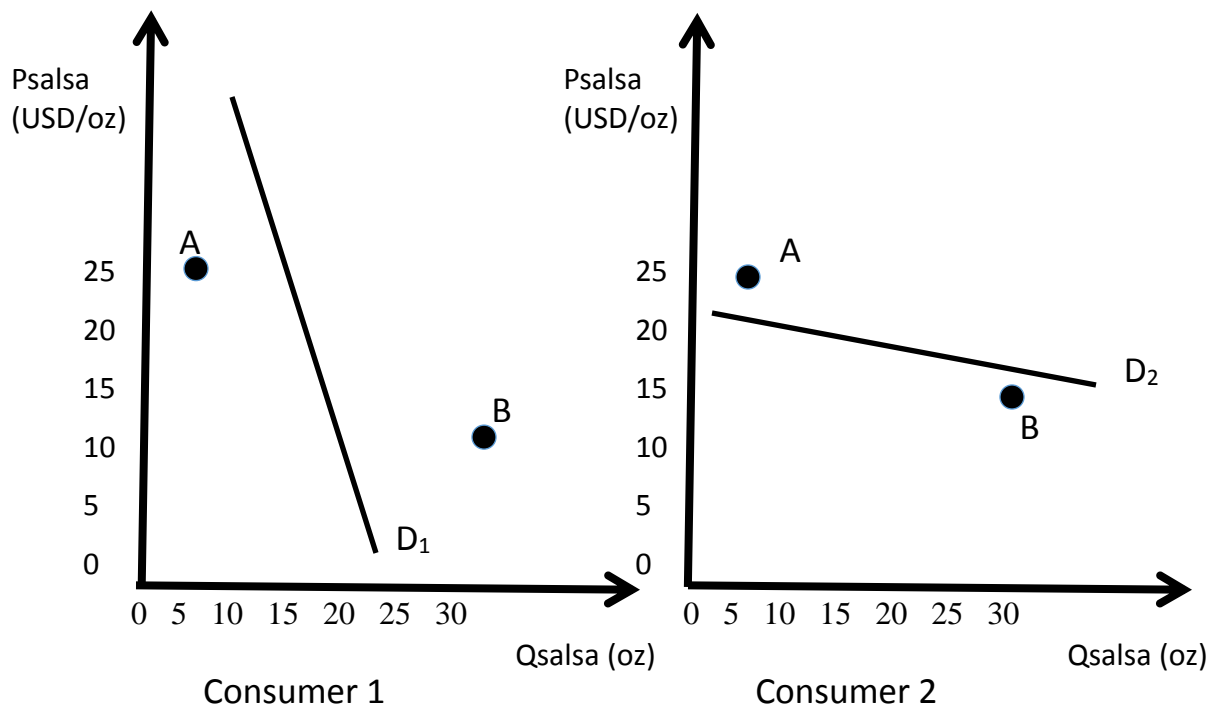


Figure 4.4 Second Degree Price Discrimination

Consumer 1 has a preference for smaller quantities. This consumer could be a single person who desires to purchase a small jar of salsa. Consumer 1's demand curve demonstrates that she is willing to pay for the 8 ounce jar of salsa (A), but not the 32 ounce jar (B). This is because A lies below demand curve D_1 , but not B. On the other hand, consumer 2 desires the large jar of salsa, perhaps this is a family of four persons. Consumer 2 is willing to purchase the 32 ounce jar (B), but not the 8 ounce jar (A). This is because B lies below the demand curve D_2 , but not A.

It can be shown that the salsa firm can enhance profits by offering both sizes A and B. Assume that the costs of producing salsa are equal to ten cents per ounce:

$$MC = 0.10 \text{ USD/oz}$$

Situation One. Firm sells 8-ounce jar only.

Consumer 1 buys, Consumer 2 does not buy.

$$Q = 8 \text{ oz}; \quad P = 0.25 \text{ USD/oz}; \quad MC = 0.10 \text{ USD/oz}$$

$$\pi_1 = (P - MC)Q = (0.25 - 0.10)8 = (0.15)8 = 1.20 \text{ USD}$$

Situation Two. Firm sells 32-ounce jar only.

Consumer 2 buys, Consumer 1 does not buy.

$$Q = 32 \text{ oz}; \quad P = 0.15 \text{ USD/oz}; \quad MC = 0.10 \text{ USD/oz}$$

$$\pi_2 = (P - MC)Q = (0.15 - 0.10)32 = (0.05)32 = 1.60 \text{ USD}$$

Situation Three. Firm sells both 8-oz and 32-ounce jars.

Consumer 1 buys 8 ounce jar, Consumer 2 buys 32 ounce jar.

$$\pi_3 = (0.25 - 0.10)8 + (0.15 - 0.10)32 = (0.15)8 + (0.05)32 = 2.80 \text{ USD}$$

Profits are larger if different sized packages are sold at the same time. Second degree price discrimination takes advantage of differences between consumers, and is usually more profitable than offering a good in only one package size. This explains the huge diversity of package sizes available for a large number of consumer goods.

4.2.3 Third Degree Price Discrimination

Third degree price discrimination is a practice of charging different prices to different consumer groups.

Third Degree Price Discrimination = charging different prices to different consumer groups.

A firm that faces more than one group of consumers can increase profits by offering a good at different prices to groups of consumers with different willingness to pay. The firm will maximize profits by setting the marginal revenue for each consumer group

equal to the marginal cost of production. This solution is shown in equation 4.2 for two consumer groups:

$$(4.2) \quad MR_1 = MR_2 = MC.$$

Two things are interesting about this result. First, the firm practicing third degree price discrimination is simply following the profit-maximizing strategy of continuing any activity as long as the benefits outweigh the costs. The firm will stop when marginal benefits from selling the good to both groups are equal to the marginal costs of producing the good. Second, this solution is similar to the solution for the multiplant monopoly: $MC_1 = MC_2 = MR$. Profit-maximizing firms use the same strategy for multiple plants and multiple consumers groups: set MR equal to MC in all circumstances.

Movie theaters often offer a student discount to students, as well as discounts for children, senior citizens, and military personnel. It may seem as if the theaters and other firms that offer these discounts are being nice to these groups. In reality, however, the firms are practicing third degree price discrimination in order to maximize profits! These groups of consumers have more elastic demands for movies, and would purchase a smaller number of movie tickets if the price was not discounted for them. A numerical example will demonstrate how third degree price discrimination works. Suppose that movie tickets are in thousands.

Movie ticket price = 12 USD/ticket

Student ticket price = 7 USD/ticket

Inverse Demand for movies: $P_1 = 20 - 4Q_1$

Inverse Demand for students: $P_2 = 10 - Q_2$

MC = 4 USD/ticket

$\max \pi = TR - TC$

$$= TR_1 - TC_1 + TR_2 - TC_2$$

$$= P_1Q_1 - 4Q_1 + P_2Q_2 - 4Q_2$$

$$= (20 - 4Q_1)Q_1 - 4Q_1 + (10 - Q_2)Q_2 - 4Q_2$$

$$= 20Q_1 - 4Q_1^2 - 4Q_1 + 10Q_2 - Q_2^2 - 4Q_2$$

$$\partial\pi/\partial Q_1 = 20 - 8Q_1 - 4 = 0$$

$$8Q_1 = 16$$

$$Q_1^* = 2 \text{ thousand movie tickets}$$

$$P_1^* = 20 - 4(2) = 12 \text{ USD/ticket}$$

$$\partial\pi/\partial Q_2 = 10 - 2Q_2 - 4 = 0$$

$$2Q_2 = 6$$

$$Q_2^* = 3 \text{ thousand movie tickets}$$

$$P_2^* = 10 - (3) = 7 \text{ USD/ticket}$$

The third degree price discrimination strategy is graphed in Figure 4.5.

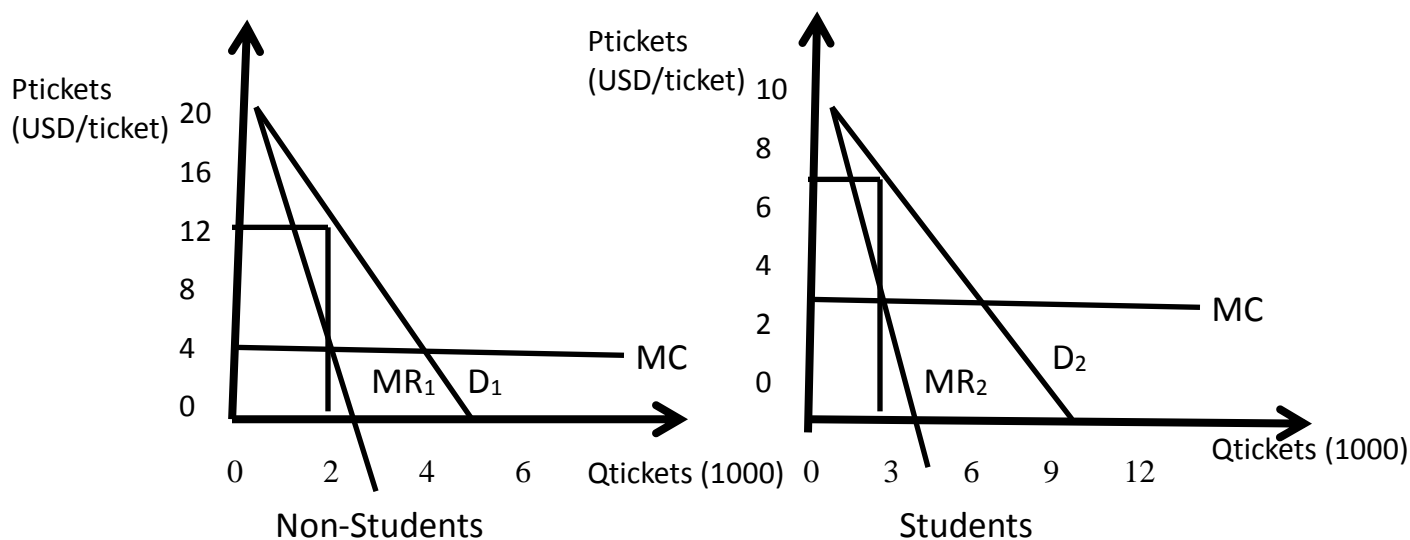


Figure 4.5 Third Degree Price Discrimination

A pricing rule for third degree price discrimination can be derived. Recall the pricing rule that was derived for a monopoly in Chapter 3:

$$(4.3) \quad MR = P[1 + (1/E^d)]$$

This pricing rule can be extended to include two groups of consumers, as follows.

$$MR_1 = MR_2 = MC$$

$$P_1[1 + (1/E_1)] = P_2[1 + (1/E_2)]$$

$$P_1/P_2 = [1 + (1/E_2)] / [1 + (1/E_1)]$$

The pricing rule for the third degree price discriminating firm shows that the highest price is charged to the consumer group with the smallest (most inelastic) price elasticity of demand (E^d). This follows what we have learned about the elasticity of demand: consumers with an elastic demand will switch to a substitute good if the price increases, whereas consumers with an inelastic demand are more likely to pay the price increase.

The next section will present intertemporal price discrimination, or charging different prices at different times.

4.3 Intertemporal Price Discrimination

Intertemporal price discrimination provides a method for firms to separate consumer groups based on willingness to pay. The strategy involves charging a high price initially, then lowering price after time passes. Many technology products and recently-released products follow this strategy.

Intertemporal Price Discrimination = charging a high price initially, then lowering price after time passes.

Intertemporal price discrimination is similar to second degree price discrimination, but charges a different price across time. Second degree price discrimination charges a different price for different quantities at the same time. Intertemporal price discrimination is shown in Figure 4.6.

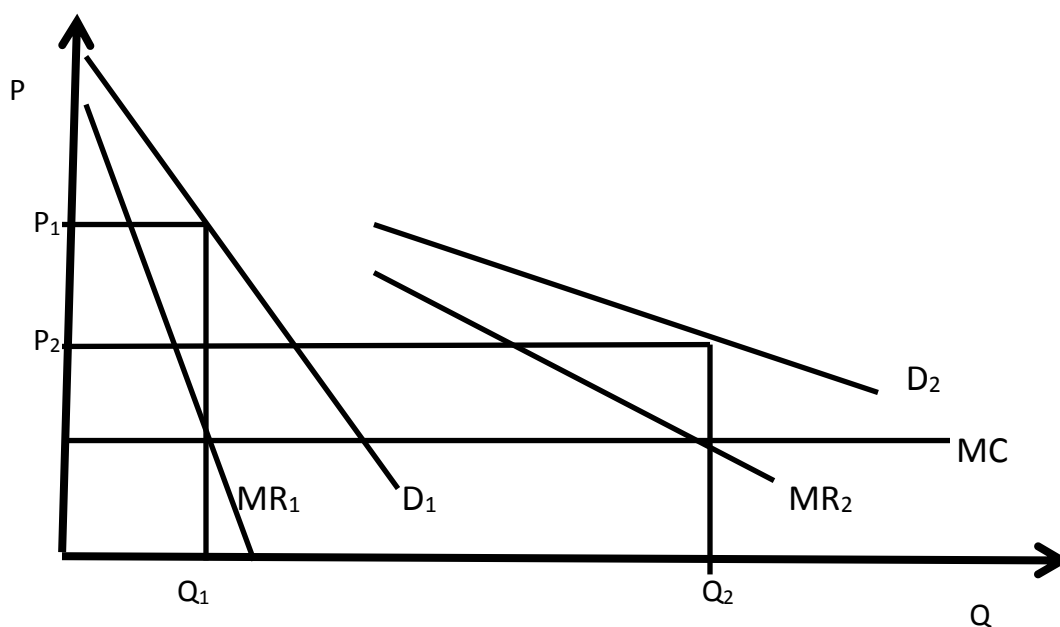


Figure 4.6 Intertemporal Price Discrimination, Graph One

The first group has a higher willingness to pay for the good, as shown by demand curve D_1 . This group will pay the higher initial price charged by the firm. A new iPhone release is a good example. Over time, Apple will lower the price to capture additional

consumer group, such as group two in Figure 4.6. In this fashion, the firm will extract a larger amount of consumer surplus than with a single price.

Intertemporal price discrimination can also be shown in a slightly different graph. The key feature of intertemporal price discrimination is a high initial price, followed by lower prices charged over time, as shown in Figure 4.7.

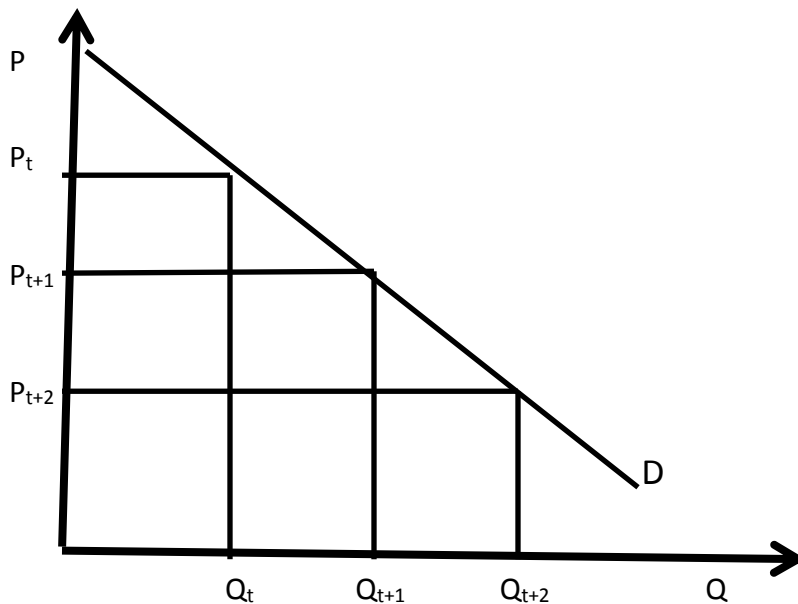


Figure 4.7 Intertemporal Price Discrimination, Graph Two

The concept of intertemporal price discrimination explains why new products are often priced at high prices, and the price is lowered over time. In the next section, peak-load pricing will be introduced.

4.4 Peak Load Pricing

The demand for many goods is larger during certain times of the day or week. For example, roads are congested during rush hours during the morning and evening commutes. Electricity has larger demand during the day than at night. Ski resorts have large (peak) demands during the weekends, and smaller demand during the week.

Peak Load Pricing = charging a high price during demand peaks, and a lower price during off-peak time periods.

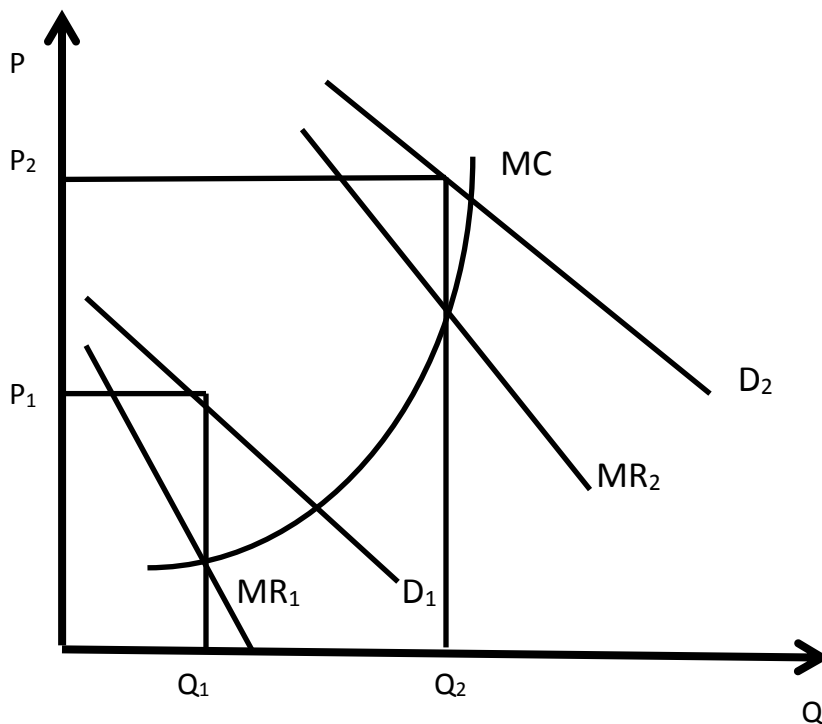


Figure 4.7 Peak Load Pricing

Figure 4.7 describes the demand for electricity during the day. Demand curve D_1 represents demand at off-peak hours at night. The electricity utility company will charge a price P_1 for the off-peak hours. The costs of producing electricity increase dramatically during peak hours. Electricity generation reaches the capacity of the generating plants, causing larger quantities of electricity to be expensive to produce. For large coal-fired plants, when capacity is reached, the firm will use natural gas to

generate the peak demand. To cover these higher costs, the firm will charge the higher price P_2 during peak hours. The same graph represents a large number of other goods that have peak demand at different times during a day, week, or year.

Economic efficiency is greatly improved by charging higher prices during peak times. If the utility were required to charge a single price at all times, it would lose the ability to charge consumers an appropriate price during peak demand periods. Charging a higher price during peak hours provides an incentive for consumers to switch consumption to off-peak hours. This saves society resources, since costs are lower during those times.

An example is electricity consumption. If consumers were charged higher prices during peak hours, they are able to shift some electricity demand to night, the off-peak hours. Dishwashers, laundry, and bathing can be shifted to off-peak hours, saving the consumer money and saving society resources. Electricity companies also promote “smart grid” technology that automatically turns thermostats down when individuals and families are not at home... saving the consumer and society money.

The next section will discuss a two-part tariff, or charging consumers a fixed fee for the right to purchase a good, and a per-unit fee for each unit purchased.

4.5 Two-Part Pricing

A monopoly or firm with market power can increase profits by charging a price structure with a fixed component, or entry fee, and a variable component, or usage fee.

Two-Part Pricing (also called Two Part Tariff) = a form of pricing in which consumers are charged both an entry fee (fixed price) and a usage fee (per-unit price).

Examples of two-part pricing include a phone contract that charges a fixed monthly charge and a per-minute charge for use of the phone. Amusement parks often charge an admission fee and an additional price per ride. Golf clubs typically charge an initiation fee and then usage fees based on meals eaten and golf rounds played. College football tickers usually require a “donation” to the athletic department, used for scholarships, and a per-ticket charge for the tickets.

Two-part pricing is shown in Figure 4.8, where a monopoly graph is presented.

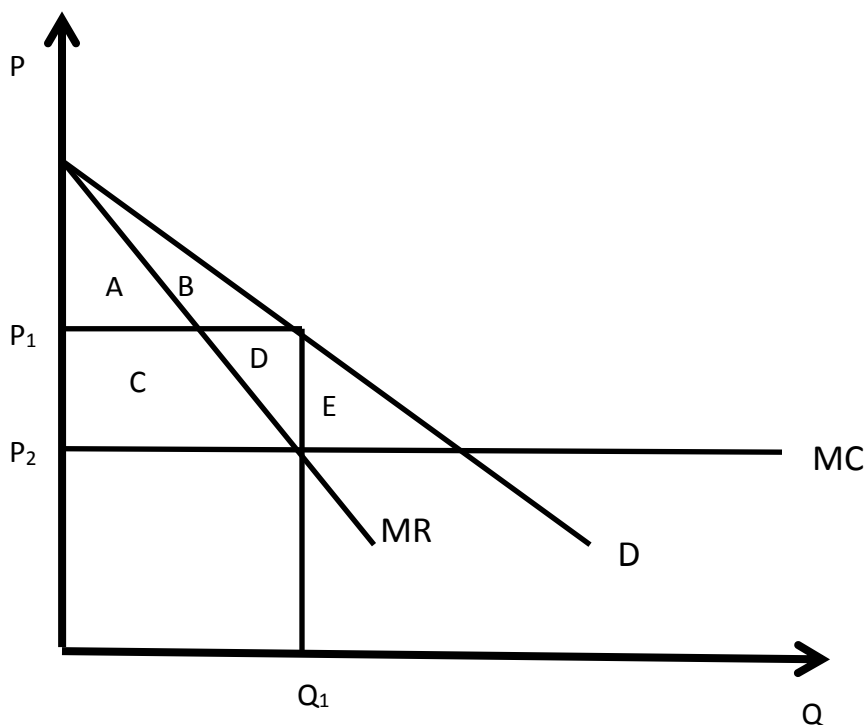


Figure 4.8 Two-Part Pricing

Suppose that the graph represents an individual consumer’s demand. In competitive equilibrium (subscript 0), price is equal to MC, and producer and consumer surplus are given by:

$$PS_0 = 0$$

$$CS_0 = ABCDE$$

This is because the firm charges a price equal to the constant marginal cost ($P = MC$), and there is no surplus. Consumers receive the total area between the demand curve (willingness to pay) and the price line (price paid).

A profit-maximizing firm (subscript 1) that charged a single price would maximize profits by producing Q_1 units of the good, and charging a price of P_1 . Surplus levels would be:

$$PS_1 = CD$$

$$CS_1 = AB$$

In this case, consumers have transferred areas C and D to producers, but still have surplus equal to area AB. Producers interested in increasing profits could devise a two-part pricing strategy that transfers more consumer surplus into producer surplus. Since $CS > 0$, consumers are willing to pay more than the monopoly price, and firms can extract a greater level of consumer surplus. The firm could charge an entry fee (T), and consumers would be willing to pay as long as the fee was less than their consumer surplus at the monopoly level ($CS_1 = AB$).

Consider the following two-part pricing scheme (subscript 2):

$$\text{Usage fee: } P_2 = MC$$

$$\text{Entry fee: } T = A+B+C+D+E \quad [T \text{ is set equal } CS_0 = CS \text{ under competition}]$$

$$PS_2 = ABCDE$$

$$CS_2 = 0$$

With a two-part pricing scheme, the firm has extracted every dollar of willingness to pay from consumers. The total amount of producer surplus under two-part pricing is given by:

$$PS_2 = T + (P_2 - MC)Q_2 = ABCDE$$

Notice that the firm earns zero profit from the usage fee (per-unit fee), since it sets the usage fee equal to the cost of production (MC). All of the profits come from the entry fee (fixed price) in this case.

To summarize, a two-part tariff for consumers with identical demands would (1) set usage fee (price per unit) equal to MC ($P = MC$), and (2) set a membership fee (entry fee) equal to consumer surplus at this price ($T = CS$ at $P = MC$). The two-part price will result in (1) $CS = 0$, and (2) $PS = T + (P - MC)Q = T$.

A numerical example will further elucidate the two-part price. Assume that an individual's inverse demand curve is given by: $P = 20 - 2Q$, and the cost function is $C(Q) = 2Q$. The firm seeks to find the optimal, profit-maximizing two-part tariff. The situation is shown in Figure 4.9.

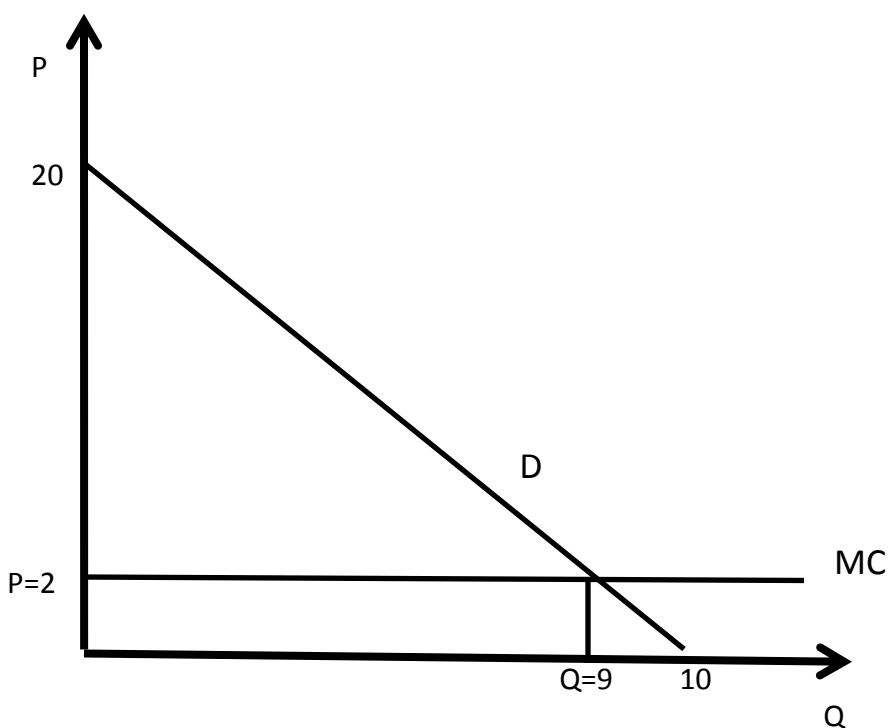


Figure 4.9 Two-Part Pricing Example

The firm will set the usage fee (per-unit price) equal to marginal cost: $P^* = MC = 2$. At this price, the quantity sold is found by substitution of the price into the inverse demand function: $2 = 20 - 2Q$, or $2Q = 18$, $Q^* = 9$ units, as shown in Figure 4.9. Next, the firm will determine the entry fee (fixed price), by calculating the area of consumer surplus at this price: $CS = 0.5(20 - 2)(9 - 0) = 0.5(18)(9) = 9 \cdot 9 = 81$ USD. Therefore, the firm sets the usage fee: $T = 81$ USD. The resulting levels of surplus are $CS = 0$ and $PS =$

81 USD. To summarize, the optimal two-part tariff is to set the usage fee equal to marginal cost and the entry fee equal to the level of consumer surplus at that price: $P^* = 2$ USD/unit, $T^* = 81$ USD.

In our investigation of two-part pricing, identical consumer demands have been assumed. In the real world, consumer demands may differ quite markedly across individuals. Given this possibility, the two-part pricing strategy can be summarized as follows.

1. If consumer demands are nearly identical, a two-part pricing scheme can increase profits by charging a price close to marginal cost and an entry fee.
2. If consumer demands are different, a two-part pricing scheme or a single price scheme can be utilized by setting a price well above marginal cost and a lower entry fee to capture all consumers. Or, set a single price.

In the next section, commodity bundling will be explained and explored.

4.6 Bundling

The practice of bundling is that of selling two or more goods together as a package.

Bundling = The practice of selling two or more goods together as a package.

Bundling is a widely-practiced sales strategy that takes advantage of differences in consumer willingness to pay for different goods. McDonalds Happy Meals are an example of bundling, since the customer purchases a hamburger, French fries, beverage, and toy as a single purchase. McDonalds was an innovator in bundling, and has expanded the practice to include “Value Meals.” Communication companies often package internet service, cable television, and phone service together into a package.

4.6.1 Bundling Examples

A simple example of bundling is a value meal at a fast food restaurant. To make things simple, assume that there are two consumers (A and B), two products (burger and fries) and marginal costs are equal to zero. The zero-cost assumption is not realistic, but the model results do not change when we assume zero costs.

Table 4.1 shows the reservation prices (willingness to pay) for both consumers for each good.

Table 4.1 Reservations Prices for Two Different Consumers.

<u>Consumer</u>	<u>Reservation Prices (USD/unit)</u>		
	<u>Burger</u>	<u>Fries</u>	<u>Bundle</u>
A	6	2	8
B	4	3	7

Recall that the reservation price is the maximum amount that a consumer is willing to pay for a good. The reservation price for the bundle is simply the sum of the two reservation prices for the burger and fries. Next, a comparison is made between selling the two good individually versus selling them as a bundle.

CASE ONE: Sell each product individually.

Π_{burger}

1. If set $P_{\text{burger}} = 6$ USD/unit, A buys, $\Pi_{\text{burger}} = 6 \cdot 1 = 6$ USD
2. If set $P_{\text{burger}} = 4$ USD/unit, A and B buy, $\Pi_{\text{burger}} = 4 \cdot 2 = 8$ USD

>>>Set $P^*_{\text{burger}} = 4$ USD/unit

Π_{fries}

1. If set $P_{\text{fries}} = 2$ USD/unit, A and B buy, $\Pi_{\text{fries}} = 2 \cdot 2 = 4$ USD
2. If set $P_{\text{fries}} = 3$ USD/unit, B buys, $\Pi_{\text{fries}} = 3 \cdot 1 = 3$ USD

>>>Set $P^*_{\text{fries}} = 2$ USD/unit

$\Pi_{\text{total individual}} = P_b Q_b + P_f Q_f = 4 \cdot 2 + 2 \cdot 2 = 8 + 4 = 12$ USD

CASE TWO: Bundle burger and fries into a single package.

Π_{bundle}

1. If set $P_{\text{bundle}} = 8$ USD/unit, A buys, $\Pi_{\text{bundle}} = 8 \cdot 1 = 8$ USD
2. If set $P_{\text{bundle}} = 7$ USD/unit, A and B buy, $\Pi_{\text{bundle}} = 7 \cdot 2 = 14$ USD

>>>Set $P^*_{\text{bundle}} = 7$ USD/unit

Bundling increases profit from 12 to 14 USD. This result will occur if the reservation prices are inversely correlated. To see this, work out the profits for selling goods individually and as a bundle for the reservation prices that appear in Table 4.2.

Table 4.2 Reservations Prices for Two Consumers with Correlated Reservation Prices.

<u>Consumer</u>	<u>Reservation Prices (USD/unit)</u>		
	<u>Burger</u>	<u>Fries</u>	<u>Bundle</u>
A	6	3	9
B	4	2	6

Bundling enhances profits when consumers have uncorrelated reservation prices. In this way, bundling takes advantage of differences in consumer willingness to pay.

Many firms have used “Green Bundling” to tie goods with environmental or sustainable goods. As long as consumer preferences for the good and the sustainability goal are uncorrelated, this strategy will increase profits.

4.6.2 Tying

A practice related to bundling is tying.

Tying = The practice of requiring a customer to purchase one good in order to purchase another.

Tying is a specific form of bundling. An example is Microsoft selling Windows software together with Internet Explorer, a web browser. A second example is printers and ink cartridges. Many hardware companies make a great deal of profit from selling ink cartridges for printers. The cartridges do not have a universal shape, so must be purchased specifically for each printer. The next section will discuss advertising.

4.7 Advertising

Advertising is a huge industry, with billions spent every year on marketing products. Are these enormous expenditures worth it? The benefits of increased sales and revenues must be at least as large as the increased costs to make it a good investment. In this section, the profit-maximizing level of advertising will be identified and evaluated.

One important point about advertising is the costs associated with advertising expenditures. If advertising works, it increases sales of the product. There are two major costs, the direct costs of advertising and the additional costs associated with increasing production if the advertising is effective.

A typical analysis sets the marginal revenues of advertising equal to the marginal costs of advertising ($MR_A = MC_A$). This would be correct if the level of output remained constant. However, the output level will increase if advertising works, and the additional costs of increased output must be taken into account for a comprehensive and correct analysis, as will be shown below.

4.7.1 Graphical Analysis

The graph for advertising is shown in Figure 4.10. Notice the two major effects of advertising and marketing efforts: (1) an increase in demand, in this case from D_0 to D_A , and (2) an increase in costs, shown here as the movement from ATC_0 to ATC_A . In the analysis shown here, advertising costs are considered to be fixed costs that do not vary with the level of output. This is true for a billboard, or television commercial. Note that the marginal costs do not change, since marginal costs are variable costs. The analysis could be easily extended to include variable advertising costs.

Economic analysis of advertising and marketing is straightforward: continue to advertise as long as the benefits outweigh the costs. In Figure 4.10, the optimal level of advertising occurs at quantity Q_A and price P_A . Profits with advertising are shown by the rectangle π_A . If profits are larger than without advertising, then advertising should be undertaken.

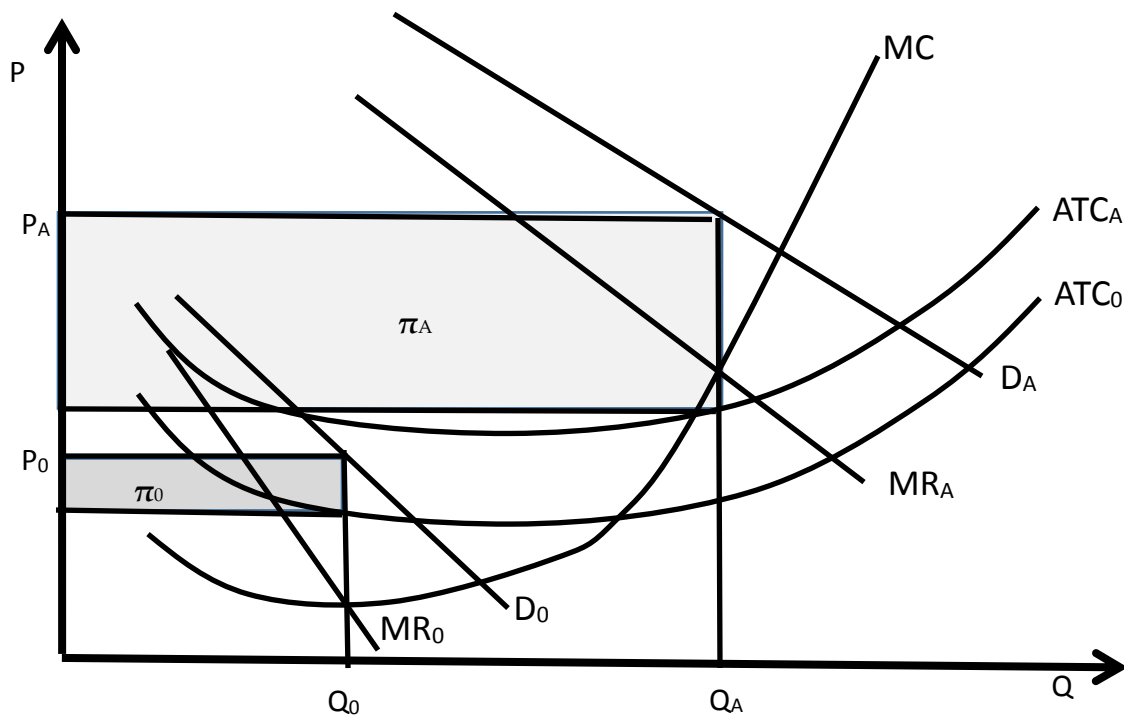


Figure 4.10 Advertising

In general, if the increase in sales is larger than the increase in costs, advertising should be undertaken. The optimal level of advertising can be found using marginal economic analysis, as described in the next section.

4.7.2 General Rule for Advertising

The profit-maximizing level of advertising can be derived, and the outcome is interesting and important, since it diverges from setting the marginal costs of advertising equal to the marginal revenues of advertising. Note that the graphical and mathematical analyses of advertising presented here could be used for any marketing program, not only advertising campaigns.

Assume that the demand for a product is given in Equation (4.4), where it can be seen that quantity demanded is a function of price and the level of advertising, A .

$$(4.4) Q^d = Q(P, A)$$

This demand equation differs from the usual approach of using an inverse demand equation. For this model, it is more useful to use the actual demand equation instead of an inverse demand equation. The profit equation is shown in Equation (4.5), where the cost function is given by $C(Q)$.

$$(4.5) \quad \max \pi = TR - TC$$

$$\pi = PQ(P, A) - C(Q) - A$$

The profit-maximizing level of advertising (A^*) is found by taking the first derivative of the profit function, and setting it equal to zero. This derivative is slightly more complex than usual, since the quantity that appears in the cost function depends on advertising, as shown in Equation 4.4. Therefore, to find the first derivative, we will need to use the chain rule from calculus, which is used to differentiate a composition of functions, such as the derivative of the function $f(g(x))$ shown in Equation (4.6).

$$(4.6) \quad \text{If } f(g(x)) \text{ then } \partial f/\partial x = f'(g(x)) * g'(x)$$

The chain rule simply says that to differentiate a composition of functions, first differentiate the outer layer, leaving the inner layer unchanged [the term $f'(g(x))$], then differentiate the inner layer [the term $g'(x)$].

In Equation (4.5), the cost function is a composition of the cost function and the demand function: $C(Q(P, A))$. So the derivative $\partial C/\partial A = C'(Q(A)) * Q'(A) = (\partial C/\partial Q) * (\partial Q/\partial A)$.

Thus, the first derivative of the profit equation with respect to advertising is given by:

$$\partial \pi / \partial A = P(\partial Q / \partial A) - (\partial C / \partial Q) * (\partial Q / \partial A) - 1 = 0$$

Rearranging, the first derivative can be written as in Equation (4.7):

$$(4.7) \quad P(\partial Q / \partial A) = MC * (\partial Q / \partial A) + 1.$$

The term on the left hand side is marginal revenues of advertising (MR_A), and the term on the right hand side is the marginal cost of advertising ($MC_A = 1$), plus the additional costs associated with producing a larger output to meet the increased demand resulting from advertising [$MC * (\partial Q / \partial A)$].

This result can be used to find an optimal “rule of thumb” for advertising, or a “General Rule for Advertising.” There are three preliminary definitions that will be useful in deriving this important result. First, the advertising to sales ratio is given by A/PQ , and

reflects the percentage of advertising in total revenues (price multiplied by quantity, PQ). Second, the advertising elasticity of demand is defined.

Advertising Elasticity of Demand (E^A) = The percentage change in quantity demanded resulting from a one percent change in advertising expenditure.

$$(4.8) \quad E^A = \% \Delta Q^d / \% \Delta A = (\partial Q / \partial A)(A/Q).$$

Third, recall the Lerner Index (L), a measure of monopoly power. We derived the relationship between the Lerner Index and the price elasticity of demand, shown in Equation (4.9):

$$(4.9) \quad L = (P - MC) / P = -1 / E^d.$$

With these three preliminary equations, we can derive a relatively simple and very useful general rule of advertising from the profit-maximizing condition for advertising, given in Equation (4.7).

$$P(\partial Q / \partial A) = MC * (\partial Q / \partial A) + 1$$

$$(P - MC)(\partial Q / \partial A) = 1$$

$$(P - MC) / P * (\partial Q / \partial A)(A/Q) = (A/PQ)$$

$$A/PQ = -E^A / E^d$$

This simple rule states that the profit-maximizing advertising to sales ratio (A/PQ) is equal to minus the elasticity of advertising divided by the price elasticity of demand. The result is simple and powerful: (1) if the elasticity of advertising is large, increase the advertising to sales ratio, and (2) if the price elasticity of demand is large, decrease the advertising to sale ratio. A firm with monopoly power, or a higher Lerner Index, will want to advertise more (E^d small), since the marginal profit from each additional dollar of advertising or marketing expenditure is greater.

Most business firms have at least crude approximations of the two elasticities needed to use this simple rule. Many firms advertise less than the optimal rate, since marketing can appear to be expensive if it is a large percentage of sales. However, simple economic principles can be used to determine the optimal, profit-maximizing level of advertising and/or marketing expenditures using this simple rule.

Chapter 5. Monopolistic Competition and Oligopoly

5.1 Market Structures

5.1.1 Market Structure Spectrum and Characteristics

Table 5.1 shows the four major categories of market structures and their characteristics.

Table 5.1 Market Structure Characteristics

<u>Perfect Competition</u>	<u>Monopolistic Competition</u>	<u>Oligopoly</u>	<u>Monopoly</u>
Homogeneous good	Differentiated good	Differentiated good	One good
Numerous firms	Many firms	Few firms	One firm
Free entry and exit	Free entry and exit	Barriers to entry	No entry

Perfect competition is on one end of the market structure spectrum, with numerous firms. The word, “numerous” has special meaning in this context. In a perfectly competitive industry, each firm is so small relative to the market that it cannot affect the price of the good. Each perfectly competitive firm is a price taker. Therefore, numerous firms means that each firm is so small that it is a price taker.

Monopoly is the other extreme of the market structure spectrum, with a single firm. Monopolies have monopoly power, or the ability to change the price of the good. Monopoly power is also called market power, and is measured by the Lerner Index.

This chapter defines and describes two intermediary market structures: monopolistic competition and oligopoly.

Monopolistic Competition = A market structure characterized by a differentiated product and freedom of entry and exit.

Monopolistically Competitive firms have one characteristic that is like a monopoly (a differentiated product provides market power), and one characteristic that is like a competitive firm (freedom of entry and exit). This form of market structure is common in market-based economies, and a trip to the grocery store reveals large numbers of differentiated products: toothpaste, laundry soap, breakfast cereal, and so on.

Oligopoly = A market structure characterized by barriers to entry and a few firms.

Oligopoly is a fascinating market structure due to interaction and interdependency between oligopolistic firms. What one firm does affects the other firms in the oligopoly.

Since monopolistic competition and oligopoly are intermediary market structures, the next section will review the properties and characteristics of perfect competition and monopoly. These characteristics will provide the defining characteristics of monopolistic competition and oligopoly.

5.1.2 Review of Perfect Competition

The perfectly competitive industry has four characteristics:

1. Homogenous product,
2. Large number of buyers and sellers (numerous firms),
3. Freedom of entry and exit, and
4. Perfect information.

The possibility of entry and exit of firms occurs in the long run, since the number of firms is fixed in the short run.

An equilibrium is defined as a point where there is no tendency to change. The concept of equilibrium can be extended to include the short run and long run.

Short Run Equilibrium = A point from which there is no tendency to change (a steady state), and a fixed number of firms.

Long Run Equilibrium = A point from which there is no tendency to change (a steady state), and entry and exit of firms.

In the short run, the number of firms is fixed, whereas in the long run, entry and exit of firms is possible, based on profit conditions. We will compare the short and long run for a competitive firm in Figure 5.1. The two panels in Figure 5.1 are for the firm (left) and industry (right), with vastly different units. This is emphasized by using “q” for the firm’s output level, and “Q” for the industry output level. The graph shows both short run and long run equilibria for a perfectly competitive firm and industry. In short run equilibrium, the firm faces a high price (P_{SR}), produces quantity Q_{SR} at $P_{SR} = MC$, and earns positive profits π_{SR} .

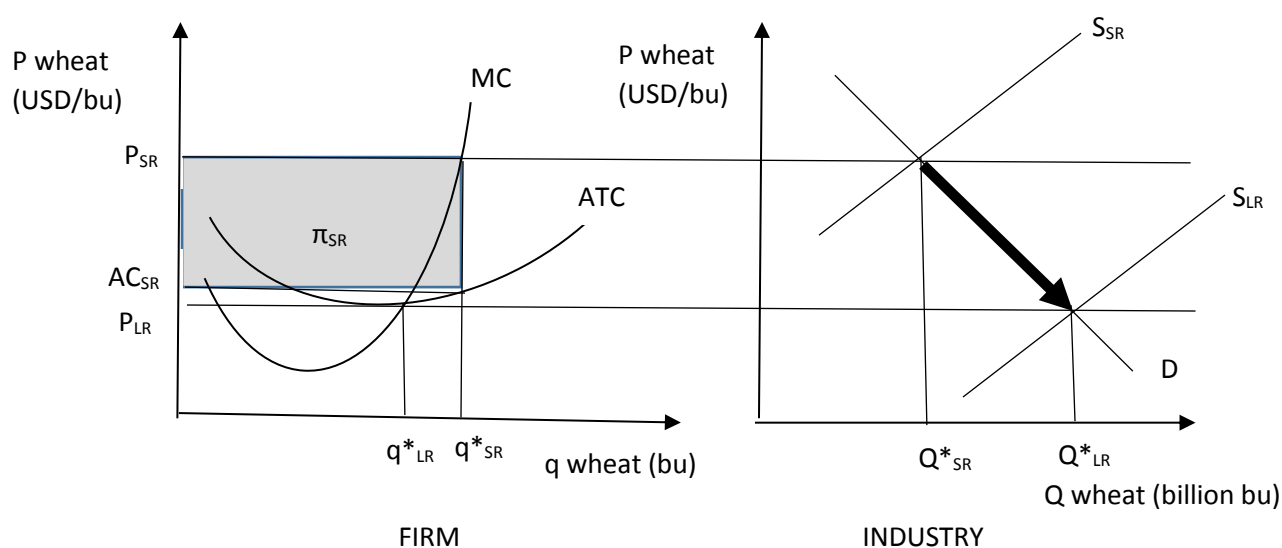


Figure 5.1 Short Run and Long Run Equilibria for a Perfectly Competitive Firm

Positive profits in the short run ($\pi_{SR} > 0$) lead to entry of other firms, as there are no barriers to entry in a competitive industry. The entry of new firms shifts the supply curve in the industry graph from supply S_{SR} to supply S_{LR} . Entry will occur until profits are driven to zero, and long run equilibrium is reached. In the long run, economic profits are equal to zero, so there is no incentive for entry or exit in the long run. Each firm is earning exactly what it is worth, the opportunity costs of all resources. In long run equilibrium, profits are zero ($\pi_{LR} = 0$), and price equals the minimum average cost point ($P = \min AC = MC$). Marginal costs equal average costs at the minimum average cost point. At the long run price, supply equals demand at price P_{LR} .

5.1.3 Review of Monopoly

The characteristics of monopoly include: (1) one firm, (2) one product, and (3) no entry (Table 5.1). The monopoly solution is shown in Figure 5.2.

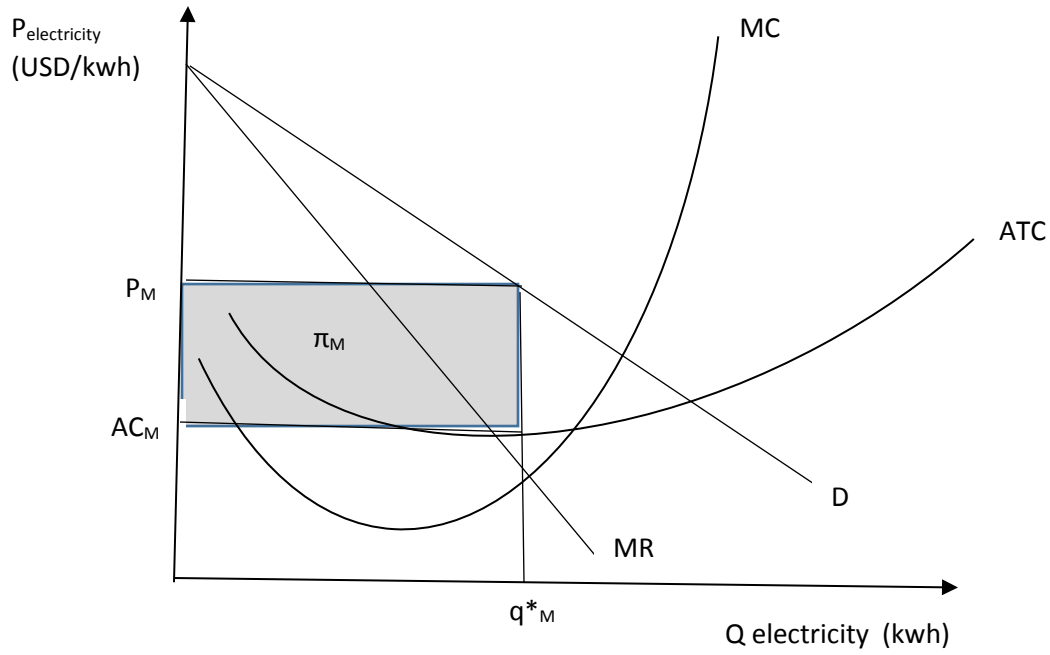


Figure 5.2 Monopoly Profit Maximization

5.2 Monopolistic Competition

Monopolistic competition is a market structure defined by free entry and exit, like competition, and differentiated products, like monopoly. Differentiated products provide each firm with some market power. Advertising and marketing of each individual product provide uniqueness that causes the demand curve of each good to be downward sloping. Free entry indicates that each firm competes with other firms and profits are equal to zero on long run equilibrium. If a monopolistically competitive firm is earning positive economic profits, entry will occur until economic profits are equal to zero.

5.2.1 Monopolistic Competition in the Short and Long Runs

The demand curve of a monopolistically competitive firm is downward sloping, indicating that the firm has a degree of market power. Market power derives from product differentiation, since each firm produces a different product. Each good has many close substitutes, so market power is limited: if the price is increased too much, consumers will shift to competitors' products.

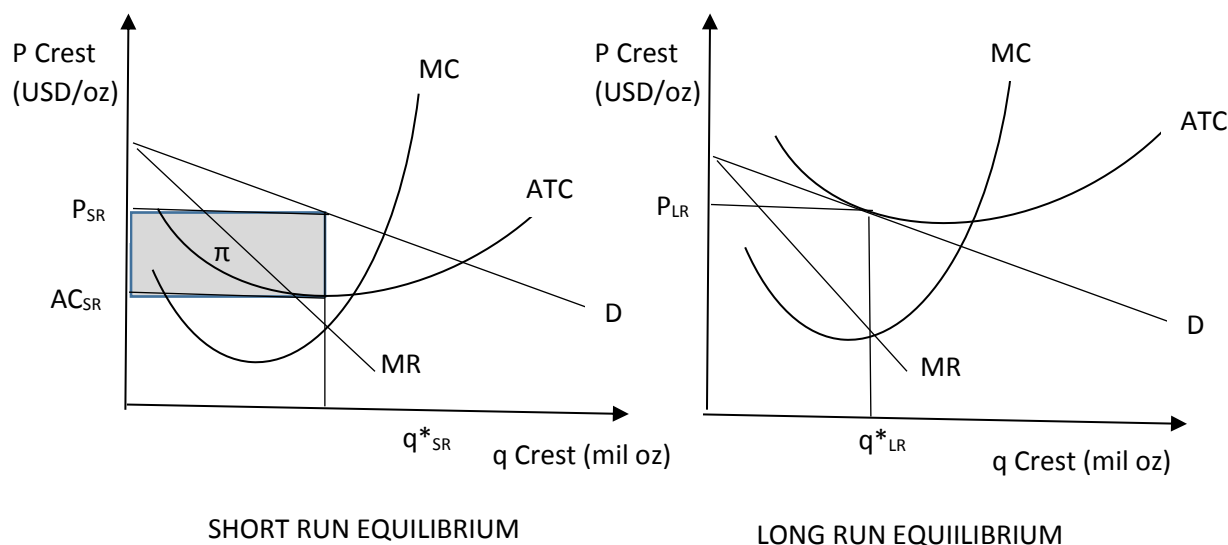


Figure 5.3 Monopolistic Competition in the Short Run and Long Run

Short and long run equilibria for the monopolistically competitive firm are shown in Figure 5.3. The demand curve facing the firm is downward sloping, but relatively elastic due to the availability of close substitutes. The short run equilibrium appears in

the left hand panel, and is nearly identical to the monopoly graph. The only difference is that for a monopolistically competitive firm, the demand is relatively elastic, or flat. Otherwise, the short run profit-maximizing solution is the same as a monopoly. The firm sets marginal revenue equal to marginal cost, produces output level q^*_{SR} and charges price P_{SR} . The profit level is shown by the shaded rectangle π .

The long run equilibrium is shown in the right hand panel. Entry of other firms occurs until profits are equal to zero; total revenues are equal to total costs. Thus, the demand curve is tangent to the average cost curve at the optimal long run quantity, q_{LR} . The long run profit-maximizing quantity is found where marginal revenue equals marginal cost, which also occurs at q_{LR} .

5.2.2 Economic Efficiency and Monopolistic Competition

There are two sources of inefficiency in monopolistic competition. First, dead weight loss due to monopoly power: price is higher than marginal cost. Second, excess capacity: the equilibrium quantity is smaller than the lowest cost quantity at the minimum point on the average cost curve. These two sources of inefficiency can be seen in Figure 5.4.

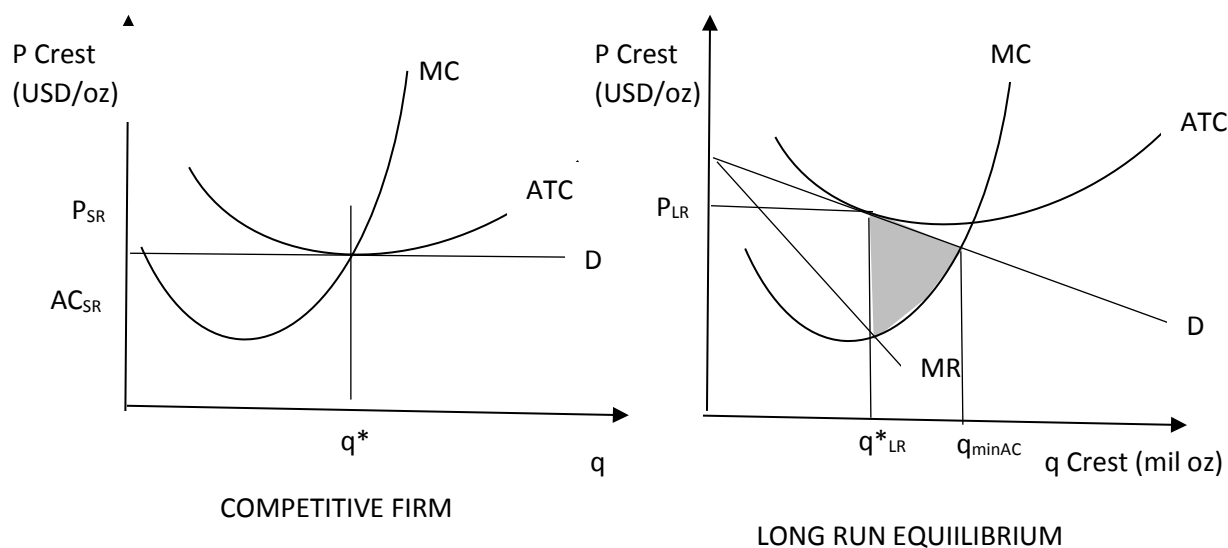


Figure 5.4 Comparison of Efficiency for Competition and Monopolistic Competition

First, there is dead weight loss (DWL) due to market power: the price is higher than marginal cost in long run equilibrium. In the right hand panel of Figure 5.4, the price at the long run equilibrium quantity is P_{LR} , and marginal cost is lower: $P_{LR} > MC$. This

causes dead weight loss to society, since the competitive equilibrium would be at a larger quantity where $P = MC$.

The second source of inefficiency associated with monopolistic competition is excess capacity. This can also be seen in the right hand panel of Figure 5.4, where the long run equilibrium quantity is lower than the quantity where average costs are lowest ($q_{\min AC}$). Therefore, the firm could produce at a lower cost by increasing output to the level where average costs are minimized.

Given these two inefficiencies associated with monopolistic competition, some individuals and groups have called for government intervention. Regulation could be used to reduce or eliminate the inefficiencies by removing product differentiation. This would result in a single product instead of a large number of close substitutes.

Regulation is probably not a good solution to the inefficiencies of monopolistic competition, for two reasons. First, the market power of a typical firm in most monopolistically competitive industries is small. Each monopolistically competitive industry has many firms that produce sufficiently substitutable products to provide enough competition to result in relatively low levels of market power. If the firms have small levels of market power, then the deadweight loss and excess capacity inefficiencies are likely to be small.

Second, the benefit provided by monopolistic competition is product diversity. The gain from product diversity can be large, as consumers are willing to pay for different characteristics and qualities. Therefore, the gain from product diversity is likely to outweigh the costs of inefficiency. Evidence for this claim can be seen in market-based economies, where there is a huge amount of product diversity.

The next Chapter will introduce and discuss oligopoly.

5.3 Oligopoly

An oligopoly is defined as a market structure with a few firms and barriers to entry.

Oligopoly = A market structure with a few firms and barriers to entry.

There is often a high level of competition between firms, as each firm makes decisions on prices, quantities, and advertising to maximize profits. Since there are a small number of firms, each firm's profit level depends not only on the firm's own decisions, but also on the decisions of the other firms in the oligopolistic industry.

5.3.1 Strategic Interactions

Each firm must consider both: (1) other firms' reactions to the firm's own decisions, and (2) own firm's reactions to the other firms' decisions. Thus, there is a continuous interplay between decisions and reactions to those decisions by all firms in the industry. Each oligopolist must take into account these strategic interactions when making decisions. Since all firms in an oligopoly have outcomes that depend on the other firms, these strategic interactions are the foundation of the study and understanding of oligopoly.

For example, each automobile firm's market share depends on the prices and quantities of all of the other firms in the industry. If Ford lowers prices relative to other car manufacturers, it will increase its market share at the expense of the other companies.

When making decisions that consider the possible reactions of other firms, firm managers usually assume that the manager of competing firms are rational and intelligent. The strategic interactions that ensue form the study of game theory, the topic of Chapter 6. John Nash (1928-2015) was an American mathematician who was one of the pioneers in game theory. Economists and mathematicians use the concept of a Nash Equilibrium to describe a common outcome in game theory that is frequently used in the study of oligopoly.

Nash Equilibrium = An outcome where there is no tendency to change based on each individual choosing a strategy given the strategy of rivals.

In the study of oligopoly, the Nash Equilibrium assumes that each firm makes rational profit-maximizing decisions while holding the behavior of rival firms constant. This assumption is made to simplify oligopoly models, given the potential for enormous complexity of strategic interactions between firms. As an aside, this assumption is one of the interesting themes of the motion picture, “A Beautiful Mind,” starring Russell Crowe as John Nash. The concept of Nash Equilibrium is also the foundation of the models of oligopoly presented in the next three sections: the Cournot, Bertrand, and Stackelberg models of oligopoly.

5.3.2 Cournot Model

Augustin Cournot (1801-1877) was a French mathematician who developed the first model of oligopoly explored here. The Cournot model is a model of oligopoly in which firms produce a homogeneous good, and assumes that the competitor’s output is fixed when deciding how much to produce.

A numerical example of the Cournot model follows, where it is assumed that there are two identical firms (a duopoly), with output given by Q_i ($i=1,2$). Therefore, total industry output is equal to: $Q = Q_1 + Q_2$. Market demand is a function of price and given by $Q^d = Q^d(P)$, thus the inverse demand function is $P = P(Q^d)$. Note that the price depends on the market output Q , which is the sum of both individual firm’s outputs. In this way, each firm’s output has an influence on the price and profits of both firms. This is the basis for strategic interaction in the Cournot model: if one firm increases output, it lowers the price facing both firms. The inverse demand function and cost function are given in Equation 5.1.

$$(5.1) \quad P = 40 - Q \quad C(Q_i) = 7Q_i \quad i = 1,2$$

Each firm chooses the optimal, profit-maximizing output level given the other firm’s output. This will result in a Nash Equilibrium, since each firm is holding the behavior of the rival constant. Firm One maximizes profits as follows:

$$\max \pi_1 = TR_1 - TC_1$$

$$\max \pi_1 = P(Q)Q_1 - C(Q_1) \quad [\text{price depends on total output } Q = Q_1 + Q_2]$$

$$\max \pi_1 = [40 - Q]Q_1 - 7Q_1$$

$$\max \pi_1 = [40 - Q_1 - Q_2]Q_1 - 7Q_1$$

$$\max \pi_1 = 40Q_1 - Q_1^2 - Q_2Q_1 - 7Q_1$$

$$\partial\pi_1/\partial Q_1 = 40 - 2Q_1 - Q_2 - 7 = 0$$

$$2Q_1 = 33 - Q_2$$

$$Q_1^* = 16.5 - 0.5Q_2$$

This equation is called the “Reaction Function” of Firm One. This is as far as the mathematical solution can be simplified, and represents the Cournot solution for Firm One. It is a reaction function since it describes what Firm One’s reaction will be given the output level of Firm Two. This equation represents the strategic interactions between the two firms, as changes in Firm Two’s output level will result in changes in Firm One’s response. Firm One’s optimal output level depends on Firm Two’s behavior and decision making. Oligopolists are interconnected in both behavior and outcomes.

The two firms are assumed to be identical in this duopoly. Therefore, Firm Two’s reaction function will be symmetrical to the Firm One’s reaction function (check this by setting up and solving the profit-maximization equation for Firm Two):

$$Q_2^* = 16.5 - 0.5Q_1$$

The two reaction functions can be used to solve for the Cournot-Nash Equilibrium. There are two equations and two unknowns (Q_1 and Q_2), so a numerical solution is found through substitution of one equation into the other.

$$Q_1^* = 16.5 - 0.5(16.5 - 0.5Q_1)$$

$$Q_1^* = 16.5 - 8.25 + 0.25Q_1$$

$$Q_1^* = 8.25 + 0.25Q_1$$

$$Q_1^* = 8.25 + 0.25Q_1$$

$$0.75Q_1^* = 8.25$$

$$Q_1^* = 8.25$$

$$Q_1^* = 11$$

Due to symmetry from the assumption of identical firms:

$$Q_i = 11 \quad i = 1,2 \quad Q = 22 \quad P = 18$$

Profits for each firm are:

$$\pi_i = P(Q)Q_i - C(Q_i) = 18(11) - 7(11) = (18 - 7)11 = 11(11) = 121 \text{ USD}$$

This is the Cournot-Nash solution for oligopoly, found by each firm assuming that the other firm holds its output level constant. The Cournot model can be easily extended to more than two firms, but the math does get increasingly complex as more firms are added. Economists utilize the Cournot model because it is based on intuitive and realistic assumptions, and the Cournot solution is intermediary between the outcomes of the two extreme market structures of perfect competition and monopoly.

This can be seen by solving the numerical example for competition, Cournot, and monopoly models, and comparing the solutions for each market structure.

In a competitive industry, free entry results in price equal to marginal cost. In the case of the numerical example, $P = 7$. When this competitive price is substituted into the inverse demand equation, $7 = 40 - Q$, or $Q_c = 33$. Profits are found by solving $(P - MC)Q$, or $\pi_c = (7 - 7)Q = 0$. The competitive solution is given in Equation (5.2).

$$(5.2) \quad P_c = 7 \quad Q_c = 33 \quad \pi_c = 0$$

The monopoly solution is found by maximizing profits as a single firm.

$$\max \pi_m = TR_m - TC_m$$

$$\max \pi_m = P(Q_m)Q_m - C(Q_m) \quad [\text{price depends on total output } Q = Q_1 + Q_2]$$

$$\max \pi_m = [40 - Q_m]Q_m - 7Q_m$$

$$\max \pi_m = 40Q_m - Q_m^2 - 7Q_m$$

$$\partial\pi_m/\partial Q_m = 40 - 2Q_m - 7 = 0$$

$$2Q_m = 33$$

$$Q_m^* = 16.5$$

$$P_m = 40 - 16.5 = 23.5$$

$$\pi_m = (P_m - MC_m)Q_m = (23.5 - 7)16.5 = 16.5(16.5) = 272.25 \text{ USD}$$

The monopoly solution is given in Equation (5.3).

$$(5.2) \quad P_m = 23.5 \quad Q_m = 16.5 \quad \pi_m = 272.5 \text{ USD}$$

The competitive, Cournot, and monopoly solutions can be compared on the same graph for the numerical example (Figure 5.5).

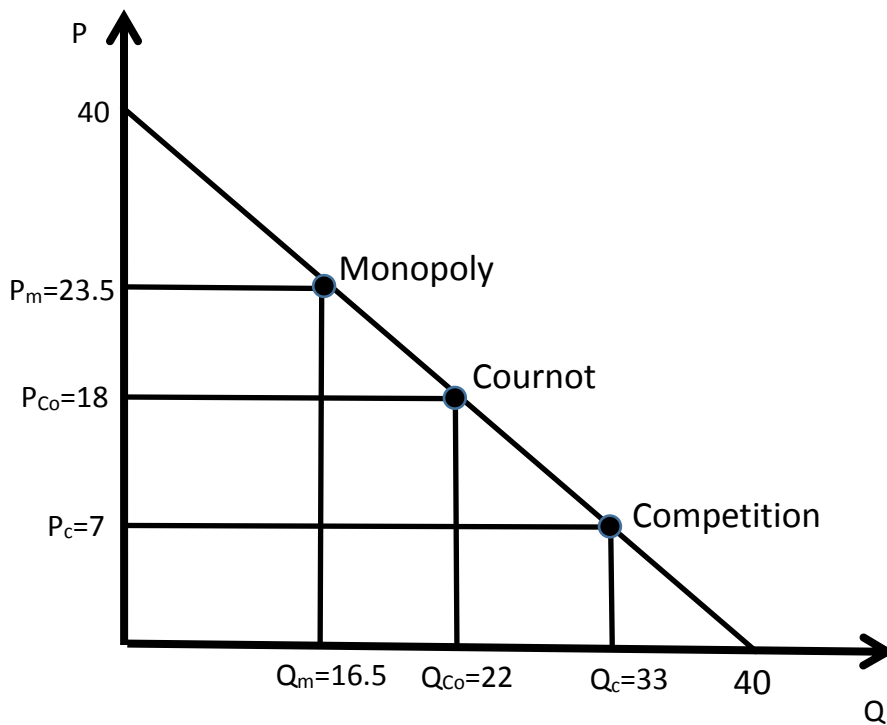


Figure 5.5 Comparison of Perfect Competition, Cournot, and Monopoly Solutions

The Cournot price and quantity are between perfect competition and monopoly, which is an expected result, since the number of firms in an oligopoly lies between the two market structure extremes.

5.3.3 Bertrand Model

Joseph Louis François Bertrand (1822-1900) was also a French mathematician who developed a competing model to the Cournot model. Bertrand asked the question, “what would happen in an oligopoly model if each firm held the other firm’s price constant?” The Bertrand model is a model of oligopoly in which firms produce a homogeneous good, and each firm takes the price of competitors fixed when deciding what price to charge.

Assume two firms in an oligopoly (a duopoly), where the two firms choose the price of their good simultaneously at the beginning of each period. Consumers purchase from the lowest price firm, since the products are homogeneous (perfect substitutes). If the two firms charge the same price, one-half of the consumers buy from each firm. Let the

demand equation be given by $Q^d = Q^d(P)$. The Bertrand model follows these three statements:

- (1) If $P_1 < P_2$, then Firm One sells Q^d and Firm Two sells 0.
- (2) If $P_1 > P_2$, then Firm One sells 0 and Firm Two sells Q^d .
- (3) If $P_1 = P_2$, then Firm One sells $0.5Q^d$ and Firm Two sells $0.5Q^d$.

A numerical example demonstrates the outcome of the Bertrand model, which is a Nash Equilibrium. Assume two firms sell a homogeneous product, and compete by choosing prices simultaneously while holding the other firm's price constant. Let the demand function be given by $Q^d = 50 - P$ and the costs are summarized by $MC_1 = MC_2 = 5$.

- (1) Firm One sets $P_1 = 20$, and Firm Two sets $P_2 = 15$. Firm Two has the lower price, so all customers purchase the good from Firm Two.
 $Q_1 = 0, Q_2 = 35. \pi_1 = 0, \pi_2 = (15 - 5)35 = 350$ USD.

After period one, Firm One has a strong incentive to lower the price below P_2 . The Bertrand assumption is that both firms will choose a price, holding the other firm's price constant. Thus, Firm One undercuts P_2 slightly, assuming that Firm Two will maintain its price at $P_2 = 15$. Firm Two will keep the same price, assuming that Firm One will maintain $P_1 = 20$.

- (2) Firm One sets $P_1 = 14$, and Firm Two sets $P_2 = 15$. Firm One has the lower price, so all customers purchase the good from Firm One.
 $Q_1 = 36, Q_2 = 0. \pi_1 = (14 - 5)36 = 324$ USD, $\pi_2 = 0$.

After period two, Firm Two has a strong incentive to lower price below P_1 . This process of undercutting the other firm's price will continue and the "price war" will result in the price being driven down to marginal cost. In equilibrium, both firms lower their price until price is equal to marginal cost: $P_1 = P_2 = MC_1 = MC_2$. The price cannot go lower than this, or the firms would go out of business due to negative economic profits. To restate the Bertrand model, each firm selects a price, given the other firm's price. The Bertrand results are given in Equation 5.3:

$$(5.3) \quad P_1 = P_2 = MC_1 = MC_2 \quad Q_1 = Q_2 = 0.5Q^d \quad \pi_1 = \pi_2 = 0 \text{ in the SR and LR.}$$

The Bertrand model of oligopoly suggests that oligopolies have the competitive solution, due to competing over price. There are many oligopolies that behave this way, such as gasoline stations at a given location. Other oligopolies may behave more like Cournot oligopolists, with an outcome somewhere in between perfect competition and monopoly.

5.3.4 Stackelberg Model

Heinrich Freiherr von Stackelberg (1905-1946) was a German economist who contributed to game theory and the study of market structures with a model of firm leadership, or the Stackelberg model of oligopoly. This model assumes that there are two firms in the industry, but they are asymmetrical: there is a “leader” and a “follower.” Stackelberg used this model of oligopoly to determine if there was an advantage to going first, or a “first-mover advantage.”

A numerical example is used to explore the Stackelberg model. Assume two firms, where Firm One is the leader and produces Q_1 units of a homogeneous good. Firm Two is the follower, and produces Q_2 units of the good. The inverse demand function is given by $P = 100 - Q$, where $Q = Q_1 + Q_2$. The costs of production are given by the cost function: $C(Q) = 10Q$.

This model is solved recursively, or backwards. Mathematically, the problem must be solved this way to find a solution. Intuitively, each firm will hold the other firm’s output constant, similar to Cournot, but the leader must know the follower’s best strategy in order to move first. Thus, Firm One solves Firm Two’s profit maximization problem in order to know what output it will produce, or Firm Two’s reaction function. Once the reaction function of the follower (Firm Two) is known, then the leader (Firm One) maximizes profits by substitution of Firm Two’s reaction function into Firm One’s profit maximization equation.

Firm One starts by solving for Firm Two’s reaction function:

$$\max \pi_2 = TR_2 - TC_2$$

$$\max \pi_2 = P(Q)Q_2 - C(Q_2) \quad [\text{price depends on total output } Q = Q_1 + Q_2]$$

$$\max \pi_2 = [100 - Q]Q_2 - 10Q_2$$

$$\max \pi_2 = [100 - Q_1 - Q_2]Q_2 - 10Q_2$$

$$\max \pi_2 = 100Q_2 - Q_1Q_2 - Q_2^2 - 10Q_2$$

$$\partial\pi_2/\partial Q_2 = 100 - Q_1 - 2Q_2 - 10 = 0$$

$$2Q_2 = 90 - Q_1$$

$$Q_2^* = 45 - 0.5Q_1$$

Next, Firm One, the leader, maximizes profits holding the follower's output constant using the reaction function:

$$\max \pi_1 = TR_1 - TC_1$$

$$\max \pi_1 = P(Q)Q_1 - C(Q_1) \quad [\text{price depends on total output } Q = Q_1 + Q_2]$$

$$\max \pi_1 = [100 - Q]Q_1 - 10Q_1$$

$$\max \pi_1 = [100 - Q_1 - Q_2]Q_1 - 10Q_1$$

$$\max \pi_1 = [100 - Q_1 - (45 - 0.5Q_1)]Q_1 - 10Q_1 \quad [\text{substitution of One's reaction function}]$$

$$\max \pi_1 = [100 - Q_1 - 45 + 0.5Q_1]Q_1 - 10Q_1$$

$$\max \pi_1 = [55 - 0.5Q_1]Q_1 - 10Q_1$$

$$\max \pi_1 = 55Q_1 - 0.5Q_1^2 - 10Q_1$$

$$\partial\pi_1/\partial Q_1 = 55 - Q_1 - 10 = 0$$

$$Q_1^* = 45$$

This can be substituted back into Firm Two's reaction function to solve for Q_2^* .

$$Q_2^* = 45 - 0.5Q_1 = 45 - 0.5(45) = 45 - 22.5 = 22.5$$

$$Q = Q_1 + Q_2 = 45 + 22.5 = 67.5$$

$$P = 100 - Q = 100 - 67.5 = 32.5$$

$$\pi_1 = (32.5 - 10)45 = 22.5(45) = 1012.5 \text{ USD}$$

$$\pi_2 = (22.5 - 10)22.5 = 12.5(22.5) = 506.25 \text{ USD}$$

We have now covered three models of oligopoly: Cournot, Bertrand, and Stackelberg. These three models are alternative representations of oligopolistic behavior. The Bertrand model is relatively easy to identify in the real world, since it results in a price war and competitive prices. It may be more difficult to identify which of the quantity models to use to analyze a real-world industry: Cournot or Stackelberg?

The model that is most appropriate depends on the industry under investigation.

- (1) The Cournot model may be most appropriate for an industry with similar firms, with no market advantages or leadership.
- (2) The Stackelberg model may be most appropriate for an industry dominated by relatively large firms.

Oligopoly has many different possible outcomes, and several economic models to better understand the diversity of industries. Notice that if the firms in an oligopoly colluded, or acted as a single firm, they could achieve the monopoly outcome. If firms banded together to make united decisions, the firms could set the price or quantity as a monopolist would. This is illegal in many nations, including the United States, since the outcome is anti-competitive, and consumers would have to pay monopoly prices under collusion.

If firms were able to collude, they could divide the market into shares and jointly produce the monopoly quantity by restricting output. This would result in the monopoly price, and the firms would earn monopoly profits. However, under such circumstances, there is always an incentive to “cheat” on the agreement by selling more output. If the other firms in the industry are restricting output, a firm can increase profits by increasing output, at the expense of the other firms in the collusive agreement. We will discuss this possibility in the next section.

To summarize our discussion of oligopoly thus far, we have two models that assume that a firm holds the other firm’s output constant: Cournot and Stackelberg. These two models result in positive economic profits, at a level between perfect competition and monopoly. The third model, Bertrand, assumes that each firm holds the other firm’s price constant. The Bertrand model results in zero economic profits, as the price is bid down to the competitive level, $P = MC$.

The most important characteristic of oligopoly is that firm decisions are based on strategic interactions. Each firm’s behavior is strategic, and strategy depends on the other firms’ strategies. Therefore, oligopolists are locked into a relationship with rivals that differs markedly from perfect competition and monopoly.

5.3 Oligopoly (continued)

5.3.5 Collusion and Game Theory

Collusion occurs when oligopoly firms make joint decisions, and act as if they were a single firm. Collusion requires an agreement, either explicit or implicit, between cooperating firms to restrict output and achieve the monopoly price. This causes the firms to be interdependent, as the profit levels of each firm depend on the firm's own decisions and the decisions of all other firms in the industry. This strategic interdependence is the foundation of game theory.

Game Theory = A framework to study strategic interactions between players, firms, or nations.

A game is defined as:

Game = A situation in which firms make strategic decisions that take into account each others' actions and responses.

A game can be represented as a payoff matrix, which shows the payoffs for each possibility of the game, as will be shown below. A game has players who select strategies that lead to different outcomes, or payoffs. A Prisoner's Dilemma is a famous game theory example where two prisoners must decide separately whether to confess or not confess to a crime. This is shown in Figure 5.6

		PRISONER B	
		CONFESS	NOT CONFESS
PRISONER A	CONFESS	(8,8)	(1, 15)
	NOT CONFESS	(15,1)	(3,3)

Figure 5.6 A Prisoner's Dilemma

The police have some evidence that the two prisoners committed a crime, but not enough evidence to convict for a long jail sentence. The police seek a confession from each prisoner independently to convict the other accomplice. The outcomes, or payoffs, of this game are shown as years of jail sentences in the format (A, B) where A is the number of years Prisoner A is sentenced to jail, and B is the number of years Prisoner B

is sentenced to jail. The intuition of the game is that if the two Prisoners “collude” and jointly decide to not confess, they will both receive a shorter jail sentence of three years. However, if either prisoner decides to not confess, the confessing prisoner would receive only a single year sentence for cooperating, and the partner in crime would receive a long 15-year sentence. If both prisoners confess, each receives a sentence of 8 years. This story forms the plot line of a large number of television shows and movies. The situation described by the prisoner’s dilemma is also common in many social and business interactions, as will be explored in the next chapter.

The outcome of this situation is uncertain. If both prisoners are able to strike a deal, and “collude,” or act cooperatively, they both choose to NOT CONFESS, and they each receive three year sentences, in the lower right hand outcome of Figure 5.6. This is the cooperative agreement: (NOT, NOT) = (3,3). However, once the prisoners are in this outcome, they have a temptation to “cheat” on the agreement by choosing to CONFESS, and reducing their own sentence to a single year at the expense of their partner. How should a prisoner proceed? One way is to work through all of the possible outcomes, given what the other prisoner chooses.

A Solution to the Prisoner’s Dilemma: Dominant Strategy

1. If B CONF, A should CONF ($8 < 15$)
2. If B NOT, A should CONF ($1 < 3$)
 ...A has the same strategy no matter what B does.
3. If A CONF, B should CONF ($8 < 15$)
4. If A NOT, B should CONF ($1 < 3$)
 ...B has the same strategy no matter what A does.

Thus, A chooses to CONFESS no matter what. This is called a Dominant Strategy, since it is the best choice given any of the strategies selected by the other player. Similarly, CONFESS is the dominant strategy for prisoner B.

Dominant Strategy = A strategy that results in the highest payoff to a player regardless of the opponent’s action.

The Equilibrium in Dominant Strategies for the Prisoner’s Dilemma is (CONF, CONF). This is an interesting outcome, since each prisoner receives eight-year sentences. If they could only cooperate, they could both be better off with much lighter sentences of three years.

A second example of a game is the decision of whether to produce natural beef or not. Natural beef is typically defined as beef produced without antibiotics or growth hormones. The definition is difficult, since it means different things to different people, and there is no common legal definition. This game is shown in Figure 5.7, where Cargill and Tyson decide whether to produce natural beef.

		TYSON	
		NATURAL	NO NATURAL
CARGILL	NATURAL	(10,10)	(12,8)
	NO NATURAL	(8,12)	(6,6)

Figure 5.7 The Decision to Produce Natural Beef

There are two players in the game: Cargill and Tyson. Each firm has two possible strategies: produce natural beef or not. The payoffs in the payoff matrix are profits (million USD) for the two companies: $(\pi_{\text{Cargill}}, \pi_{\text{Tyson}})$.

Strategy = Each player's plan of action for playing a game.

Outcome = A combination of strategies for players.

Payoff = The value associated with possible outcomes.

In this game, profits are made from the premium associated with natural beef. If only one firm produced natural beef,

Dominant Strategy for the Natural Beef Game

1. If TYSON NAT, CARGILL should NAT ($10 > 8$)
2. If TYSON NOT, CARGILL should NAT ($12 > 6$)
...CARGILL has the same strategy no matter what TYSON does.
3. If CARGILL NAT, TYSON should NAT ($10 > 8$)
4. If CARGILL NOT, TYSON should NAT ($12 > 6$)
...TYSON has the same strategy no matter what CARGILL does.

Both firms choose to produce natural beef, no matter what, so this is a Dominant Strategy for both firms. The Equilibrium in Dominant Strategies is (NAT, NAT). The outcome of this game demonstrates why all beef processors have moved quickly into

the production of natural beef in the past few years, and are all earning higher levels of profits.

Prisoner's Dilemmas are very common in oligopoly markets: gas stations, grocery stores, garbage companies are frequently in this situation. If all oligopolists in a market could agree to raise the price, they could all earn higher profits. Collusion, or the cooperative outcome, could result in monopoly profits. In the USA, explicit collusion is illegal. "Price setting" is outlawed to protect consumers. However, implicit collusion (tacit collusion) could result in monopoly profits for firms in a prisoner's dilemma. For example, if gas stations in a city such as Manhattan, Kansas all matched a higher price, they could all make more money. However, there is an incentive to cheat on this implicit agreement by cutting the price and attracting more customers away from the other firms to your own gas station. Firms in a cooperative agreement are always tempted to break the agreement to do better.

The Nash Equilibrium calculated for the three oligopoly models (Cournot, Bertrand, and Stackelberg) is a noncooperative equilibrium, as the firms are rivals and do not collude. In these models, firms maximize profits given the actions of their rivals. This is common, since collusion is illegal and price wars are costly. How do real-world oligopolists deal with prisoner's dilemmas is the topic of the next section.

5.3.6 Rigid Prices: Kinked Demand Curve Model

Oligopolists have a strong desire for price stability. Firms in oligopolies are reluctant to change prices, for fear of a price war. If a single firm lowers its price, it could lead to the Bertrand equilibrium, where price is equal to marginal costs, and economic profits are equal to zero. The kinked demand curve model was developed to explain price rigidity, or oligopolist's desire to maintain price at the prevailing price, P^* .

The kinked demand model asserts that a firm will have an asymmetric reaction to price changes. Rival firms in the industry will react differently to a price change, which results in different elasticities for price increases and price decreases.

1. If a firm increases price, $P > P^*$, other firms will not follow
... the firm will lose most customers, the demand is highly elastic above P^*
2. If a firm decreases price, $P < P^*$, other firms will follow immediately
...each firm will keep the same customers, demand is inelastic below P^*

The kinked demand curve is shown in Figure 5.8, where the different reactions of other firms leads to a kink in the demand curve at the prevailing price P^* .

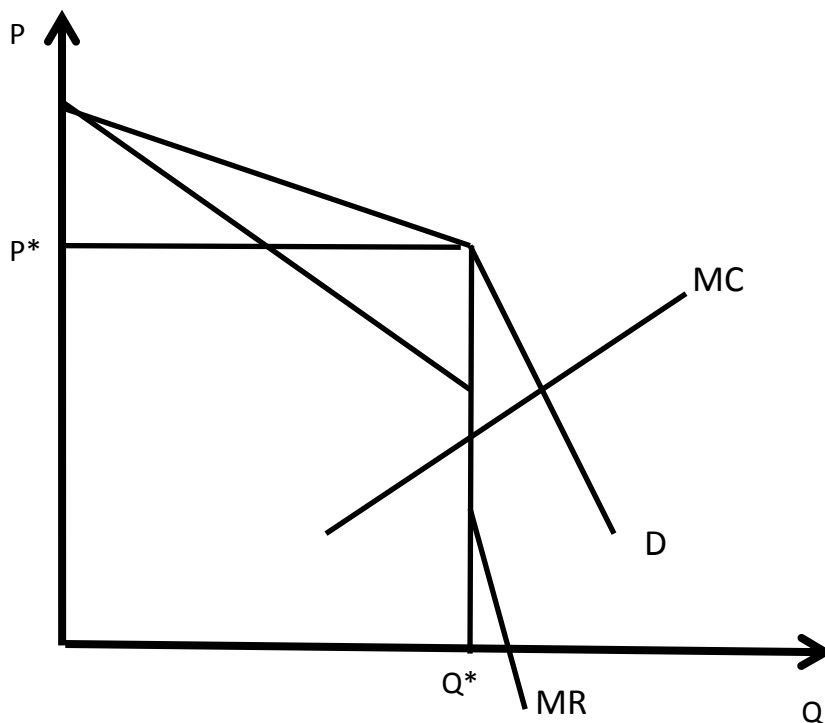


Figure 5.8 Kinked Demand Curve Model

In the kinked demand curve model, MR is discontinuous, due to the asymmetric nature of the demand curve. For linear demand curves, MR has the same y-intercept and two times the slope... resulting in two different sections for the MR curve when demand has a kink. The graph shows how price rigidity occurs: any changes in marginal cost result in the same price and quantity in the kinked demand curve model. As long as the MC curve stays between the two sections of the MR curve, the optimal price and quantity will remain the same.

One important feature of the kinked demand model is that the model describes price rigidity, but does not explain it with a formal, profit-maximizing model. The explanation for price rigidity is rooted in the prisoner's dilemma and the avoidance of a price war, which are not part of the kinked demand curve model. The kinked demand model is criticized because it is not based on profit-maximizing foundations, as the other oligopoly models.

Two additional models of pricing are price signaling and price leadership.

Price Signaling = A form of implicit collusion in which a firm announces a price increase in the hope that other firms will follow suit.

Price signaling is common for gas stations and grocery stores, where price are posted publically.

Price Leadership = A form of pricing where one firm, the leader, regularly announces price changes that other firms, the followers, then match.

There are many examples of price leadership, including General Motors in the automobile industry, local banks may follow a leading bank's interest rates, and US Steel in the steel industry.

5.3.7 Dominant Firm Model: Price Leadership

A dominant firm is defined as a firm with a large share of total sales that sets a price to maximize profits, taking into account the supply response of smaller firms. The dominant firm model is also known as the price leadership model. The smaller firms are referred to as the "fringe." Let F = fringe, or many competing firms in the same industry as the dominant firm. Let Dom = the dominant firm. The market demand for the good (D_{mkt}) is equal to the sum of the demand facing the dominant firm (D_{dom}) and the demand facing the fringe firms (D_{F}).

$$D_{\text{dom}} = D_{\text{mkt}} - D_{\text{F}}$$

Total quantity (Q_{T}) is also the sum of output produced by the dominant and fringe firms.

$$Q_{\text{T}} = Q_{\text{dom}} + Q_{\text{F}}$$

The dominant firm model is shown in Figure 5.9. The supply curve for the fringe firms is given by S_{F} , and the marginal cost of the dominant firm is MC_{dom} . The dominant firm has the advantage of lower costs due to economies of scale. In what follows, the dominant firm will set a price, allow the fringe firms to produce as much as they desire, and then find the profit-maximizing quantity and price with the remainder of the market.

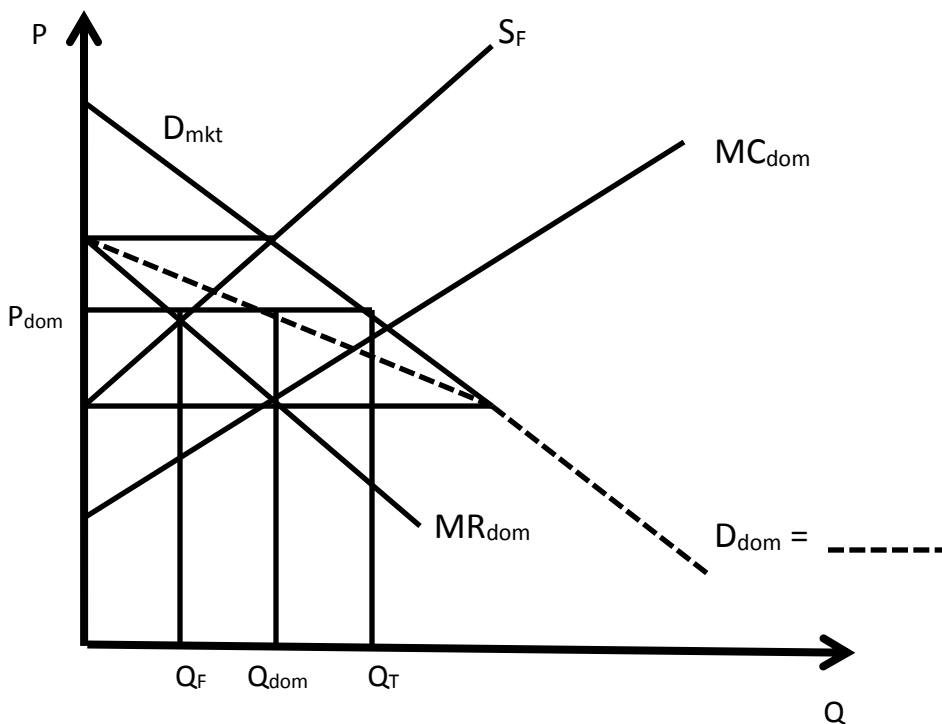


Figure 5.9 The Dominant Firm Model

To find the profit-maximizing level of output, the dominant firm first finds the demand curve facing the dominant firm (the dashed line in Figure 5.9), then sets marginal revenue equal to marginal cost. The dominant firm's demand curve is found by subtracting the supply of the fringe firms (S_F) from the total market demand (D_{mkt}).

The dominant firm demand curve is found by the following procedure. The y-intercept of the dominant firm's demand curve occurs where S_F is equal to the D_{mkt} . At this point, the fringe firms supply the entire market, so the residual facing the dominant firm is equal to zero. Therefore, the demand curve of the dominant firm starts at the price where fringe supply equals market demand. The second point on the dominant firm demand curve is found at the y-intercept of the fringe supply curve (S_F). At any price equal to or below this point, the supply of the fringe firms is equal to zero, since the supply curve represents the cost of production. At this point, and all prices below this point, the market demand (D_{mkt}) is equal to the dominant firm demand (D_{dom}). Thus, the dashed line below the y-intercept of the fringe supply is equal to the market demand curve. The dominant firm demand curve for prices above this point is found by drawing a line from the y-intercept at price ($S_F = D_{mkt}$) to the point on the market

demand curve at the price of the S_F y-intercept. This is the dashed line above the S_F y-intercept.

Once the dominant firm demand curve is identified, the dominant firm maximizes profits by setting marginal revenue equal to marginal cost at quantity Q_{dom} . This level of output is then substituted into the dominant firm demand curve to find the price P_{dom} . The fringe firms take this price as given, and produce Q_F . The sum of Q_{dom} and Q_F is the total output Q_T .

In this way, the dominant firm takes into account the reaction of the fringe firms while making the output decision. This is a Nash equilibrium for the dominant firm, since it is taking the other firms' behavior into account while making its strategic decision. The model effectively captures an industry with one dominant firm and many smaller firms.

5.3.8 Cartels

A cartel is a group of firms that have an explicit agreement to reduce output in order to increase the price.

Cartel = An explicit agreement among members to reduce output to increase the price.

Cartels are illegal in the United States, as the cartel is a form of collusion. The success of the cartel depends upon two things: (1) how well the firms cooperate, and (2) the potential for monopoly power (inelastic demand).

Cooperation among cartel members is limited by the temptation to cheat on the agreement. The Organization of Petroleum Exporting Countries (OPEC) is an international cartel that restricts oil production to maintain high oil prices. This cartel is legal, since it is outside of the American legal system. The oil cartel's success depends on how well each member nation adheres to the agreement. Frequently, one or more member nations increases oil production above the agreement, putting downward pressure on oil prices. The cartel's success is limited by the temptation to cheat. This cartel characteristic is that of a prisoner's dilemma, and collusion can be best understood in this way.

A collusive agreement, or cartel, results in a circular flow of incentives and behavior. When firms in the same industry act independently, they each have an incentive to collude, or cooperate, to achieve higher levels of profits. If the firms can jointly set the

monopoly output, they can share monopoly profit levels. When firms act together, there is a strong incentive to cheat on the agreement, to make higher individual firm profits at the expense of the other members. The business world is competitive, and as a result oligopolistic firms will strive to hold collusive agreements together, when possible. This type of strategic decisions can be usefully understood with game theory, the subject of the next Chapter.

Chapter 6. Game Theory One

6.1 Game Theory Introduction

Game theory was introduced to better understand oligopoly. Recall the definition of game theory.

Game Theory = A framework to study strategic interactions between players, firms, or nations.

Game theory is the study of strategic interactions between players. The key to understanding strategic decision making is to understand your opponent's point of view, and to deduce his or her likely responses to your actions.

A game is defined as:

Game = A situation in which firms make strategic decisions that take into account each other's actions and responses.

A payoff is the outcome of a game that depends of the selected strategies of the players.

Payoff = The value associated with a possible outcome of a game.

Strategy = A rule or plan of action for playing a game.

An optimal strategy is one that provides the best payoff for a player in a game.

Optimal Strategy = A strategy that maximizes a player's expected payoff.

Games are of two types: cooperative and noncooperative games.

Cooperative Game = A game in which participants can negotiate binding contracts that allow them to plan joint strategies.

Noncooperative Game = A game in which negotiation and enforcement of binding contracts are not possible.

In noncooperative games, individual players take actions, and the outcome of the game is described by the action taken by each player, along with the payoff that each player achieves. Cooperative games are different. The outcome of a cooperative game will be specified by which group of players become a cooperative group, and the joint action that that group takes. The groups of players are called coalitions. Examples of

noncooperative games include checkers, the prisoner's dilemma, and most business situations where there is competition for the payoff. An example of a cooperative game is a joint venture of several companies who band together to form a group.

The discussion of the prisoner's dilemma led to one solution to games, the equilibrium in dominant strategies. There are several different strategies and solutions for games, including:

1. Dominant strategy
2. Nash equilibrium
3. Maximin strategy (safety first, or secure strategy)
4. Cooperative strategy (collusion).

6.2 Equilibrium in Dominant Strategies

The dominant strategy was introduced in the previous chapter.

Dominant Strategy = A strategy that results in the highest payoff to a player regardless of the opponent's action.

Equilibrium in Dominant Strategies = An outcome of a game in which each firm is doing the best that it can regardless of what its competitor is doing

Recall the prisoner's dilemma from Chapter Five.

		PRISONER B	
		CONFESS	NOT CONFESS
PRISONER A	CONFESS	(8,8)	(1, 15)
	NOT CONFESS	(15,1)	(3,3)

Figure 6.1 A Prisoner's Dilemma

6.2.1 Prisoner's Dilemma: Dominant Strategy

1. If B CONF, A should CONF ($8 < 15$)
2. If B NOT, A should CONF ($1 < 3$)
...A has the same strategy (CONF) no matter what B does.
3. If A CONF, B should CONF ($8 < 15$)

4. If A NOT, B should CONF ($1 < 3$)
 - ...B has the same strategy (CONF) no matter what A does.

Thus, the equilibrium in dominant strategies for this game is (CONF, CONF) = (8,8).

6.3 Nash Equilibrium

A second solution to games is a Nash Equilibrium.

Nash Equilibrium = A set of strategies in which each player has chosen its best strategy given the strategy of its rivals.

To solve for a Nash Equilibrium:

- (1) Check the outcomes of a game to see if any player wants to change strategies, given the strategy of its rival.
 - a. If no player wants to change, the outcome is a Nash Equilibrium.
 - b. If one or more player wants to change, the outcome is not a Nash Equilibrium.

A game may have zero, one, or more than one Nash Equilibria. The Prisoner's Dilemma is shown in Figure 6.1. We will review the dominant strategy, and then determine if this game has any Nash Equilibria.

6.3.1 Prisoner's Dilemma: Nash Equilibrium

1. Outcome = (CONF, CONF)
 - a. Is CONF best for A given B CONF? Yes.
 - b. Is CONF best for B given A CONF? Yes.

...(CONF, CONF) is a Nash Equilibrium.
2. Outcome = (CONF, NOT)
 - a. Is CONF best for A given B NOT? Yes.
 - b. Is NOT best for B given A CONF? No.

...(CONF, NOT) is not a Nash Equilibrium.

3. Outcome = (NOT, CONF)
 - a. Is NOT best for A given B CONF? No.
 - b. Is CONF best for B given A NOT? Yes.

...(NOT, CONF) is not a Nash Equilibrium.
4. Outcome = (NOT, NOT)
 - a. Is NOT best for A given B NOT? No.
 - b. Is NOT best for B given A NOT? No.

...(NOT, NOT) is not a Nash Equilibrium.

Therefore, (CONF, CONF) is a Nash Equilibrium, and the only one Nash Equilibrium in the Prisoner's Dilemma game. Note that in the Prisoner's Dilemma game, the Equilibrium in Dominant Strategies is also a Nash Equilibrium.

6.4 Advertising Game

In this advertising game, two computer software firms (Microsoft and Apple) decide whether to advertise or not. The outcomes depend on their own selected strategy and the strategy of the rival firm.

		APPLE	
		ADVERTISE	NO ADVERTISE
MICROSOFT	ADVERTISE	(20, 20)	(10, 5)
	NO ADVERTISE	(5, 10)	(14, 14)

Figure 6.2 Advertising: Two Software Firms. Outcomes in million USD.

6.4.1 Advertising: Dominant Strategy

1. If APP AD, MIC should AD ($20 > 5$)
2. If APP NOT, MIC should NOT ($14 > 10$)

...different strategies, so no dominant strategy for Microsoft.
3. If MIC AD, APP should AD ($20 > 5$)
4. If MIC NOT, APP should NOT ($14 > 10$)

...different strategies, so no dominant strategy for Apple.

Thus, there are no dominant strategies, and no equilibrium in dominant strategies for this game.

6.4.2 Advertising: Nash Equilibria

1. Outcome = (AD, AD)
 - a. Is AD best for MIC given APP AD? Yes.
 - b. Is AD best for APP given MIC AD? Yes.

...(AD, AD) is a Nash Equilibrium.
2. Outcome = (AD, NOT)
 - a. Is AD best for MIC given APP NOT? No.
 - b. Is NOT best for APP given MIC AD? No.

...(AD, NOT) is not a Nash Equilibrium.
3. Outcome = (NOT, AD)
 - a. Is NOT best for MIC given APP AD? No.
 - b. Is AD best for APP given MIC NOT? No.

...(NOT, AD) is not a Nash Equilibrium.
4. Outcome = (NOT, NOT)
 - a. Is NOT best for MIC given APP NOT? Yes.
 - b. Is NOT best for APP given MIC NOT? Yes.

...(NOT, NOT) is a Nash Equilibrium.

There are two Nash Equilibria in the Advertising game: (AD, AD) and (NOT, NOT). Therefore, in the Advertising game, there are two Nash Equilibria, and no Equilibrium in Dominant Strategies.

It can be proven that in game theory, every Equilibrium in Dominant Strategies is a Nash Equilibrium. However, a Nash Equilibrium may or may not be an Equilibrium in Dominant Strategies.

6.5 Maximin Strategy (Safety First)

A strategy that allows players to avoid the largest losses is the Maximin Strategy.

Maximin Strategy = A strategy that maximizes the minimum payoff for one player.

The maximin, or safety first, strategy can be found by identifying the worst possible outcome for each strategy. Then, choose the strategy where the lowest payoff is the highest.

6.5.1 Prisoner's Dilemma: Maximin Strategy (Safety First)

1. Player A

- a. If CONF, worst payoff = 8 years.
- b. If NOT, worst payoff = 15 years.

...A's Maximin Strategy is CONF ($8 < 15$).

2. Player B

- a. If CONF, worst payoff = 8 years.
- b. If NOT, worst payoff = 15 years.

...B's Maximin Strategy is CONF ($8 < 15$).

Therefore, the Maximin Equilibrium is (CONF, CONF). This outcome is also an Equilibrium in Dominant Strategies, and a Nash Equilibrium.

6.5.2 Advertising Game: Maximin Strategy (Safety First)

1. MICROSOFT

- a. If AD, worst payoff = 10.
- b. If NOT, worst payoff = 5.

...MICROSOFT's Maximin Strategy is AD ($5 < 10$).

2. APPLE

- a. If AD, worst payoff = 10.
- b. If NOT, worst payoff = 5.

...APPLE's Maximin Strategy is AD ($5 < 10$).

Therefore, the Maximin Equilibrium is (AD, AD). Recall that this outcome is one of two Nash Equilibria in the advertising game: (AD, AD) and (NOT, NOT). If both players choose Maximin, there is only one equilibrium: (AD, AD).

The relationships between the game theory strategies can be summarized:

1. An Equilibrium in Dominant Strategies is always a Maximin Equilibrium.
2. A Maximin Equilibrium is NOT always an Equilibrium in Dominant Strategies.
3. An Equilibrium in Dominant Strategies is always a Nash Equilibrium.

4. A Nash Equilibrium is NOT always an Equilibrium in Dominant Strategies.

6.6 Cooperative Strategy (Collusion)

The cooperative strategy is defined as the best joint outcome for both players together.

Cooperative Strategy = A strategy that leads to the highest joint payoff for all players.

Thus, the cooperative strategy is similar to collusion, where players work together to achieve the best joint outcome. In the Prisoner's Dilemma, the cooperative outcome is found by summing the two players' outcomes together, and finding the outcome that has the smallest jail sentence for the prisoners together: (NOT, NOT) = (3, 3).

This outcome is the collusive solution, which provides the best outcome if the prisoners could make a joint decision and stick with it. Of course, there is always the temptation to cheat on the agreement, where each player does better for themselves, at the expense of the other prisoner.

Similarly, the cooperative outcome in the advertising game is (AD, AD) = (20, 20). This outcome provides the highest profits to both firms. The advertising game is not a prisoner's dilemma, since there is no incentive to cheat once the cooperative solution has been achieved.

6.7 Game Theory Example: Steak Pricing Game

A pricing game for steaks is shown in Figure 6.3. In this game, two beef processors, Tyson and JBS, are determining what price to charge for steaks. Suppose that these two firms are the major players in this steak market, and the outcomes depend on the strategies of both firms, since players choose which company to purchase from based on price. If both firms choose low prices, the outcome is low profits. Additional profits are earned by choosing high prices. However, when both firms have high prices, there is an incentive to undercut the other firm with a low price, to increase profits at the expense of the other firm.

		TYSON	
		LOW	HIGH
JBS	LOW	(2, 2)	(12, 0)
	HIGH	(0, 12)	(10, 10)

Figure 6.3 Steak Pricing Game: Two Beef Firms. Outcomes in million USD.

6.7.1 Steak Pricing Game: Dominant Strategy

1. If TYSON LOW, JBS should LOW ($2 > 0$)
2. If TYSON HIGH, JBS should LOW ($12 > 10$)
...the dominant strategy for TYSON is LOW.
3. If JBS LOW, TYSON should LOW ($2 > 0$)
4. If JBS HIGH, TYSON should LOW ($12 > 10$)
... the dominant strategy for JBS is LOW.

The Equilibrium in Dominant Strategies for the Steak Pricing game is (LOW, LOW). This is an unexpected result, since it is a less desirable scenario than (HIGH, HIGH) for both firms. We have seen that an Equilibrium in Dominant Strategies is also a Nash Equilibrium and a Minimax Equilibrium. These results will be checked in what follows.

6.7.2 Steak Pricing Game: Nash Equilibrium

1. Outcome = (LOW, LOW)
 - a. Is LOW best for JBS given TYSON LOW? Yes.
 - b. Is LOW best for TYSON given JBS LOW? Yes.
 ... (LOW, LOW) is a Nash Equilibrium.
2. Outcome = (LOW, HIGH)
 - a. Is LOW best for JBS given TYSON HIGH? Yes.
 - b. Is HIGH best for TYSON given JBS LOW? No.
 ... (LOW, HIGH) is not a Nash Equilibrium.
3. Outcome = (HIGH, LOW)

- a. Is HIGH best for JBS given TYSON LOW? No.
- b. Is LOW best for TYSON given JBS HIGH? Yes.

...(HIGH, LOW) is not a Nash Equilibrium.

4. Outcome = (HIGH, HIGH)

- a. Is HIGH best for JBS given TYSON HIGH? No.
- b. Is HIGH best for TYSON given JBS HIGH? No.

...(HIGH, HIGH) is not a Nash Equilibrium.

Therefore, there is only one Nash Equilibrium in the Steak Pricing game: (LOW, LOW).

6.7.3 Steak Pricing Game: Maximin Equilibrium (Safety First)

1. JBS

- a. If LOW, worst payoff = 2.
- b. If HIGH, worst payoff = 0.

...JBS' Maximin Strategy is LOW ($0 < 2$).

2. TYSON

- a. If LOW, worst payoff = 2.
- b. If HIGH, worst payoff = 0.

...TYSON's Maximin Strategy is LOW ($0 < 2$).

The Maximin Equilibrium in the Steak Pricing game is (LOW, LOW). Interestingly, if both firms cooperated, they could achieve much higher profits.

6.7.4 Steak Pricing Game: Cooperative Equilibrium (Collusion)

Both JBS and Tyson can see that if they were to cooperate, either explicitly or implicitly, profits would increase significantly. The cooperative outcome is (HIGH, HIGH) = (10,10). This is the outcome with the highest combined profits. Both firms are better off in this outcome, but each firm has an incentive to cheat on the agreement to increase profits from 10 m USD to 12 m USD.

Chapter 6. Game Theory Two

6.8 Repeated Games

A game that is played only once is called a “one-shot” game. Repeated games are games that are played over and over again.

Repeated Game = A game in which actions are taken and payoffs received over and over again.

Many oligopolists and real-life relationships can be characterized as a repeated game. Strategies in a repeated game are often more complex than strategies in a one-shot game, as the players need to be concerned about the reactions and potential retaliations of other players. As such, the players in repeated games are likely to choose cooperative or “win-win” strategies more often than in one shot games. Examples include concealed carry gun permits: are you more likely to start a fight in a no-gun establishment, or one that allows concealed carry guns? Franchises such as McDonalds were established to allow consumers to get a common product and quality at locations new to them. This allows consumers to choose a product that they know will be the same, given the repeated game nature of the decision to purchase meals at McDonalds.

6.9 Sequential Games

A sequential game is played in “turns,” or “rounds” like chess or checkers, where each player takes a turn.

Sequential Game = A game in which players move in turns, responding to each others’ actions and reactions.

6.9.1 Product Choice Game One

An example of a sequential game is the product choice game shown in Figure 6.4.

		GENERAL MILLS	
		WHEAT	OAT
KELLOGGS	WHEAT	(-5, -5)	(10, 10)
	OAT	(10, 10)	(-5, -5)

Figure 6.4 Product Choice Game One: Cereal. Outcomes are in million USD.

In this game, two cereal producers (Kelloggs and General Mills) decide whether to produce and sell cereal made from wheat or oats. If both firms select the same category, both firms lose five million USD, since they have flooded the market with too much cereal. However, the two firms split the two markets, with one firm producing wheat cereal and the other firm producing oat cereal, both firms earn ten million USD. In this situation, it helps both firms if they can decide which firm goes first, to signal to the other firm. It does not matter which firm produces wheat or oat cereal, as long as the two firms divide the two markets. This type of repeated game can be solved by one firm going first, or signaling to the other firm which product it will produce, and letting the other firm take the other market.

6.9.2 Product Choice Game Two

It might be that one of the two markets is more valuable than the other. This situation is shown in Figure 6.5.

		GENERAL MILLS	
		WHEAT	OAT
KELLOGGS	WHEAT	(-5, -5)	(10, 20)
	OAT	(20, 10)	(-5, -5)

Figure 6.5 Product Choice Game Two: Cereal. Outcomes are in million USD.

This cereal market game is very similar to the previous game, but in this case the oat cereal market is worth much more than the wheat cereal market. As in the Product Choice One game, if both firms select the same market, both lose five million USD. Similarly, if each firm chooses a different market, then both firms make positive economic profits. The difference between the two product choice games is that the earnings are asymmetrical in the Product Choice Two game: the firm that is in the oat

cereal market earns 20 million USD, and the firm in the wheat cereal market earns 10 million USD. In this situation, both firms will want to choose OAT first. If Kelloggs is able to choose OAT first, then it is in General Mill's best interest to select WHEAT. The player in this sequential game who goes first has a first player advantage, worth ten million USD. Each firm would be willing to pay up to ten million USD for the right to select first. In a repeated game, the market stabilizes with one firm producing oat cereal, and the other firm producing wheat cereal. There is no advantage for either firm to switch strategies, unless the firm can play OAT first, causing the other firm to move into wheat cereal.

6.10 First Mover Advantage

The first mover advantage is similar to the Stackelberg model of oligopoly, where the leader firm had an advantage over the follower firm. In many oligopoly situations, it pays to go first by entering a market before other firms. In many situations, it pays to determine the firm's level of output first, before other firms in the industry can decide how much to produce. Game theory demonstrates how many real-world firms determine their output levels in an oligopoly.

6.10.1 First Mover Advantage Example: Ethanol

Ethanol provides a good example of the first-mover advantage. Consider an ethanol market that is a Stackelberg duopoly. To review the Stackelberg model, assume that there are two ethanol firms in the same market, and the inverse demand for ethanol is given by $P = 120 - 2Q$, where P is the price of ethanol in USD/gallon, and Q is the quantity of ethanol in million gallons. The cost of producing ethanol is given by $C(Q) = 12Q$, and total output is the sum of the two individual firm outputs: $Q = Q_1 + Q_2$.

First, suppose that the two firms are identical, and they are Cournot duopolists. To solve this model, Firm One maximizes profits:

$$\max \pi_1 = TR_1 - TC_1$$

$$\max \pi_1 = P(Q)Q_1 - C(Q_1) \quad [\text{price depends on total output } Q = Q_1 + Q_2]$$

$$\max \pi_1 = [120 - 2Q]Q_1 - 12Q_1$$

$$\max \pi_1 = [120 - 2Q_1 - 2Q_2]Q_1 - 12Q_1$$

$$\max \pi_1 = 120Q_1 - 2Q_1^2 - 2Q_2Q_1 - 12Q_1$$

$$\partial\pi_1/\partial Q_1 = 120 - 4Q_1 - 2Q_2 - 12 = 0$$

$$4Q_1 = 108 - 2Q_2$$

$$Q_1^* = 27 - 0.5Q_2 \text{ million gallons of ethanol}$$

This is Firm One's reaction function. Assuming identical firms, by symmetry:

$$Q_2^* = 27 - 0.5Q_1$$

The solution is found through substitution of one equation into the other.

$$Q_1^* = 27 - 0.5(27 - 0.5Q_1)$$

$$Q_1^* = 27 - 13.5 + 0.25Q_1$$

$$Q_1^* = 13.5 + 0.25Q_1$$

$$0.75Q_1^* = 13.5$$

$$Q_1^* = 18$$

Due to symmetry from the assumption of identical firms:

$$Q_i = 18 \text{ million gallons of ethanol, } i = 1,2$$

$$Q = 36 \text{ million gallons of ethanol}$$

$$P = 48 \text{ USD/gallon ethanol}$$

Profits for each firm are:

$$\pi_i = P(Q)Q_i - C(Q_i) = 48(18) - 12(18) = (48 - 12)18 = 36(18) = 648 \text{ million USD}$$

This result shows that if each firm produces 18 million gallons of ethanol, each firm will earn 648 million USD in profits. This is shown in Figure 6.6, where several different possible output levels are shown as strategies for Firm A and Firm B, together with payoffs. Next, suppose that the two firms are not identical, and that one firm is a leader and the other is the follower. By calculating the Stackelberg model solution, the possible outcomes of the game can be derived, as shown in Figure 6.6.

In the Stackelberg model, assume that Firm One is the leader and Firm Two is the follower. In this case, Firm One solves for Firm Two's reaction function:

$$\max \pi_2 = TR_2 - TC_2$$

$$\max \pi_2 = P(Q)Q_2 - C(Q_2) \quad [\text{price depends on total output } Q = Q_1 + Q_2]$$

$$\max \pi_2 = [120 - 2Q]Q_2 - 12Q_2$$

$$\max \pi_2 = [120 - 2Q_1 - 2Q_2]Q_2 - 12Q_2$$

$$\max \pi_2 = 120Q_2 - 2Q_1Q_2 - 2Q_2^2 - 12Q_2$$

$$\partial\pi_2/\partial Q_2 = 120 - 2Q_1 - 4Q_2 - 12 = 0$$

$$4Q_2 = 108 - 2Q_1$$

$$Q_2^* = 27 - 0.5Q_1$$

Next, Firm One, the leader, maximizes profits holding the follower's output constant using the reaction function:

$$\max \pi_1 = TR_1 - TC_1$$

$$\max \pi_1 = P(Q)Q_1 - C(Q_1) \quad [\text{price depends on total output } Q = Q_1 + Q_2]$$

$$\max \pi_1 = [120 - 2Q]Q_1 - 12Q_1$$

$$\max \pi_1 = [120 - 2Q_1 - 2Q_2]Q_1 - 12Q_1$$

$$\max \pi_1 = [120 - 2Q_1 - 2(27 - 0.5Q_1)]Q_1 - 12Q_1 \quad [\text{substitution of One's reaction function}]$$

$$\max \pi_1 = [120 - 2Q_1 - 54 + Q_1]Q_1 - 12Q_1$$

$$\max \pi_1 = [66 - Q_1]Q_1 - 12Q_1$$

$$\max \pi_1 = 66Q_1 - Q_1^2 - 12Q_1$$

$$\partial\pi_1/\partial Q_1 = 66 - 2Q_1 - 12 = 0$$

$$2Q_1^* = 54$$

$$Q_1^* = 27 \text{ million gallons of ethanol}$$

This can be substituted back into Firm Two's reaction function to solve for Q_2^* .

$$Q_2^* = 27 - 0.5Q_1 = 27 - 0.5(27) = 27 - 13.5 = 13.5 \text{ million gallons of ethanol}$$

$$Q = Q_1 + Q_2 = 27 + 13.5 = 40.5 \text{ million gallons of ethanol}$$

$$P = 120 - 2Q = 120 - 2(40.5) = 120 - 81 = 39 \text{ USD/gallon ethanol}$$

$$\pi_1 = (39 - 12)27 = 27(27) = 729 \text{ million USD}$$

$$\pi_2 = (39 - 12)13.5 = 27(13.5) = 364.5 \text{ million USD}$$

These results are displayed in Figure 6.6. In a one-shot game, the Nash Equilibrium is (18, 18), yielding payoffs of 648 million USD for each ethanol plant in the market. Each firm desires to select 18 million gallons, and have the other firm select 13.5 million gallons, in which case profits would increase to 810 million USD. However, the rival firm will not unilaterally cut production to 13.5, since it would lose profits at the expense of the other firm.

		FIRM B (m GAL)		
		13.5	18	27
FIRM A (m GAL)	13.5	(729, 729)	(607.5, 810)	(364.5, 729)
	18	(810, 364.5)	(648, 648)	(324, 486)
	27	(729, 364.5)	(486, 324)	(0, 0)

Figure 6.6 First-Mover Advantage: Ethanol. Outcomes are in million USD.

In a sequential game, if Firm A goes first, it will select 27 million gallons of ethanol. In this case, Firm B will choose to produce 13.5 million gallons of ethanol, which is the Stackelberg solution. Firm A, as the first mover, has increased profits from 648 to 729 million USD by being able to go first. This is the first mover advantage.

6.10.2 Empty Threat

Figure 6.7 shows a sequential game between two grain seed dealers: Monsanto, a large international agribusiness, and a Local Grower. Monsanto is the dominant firm, and chooses a pricing strategy first. If Monsanto selects a HIGH price strategy, the Local Grower will select a LOW price, and both firms are profitable. In this case, the Local Grower has the low price, so makes more money than Monsanto.

		LOCAL GROWER	
		HIGH PRICE	LOW PRICE
MONSANTO	HIGH PRICE	(100, 80)	(80, 100)
	LOW PRICE	(20, 0)	(10, 20)

Figure 6.7 Empty Threat: Grain Seed Dealers. Outcomes are in million USD.

Could Monsanto threaten the Local Grower that it would set a LOW price, to try to cause the Local Grower to set a HIGH price, and increasing Monsanto profits from 80 million USD to 100 million USD? Monsanto could threaten to set a LOW price, but it is not believable, since Monsanto would have very low payoffs in both outcomes. In this case, Monsanto's threat is an empty threat, since it is not credible.

6.10.3 Pre-Emptive Strike

Suppose two big box stores are considering entering a small town market in Kansas. If both Walmart and Target enter this market, both firms lose ten million USD, since the town is not large enough to support both firms. However, if one firm can enter the market first (a "pre-emptive strike"), it can gain the entire market and earn 20 million USD. The firm that goes first wins this game in a significant way. This explains why Walmart has opened so many stores in a large number of small cities.

		TARGET	
		ENTER	DON'T ENTER
WALMART	ENTER	(-10, -10)	(20, 0)
	DON'T ENTER	(0, 20)	(0, 0)

Figure 6.8 Pre-Emptive Strike: Big Box Stores. Outcomes are in million USD.

6.11 Commitment and Credibility

Figure 6.9 shows a sequential game between beef producers and beef packers. In this game, the packer is the leader, and decides to produce and sell LOW or HIGH quality beef.

		PACKERS	
		LOW QUALITY	HIGH QUALITY
PRODUCERS	LOW QUALITY	(20, 50)	(20, 5)
	HIGH QUALITY	(10, 10)	(40, 20)

Figure 6.9 Commitment and Credibility One: Beef Industry. Outcomes are in m USD.

If the packers go first, they will select LOW, since they know that by doing so, the producers would also select LOW. This results in 50 million USD for the packers and 20 million USD for the producers. The producers would prefer the outcome (HIGH, HIGH), as their profits would increase from 20 to 40 million USD. In this situation, the beef producers can threaten the packers by committing to producing HIGH quality beef only. The packers will select LOW if they do not believe the threat, in the attempt to achieve the outcome (LOW, LOW). However, if the producers can commit to the HIGH quality strategy, and prove to the packers that they will definitely choose HIGH quality, the packers would choose HIGH also, and the producers would achieve 40 million USD.

The producers could come up with a strategy of visibly and irreversibly reducing their own payoffs to prove to the packers that they are serious about HIGH quality, and cause the packers to choose HIGH also. This commitment, if credible, could change the outcome of the game, resulting in higher profits for the producers, at the expense of the packers. Such a credible commitment is shown in Figure 6.10, which replicates Figure 6.9 with the exception of the LOW outcomes for the producers. If the beef producers sell off their low quality herd, and have no low quality cattle, they change the sequential game from the one shown in Figure 6.9 to the one in Figure 6.10.

		PACKERS	
		LOW QUALITY	HIGH QUALITY
PRODUCERS	LOW QUALITY	(0, 50)	(0, 0)
	HIGH QUALITY	(10, 10)	(40, 20)

Figure 6.10 Commitment and Credibility Two: Beef Industry. Outcomes are in m USD.

If the packers are the leaders in Figure 6.10, they select the HIGH quality strategy. If they select LOW, the producers would choose HIGH, yielding 10 million USD for the packers. When the packers select HIGH, the packers earn 20 million USD. Therefore, a producer strategy of shutting down or destroying the low quality productive capacity results in the desired outcome for the producers: (HIGH, HIGH). The strategy of taking an action that appears to put a firm at a disadvantage can provide the incentives to increase the payoffs of a sequential game. This strategy can be effective, but is risky. The producers need accurate knowledge of the payoffs of each strategy.

The commitment and credibility game is related to barriers to entry in monopoly. A monopolist often has a strong incentive to keep other firms out of the market. The monopolist will engage in entry deterrence by making a credible threat of price warfare to deter entry of other firms. In many situations, a player who behaves irrationally and belligerently can keep rivals off balance, and change the outcome of a game.

A policy example of this type of strategy occurs during bargaining between politicians. If one issue is not going in a desired direction, a political group can bring in another issue to attempt to persuade the other party to compromise.

The “holdup game” is another example of commitment and credibility. Often, once significant resources are committed to a project, the investor will ask for more resources. If the project is incomplete, the funder will often agree to pay more money to have the project completed. Large building projects are often subject to the holdup game.

For example, if a contractor has been paid 20 million USD to build a campus building, and the project is only 50 percent complete, the contractor could halt construction, letting the half-way completed building sit unfinished, and ask for 10 million USD more, due to “cost overruns.” This strategy is often effective, even if a contract is carefully and legally drawn up ahead of time. The contractor has the University right where they want it: stuck with an unfinished building unless they increase the dollars to the project. The contractor is effectively saying, “do it my way, or I quit.”